

Exploring Air Friction and its Effects on Acceleration

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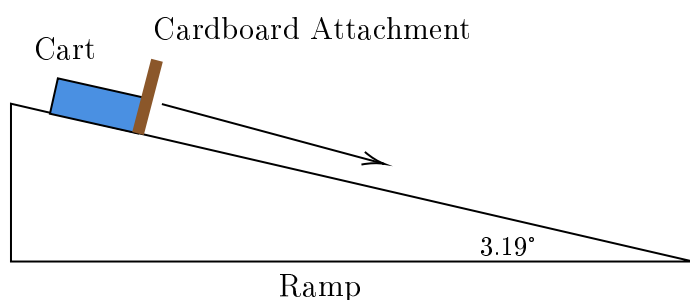
## Exploring Air Friction and its Effects on Acceleration

**Abstract**

In this experiment we studied the effects of increasing the cross-sectional area of a cart on its acceleration and velocity. Through this, we proved that air resistance exists and is directly correlated to the cross-sectional area of an object, as well as its shape. Furthermore, we found that air resistance can be decreased by keeping cross-sectional area constant and changing the shape of an object.

**Introduction**

Throughout high school physics, we have been calculating the range of projectiles, the velocity of carts, and even the acceleration of planes - all by assuming that air resistance is negligible. In this experiment, we set out to prove that air resistance does exist, and that it has a significant impact on acceleration and velocity of an object relative to its cross-sectional area

**Background**

*Figure 1.* General experimental setup with a Smart Cart rolling down a ramp.

Cross-sectional area of the cart is changed using a cardboard attachment.

Figure 1 shows the basic experimental configuration of this experiment. The cart was rolled down a ramp with an attachment on its front. Said attachment modified the cart's cross-sectional area as well as its aerodynamic properties.

We can break down the forces experienced by the cart into components 1 as shown in the free body diagram below.

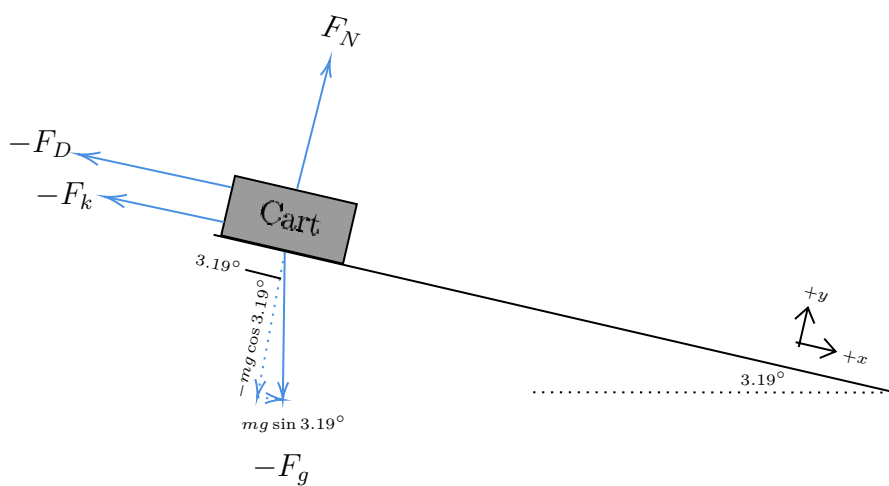


Figure 2. Free body diagram illustrating various forces acting upon the Smart Cart

In the free body diagram in figure 2, the cart is on the ramp, with the forces of air resistance ( $F_D$ ) and kinetic friction ( $F_k$ ) acting against the cart in the horizontal direction. The cart is also accelerated down the ramp by the horizontal component of gravity ( $mg \sin(3.19^\circ)$ ). Since the Smart Cart is on wheels, the wheels actually generate static friction against the ramp, but kinetic friction occurs within the axles. The exact force of friction is difficult to determine, however, we can use the average force of the cart with no attachments in order to determine the constant  $F$ . Given that the force of air resistance upon an object with a drag coefficient of  $K$  is  $Kv^2$ , the following equation can be derived to solve for the drag coefficient where acceleration and velocity are a function of time.

