

## Exercise #1-Part 2: Solving N-Puzzle Problem Using A\*

Attached are the following files:

1. frontier.py – Implementing frontier with a priority queue. Will be used to prioritize states based on a value function,  $\text{state.hdistance(s)} + \text{state.path\_len(s)}$ . You will need to write  $\text{state.hdistance(s)}$  😊
2. state.py – Implements an N-Puzzle, except for the heuristics. Your assignment!
3. search.py – Implements the search pseudocode from class.

You need to go through the attached files, understand them, and perform the following tasks:

1. Implement the `hdistance1` function to accurately return the number of tiles out of place and change the code in frontier to return  $\text{state.hdistance1(s)} + \text{state.path\_len(s)}$ . Run the code 100 times and save the output of the number of states checked – (i) total items pushed, (ii) total items popped and (iii) path cost of the solution – as averaged from 100 runs in a 4X4 puzzle (previously not always possible).
2. Implement the `hdistance2` function to accurately return the Manhattan distance of the tiles from their target position and change the code in frontier to return  $\text{state.hdistance2(s)} + \text{state.path\_len(s)}$ . Run the code 100 times and save the output of the number of states checked – (i) total items pushed, (ii) total items popped and (iii) path cost of the solution – as averaged from 100 runs in a 4X4 puzzle.
3. Re-run Steps 1 and 2, as a *weighted A\* search*. That is, with priority function  $2 * \text{state.hdistance1(s)} + \text{state.path\_len(s)}$  and  $2 * \text{state.hdistance2(s)} + \text{state.path\_len(s)}$ , respectively. How does this affect the runtime (number of states checked) and optimality (actual cost of found solution) of the code?

\* Reminder from the lecture:

	Search Cost (nodes generated)			Effective Branching Factor		
$d$	IDS	$A^*(h_1)$	$A^*(h_2)$	IDS	$A^*(h_1)$	$A^*(h_2)$
2	10	6	6	2.45	1.79	1.79
4	112	13	12	2.87	1.48	1.45
6	680	20	18	2.73	1.34	1.30
8	6384	39	25	2.80	1.33	1.24
10	47127	93	39	2.79	1.38	1.22
12	3644035	227	73	2.78	1.42	1.24
14	–	539	113	–	1.44	1.23
16	–	1301	211	–	1.45	1.25
18	–	3056	363	–	1.46	1.26
20	–	7276	676	–	1.47	1.27
22	–	18094	1219	–	1.48	1.28
24	–	39135	1641	–	1.48	1.26

**Figure 3.29** Comparison of the search costs and effective branching factors for the ITERATIVE-DEEPENING-SEARCH and  $A^*$  algorithms with  $h_1$ ,  $h_2$ . Data are averaged over 100 instances of the 8-puzzle for each of various solution lengths  $d$ .