

The parameters are b_1 and b_2 , the data are $\mathbf{y} = (y_1, \dots, y_{10})$ (and also \mathbf{x} , but the x values are treated as known in advance and not observed samples of a random variable, and hence are conditioned on throughout).

The posterior distribution of the parameters given the data is

$$\pi(b_1, b_2 | \mathbf{y}, \mathbf{x}) \propto \pi(\mathbf{y} | \mathbf{x}, b_1, b_2) \pi(b_1, b_2),$$

i.e. likelihood of data \times prior.

For the likelihood, note that each y_i (given \mathbf{x}, b_1, b_2) is of the form $y_i = \text{constant}_i + \epsilon_i$,

where ϵ_i is normal, so each y_i is also normal (with a particular mean and variance).

Finally, note that the y_i (given \mathbf{x}, b_1, b_2) are considered independent of each other.