$$\begin{aligned}
 F_{\text{net}} &= mg \sin(\theta) - F_K - Kv(t)^2 \\
 F &= mg \sin(\theta) - F_K \\
 F &= \frac{\text{Average Force}}{\text{Mass of Cart with No Attachments}} \\
 ma(t) &= F - Kv(t)^2 \\
 F - ma(t) &= Kv(t)^2
 \end{aligned}$$

$$K = \frac{F - a(t)m}{v(t)^2} \quad (1)$$

### Methods

1. A 250g weight was taped onto the Smart Cart to make the effect of additional weight negligible
2. A 1.22m ramp was placed on top of a textbook so that it made a 3.19 degree angle with the lab bench counter
3. Depending on the trial being run, a cardboard attachment was measured and cut to proper dimensions and taped to the front of the Smart Car
4. The Smart Car's position, velocity, force, and acceleration were all recorded relative to time using Pasco Capstone software
5. Steps 3 and 4 were repeated eight more times until all trial data were successfully collected

## Results

Table 1

*K values relative to cross-sectional area and the shape of the attachment*

Attachment	Length	Width	Area (cm <sup>2</sup> )	K
None	3.	8.5	33.85	0.002
Orange	29	33	957	0.184
Cardboard	12	20.75	249	0.105
Cardboard	15.78	15.78	249	0.109
Orange Pocket	29	33	957	0.198
Equilateral Wedge	9.4	26.5	249	0.087
Sharp Wedge	9.4	26.5	249	0.050
Sharp Wedge on Orange	29	33	957	0.127

## Discussion

### Methodology

One unique part of our methodology that proved crucial to the statistical significance and accuracy of our data was the addition of a 250g weight on top of the Smart Cart. Adding the various cardboard attachments used to modify the aerodynamic properties of the Smart Cart would increase the total weight of our modified Smart Cart system. It would be possible to account for the variance in weight by measuring each cardboard attachment along with the tape used to affix it; however, a lack of time meant that it would be more efficient to make the additional weight negligible by increasing the overall weight of the Smart Cart itself. Although this may introduce some variance into our results, the relative effect of the additional weight is acceptable given how little the attachments weighed relative to the weighted Smart Cart.

### **Air Resistance**

A major goal of this experiment was to determine whether or not air resistance actually existed, or if it had enough of an effect to affect our data in a manner that was statistically significant. If air resistance were to exist and be statistically significant with respect to the data collected, then there should be a statistically significant decrease in acceleration due to the increasing drag forces. After collecting multiple sets of data and removing outliers based on inter-quartile ranges, the data for each trial were individually plotted on a graph. Specifically, when acceleration relative to time was plotted for each trial, as well as a linear regression for acceleration relative to time, it becomes clear that when cross-sectional area is increased, there is a time-dependent, increasing drag force that decreases acceleration. Referring to A3, A4, A5, A2, A6, A7, and A8, each of their respective linear regressions of acceleration all have negative slopes and decrease with respect to time - signifying an overall deceleration. Furthermore, when referring to the base case, A1, it can be seen that the slope of the linear regression of acceleration is practically zero. The base case did not have a cardboard attachment nor an increased cross-sectional area. This shows that increasing cross-sectional area will affect the aerodynamic properties of the cart, which will create drag forces that decelerate the cart.

### **Calculating the Drag Coefficient ( $K$ )**

## References

*What is hooke's law?* (n.d.). Retrieved March 7, 2020, from

<https://www.khanacademy.org/science/physics/work-and-energy/hookes-law/a/what-is-hookes-law>

## Appendix A

## Trial Charts

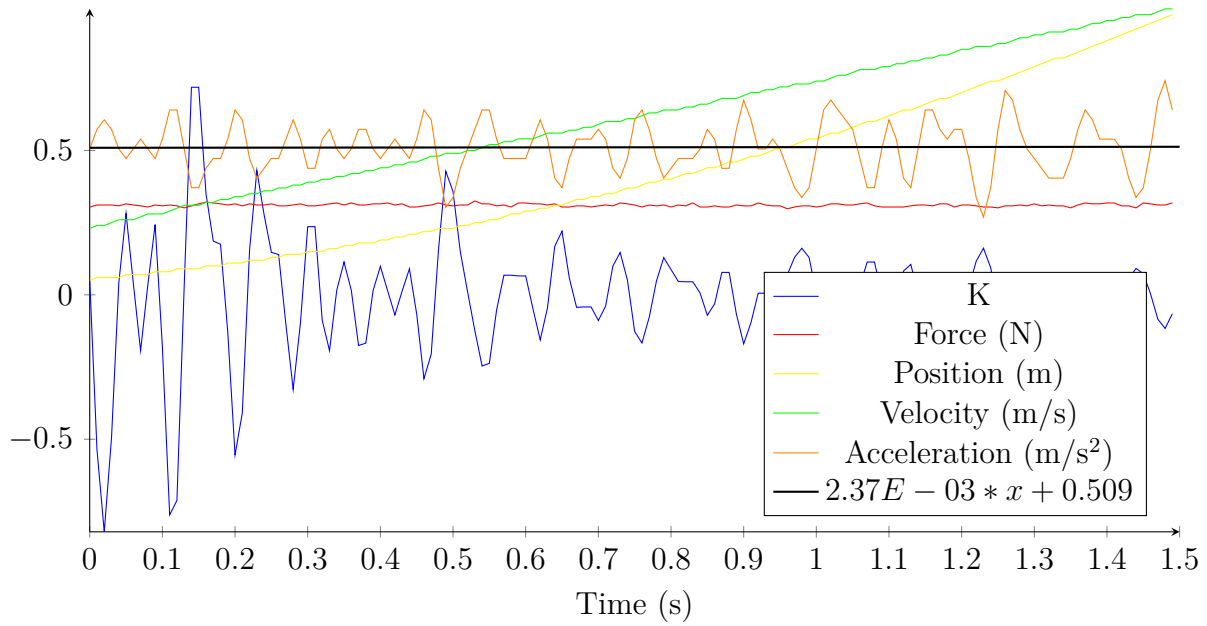
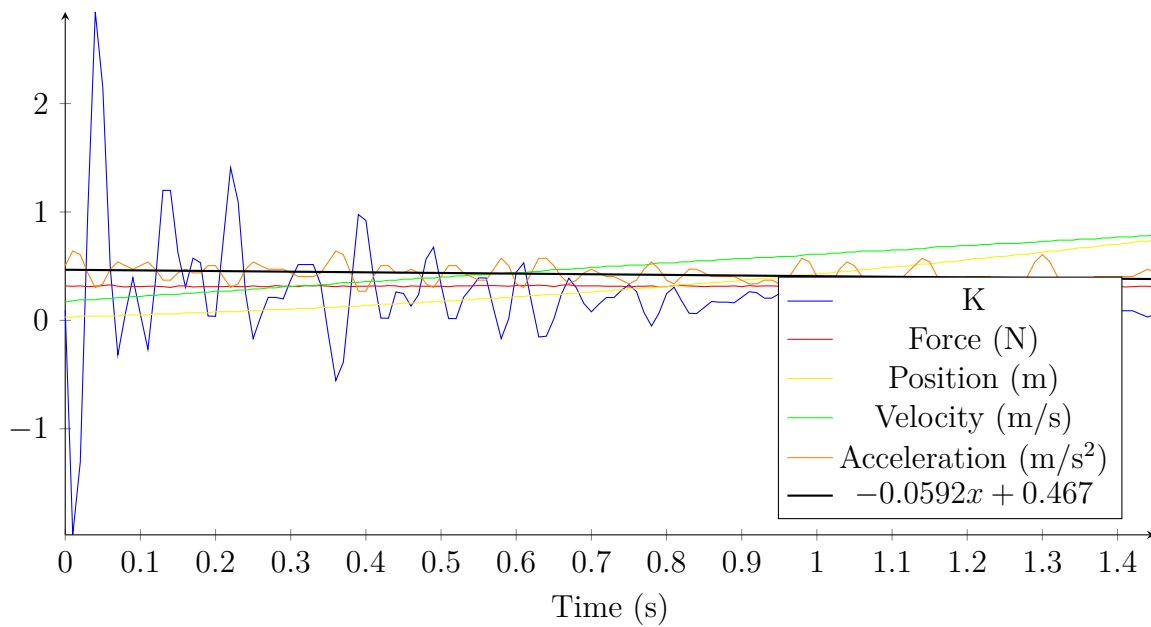
*Figure A1.* Raw Data Collected from Smart Cart and Calculated  $K$  value - No Attachment*Figure A2.* Raw Data Collected from Smart Cart and Calculated  $K$  value - Orange



Figure A3. Raw Data Collected from Smart Cart and Calculated  $K$  value - Cardboard (12 x 20.75)

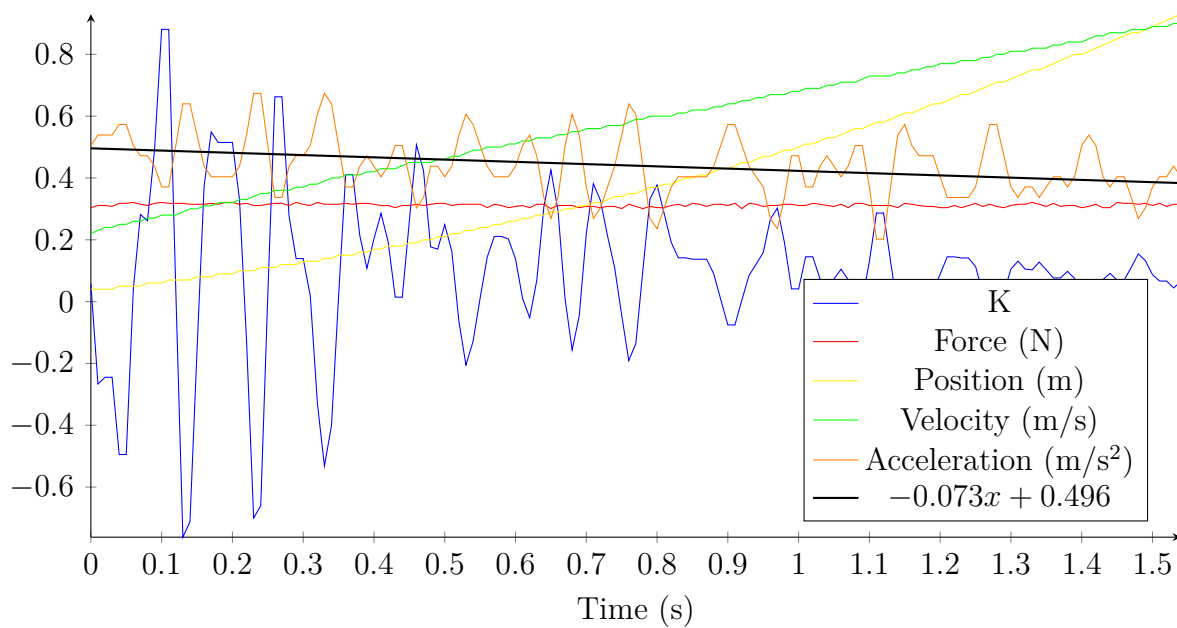


Figure A4. Raw Data Collected from Smart Cart and Calculated  $K$  value - Cardboard  
(15.78 x 15.78)

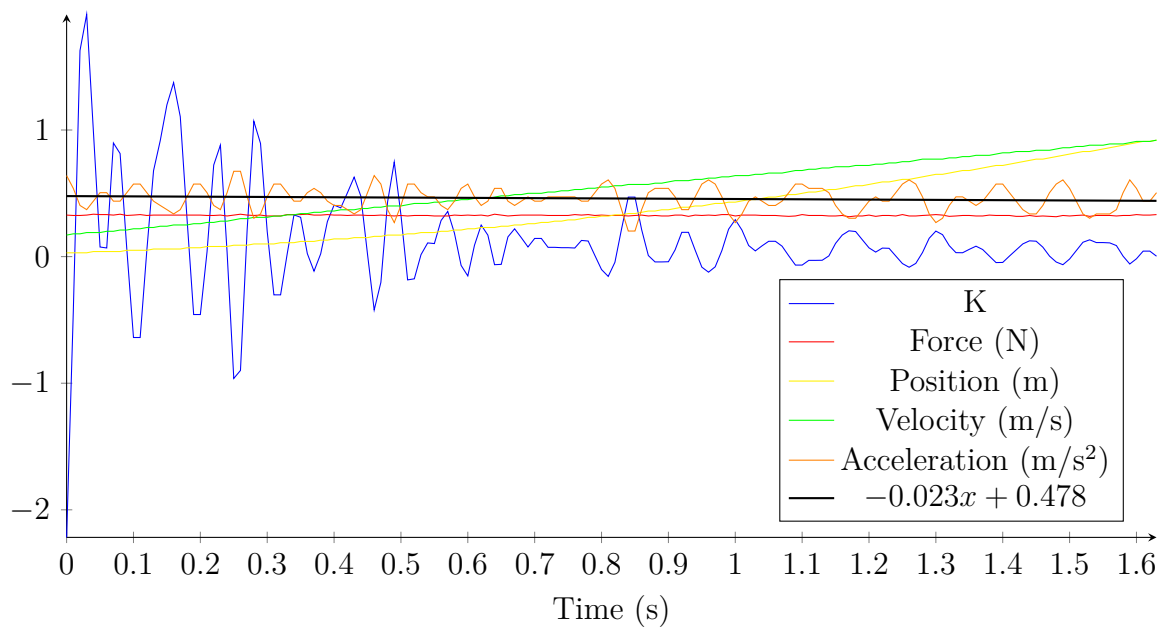


Figure A5. Raw Data Collected from Smart Cart and Calculated  $K$  value - Equilateral Wedge

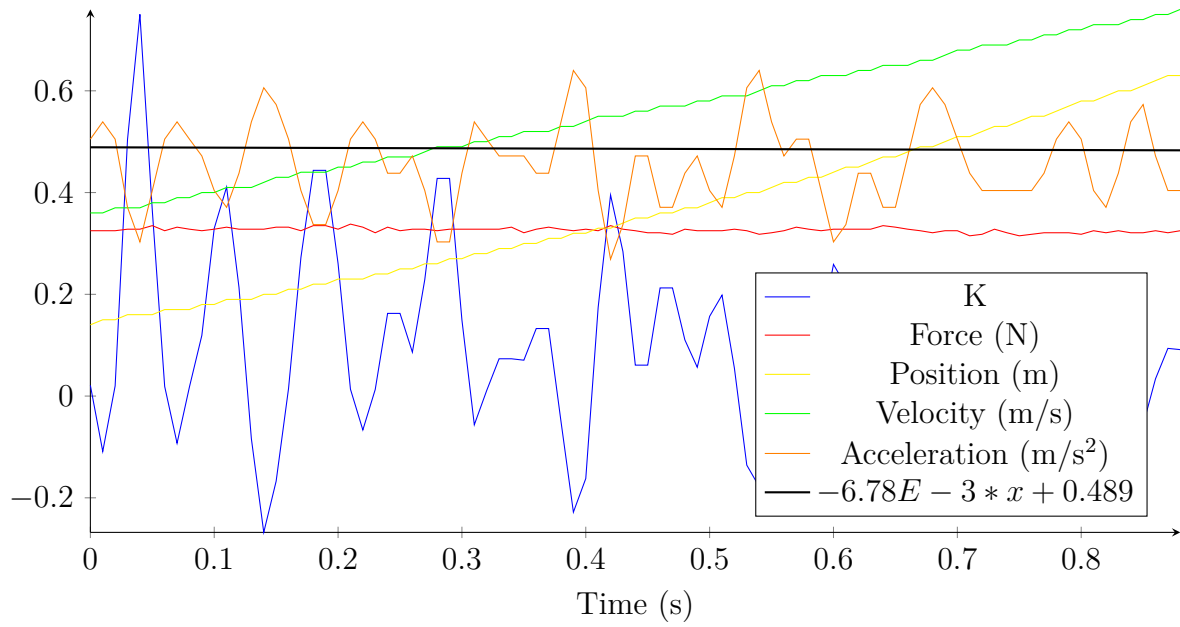


Figure A6. Raw Data Collected from Smart Cart and Calculated  $K$  value - Orange with Pocket

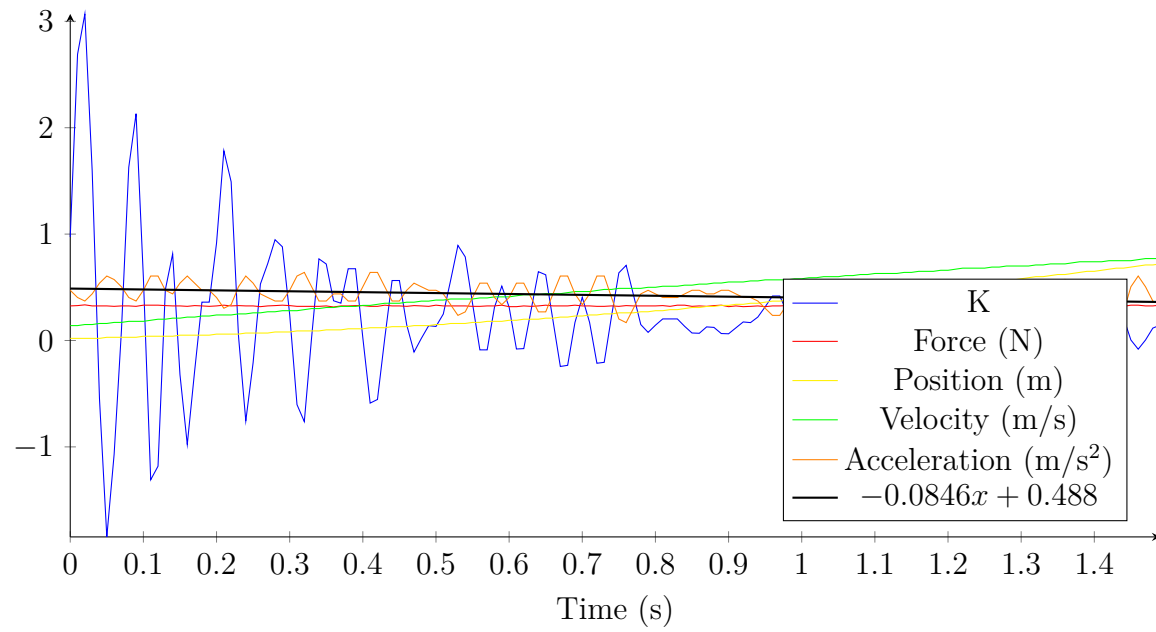


Figure A7. Raw Data Collected from Smart Cart and Calculated  $K$  value - Sharp Wedge

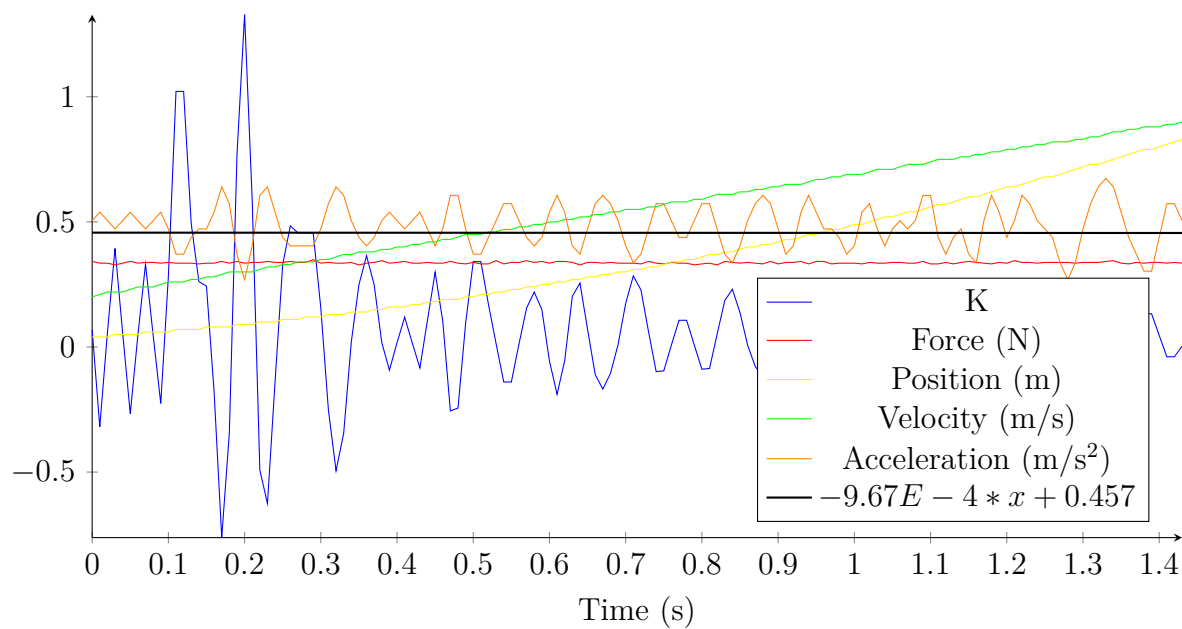
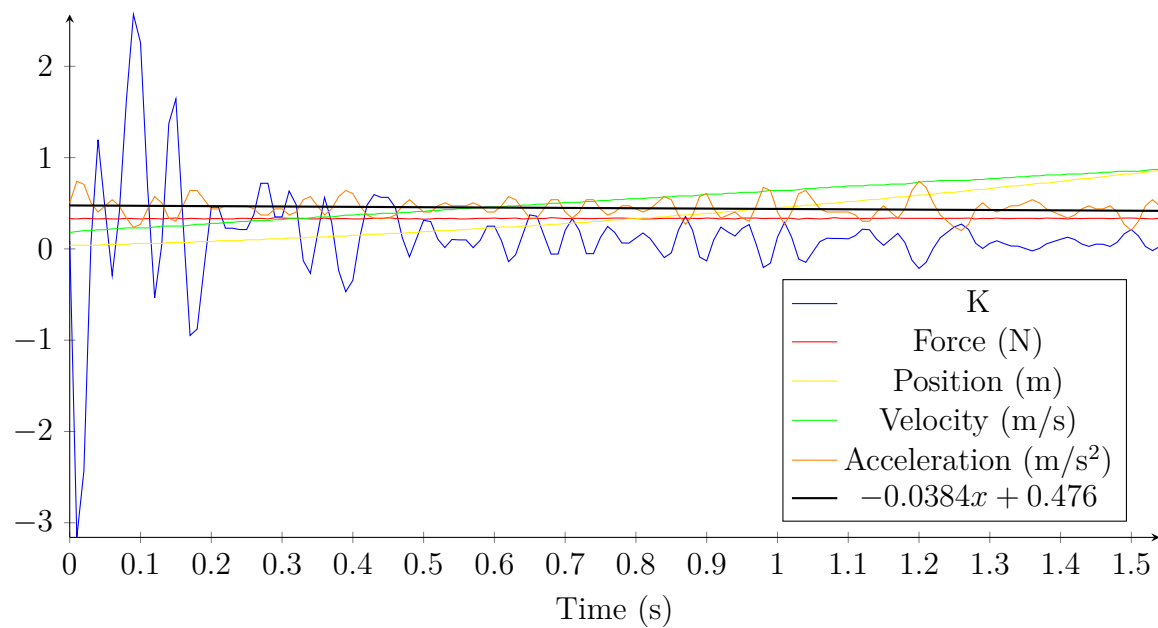


Figure A8. Raw Data Collected from Smart Cart and Calculated  $K$  value - Sharp Wedge on Orange



## Appendix B

## Sample Calculations

**Average Range**

$$\text{Average Range} = \frac{R_1 + R_2 + R_3 + \dots + R_n}{n} \quad (2)$$

$$\text{Average Range}_{12.5\text{cm}} = \frac{338 + 333 + 332 + 336 + 332}{5} \quad (3)$$

$$\text{Average Range}_{12.5\text{cm}} = 334.2 \text{ cm} \quad (4)$$