
MAE 219 Assignment 4, Part 2

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% Clear the workspace.
clear;

Constants

```
% device and human parameters
m = 0.03;    % effective mass at the handle, kg
b = 1;      % viscous damping, Ns/m
kh = 500;   % human hand stiffness, N/m
bh = 10;    % human hand damping, Ns/m

% times for dynamic simulation
tstart = 0;  % s
tend = 10;   % s
T = 0.1*10^-3; % time increment, s
t = (tstart:T:tend)'; % time vector

% human input
omega = 0.4*2*pi; % frequency of user's desired motion, rad/s
A = 0.04; % amplitude of user's desired motion, m
xd = A*sin(omega*t) - 0.01; % user's desired hand position, in m
vd = A*omega*cos(omega*t); % user's desired hand velocity, in m/s

% default virtual wall parameters
kwall = 500; % wall stiffness, N/m
xwall = 0.025; % wall position, m

% *****
% effect-specific parameters
effect = "Sensor Quantization"; % change this to change the effect
switch effect
    case "Sensor Quantization"
        label = "Nominal System Parameters";
        deltax = 0.0005; % position sensor resolution, m
    case "Nonlinear Friction"
        label = "User Moves in Free Space";
        xwall = 0.05; % user moving in free space
        vt = 0.01; % speed threshold, m/s
        bl = 10*b; % large damping, Ns/m
    case "Actuator Saturation"
        label = "User Moves Inside Wall";
        xwall = -0.05; % user moving inside wall
        ft = 15; % force threshold, N
    case "Sample and Hold"
        label = "Nominal System Parameters";
        deltat = 0.05; % sampling period
    case "Zero-Order Hold"
```

```

        label = "Nominal System Parameters";
        deltat = 0.05;    % hold period
    otherwise
        error("Effect not valid.")
    end
% *****

```

State Tracking

```

xh = zeros(length(t),1);    % handle position
vh = zeros(length(t),1);    % handle velocity
ah = zeros(length(t),1);    % handle acceleration
fa = zeros(length(t),1);    % force applied by the actuator
ffelt = zeros(length(t),1); % force felt by the human
xq = zeros(length(t),1);    % measured position

```

Dynamic Simulation

```

for sim = 1:2

    for i = 1:length(t)

        % integrate the main state derivatives
        if (i == 1)
            % first time step has no difference between desired and actual
        handle position
            vh(i) = vd(i);
            xh(i) = xd(i);
        else
            % simple Euler integration (you could use something more
accurate!)
            vh(i) = vh(i-1) + ah(i-1) * T;
            xh(i) = xh(i-1) + vh(i-1) * T;
        end

        xq(i) = xh(i);

        % *****

        if effect == "Sample and Hold" & sim == 2    % if sample and hold in
effect
            if rem(t(i),deltat) ~= 0    % if not time to sample position
                xq(i) = xq(i-1);    % hold previous position measurement
            end
        end

        % *****

        % *****

        if effect == "Sensor Quantization" & sim == 2    % if sensor
quantization in effect
            xq(i) = deltax * floor(xh(i)/deltax);    % quantization of xh with
resolution deltax
        end
        % *****
    end
end

```

```

    % force applied by the virtual environment
    if (xq(i) > xwall) % if the user is inside the wall
        fa(i) = kwall * (xwall - xq(i));
    else % if the user is outside the wall
        fa(i) = 0;
    end

    % *****

    effect == "Zero-Order Hold" & sim == 2 % if zero-order hold in
effect
        if rem(t(i),deltat) ~= 0 % if not time to update the force
            fa(i) = fa(i-1); % hold previous force output
        end
    end
    % *****

    % *****
    effect == "Actuator Saturation" & sim == 2 % if actuator
saturation in effect
        if abs(fa(i)) > ft % if actuator is saturated
            fa(i) = sign(fa(i)) * ft; % limit force applied
        end
    end
    % *****

    % force between the hand and the handle
    fh = kh * (xd(i) - xh(i)) + bh * (vd(i) - vh(i));

    % force felt by the user
    ffelt(i) = -fh;

    % default friction force
    ff = -b * vh(i);

    % *****
    effect == "Nonlinear Friction" & sim == 2 % if nonlinear
friction if effect
        if abs(vh(i)) < vt % if speed within threshold
            ff = -bl * vh(i); % large damping
        end
    end
    % *****

    % Compute the sum of forces on the handle: applied force, human
force, and friction force.
    ftotal = fa(i) + fh + ff;

    % Compute the handle's new acceleration for the next iteration.
    ah(i) = ftotal / m;

end

if sim == 1 % if ran simulation without effect

```

```

        % save data in matrices
        xdata1 = [xwall*ones(1,length(t))' xd xh];
        fdata1 = [fa, ffelt];
    else
        % save data in matrices
        xdata2 = [xwall*ones(1,length(t))' xd xh];
        fdata2 = [fa, ffelt];
    end
end
end

```

Plotting

```

figure(1); clf;

% tick mark calculations
N = 5;
% find max
xmax = max( [abs(xdata1) abs(xdata2)] ,[], "all");
% create N tick marks above and below zero
xtic = round( xmax/N, 1, 'significant');
xtics = [-fliplr(xtic:xtic:xmax) 0 xtic:xtic:xmax];
% find max
fmax = max( [abs(fdata1) abs(fdata2)] ,[], "all");
% create N tick marks above and below zero
ftic = round( fmax/N, 1, 'significant');
ftics = [-fliplr(ftic:ftic:fmax) 0 ftic:ftic:fmax];

% positions without effect
subplot(2,2,1)
h = plot(t, xdata1);
set(h(1), 'Color', [0 0 0], 'LineWidth', 1.0, 'LineStyle', '--')
set(h(2), 'Color', [1 .3 0], 'LineWidth', 1)
set(h(3), 'Color', [.8 0 .8], 'LineWidth', 2)
xlabel('time (s)')
ylabel('position (m)')
legend('x_{wall}: virtual surface', 'x_d: user's desired position', 'x_h: handle position')
subtitle(append('Without ', effect))
axis([tstart tend -xmax xmax])
set(gca, 'FontSize', 14)
title('Positions vs. Time', 'FontWeight', 'Normal', 'FontSize', 18)
xticks(0:0.5:tend)
xtickformat('%0.1f')
yticks(xtics)
ytickformat('%0.3f')

% positions with effect
subplot(2,2,2)
h = plot(t, xdata2);
set(h(1), 'Color', [0 0 0], 'LineWidth', 1.0, 'LineStyle', '--')
set(h(2), 'Color', [1 .3 0], 'LineWidth', 1)
set(h(3), 'Color', [.8 0 .8], 'LineWidth', 2)

```

```

xlabel('time (s)')
ylabel('position (m)')
legend('x_{wall}: virtual surface','x_d: user's desired position','x_h:
handle position')
subtitle(append('With ',effect))
axis([tstart tend -xmax xmax])
set(gca,'FontSize',14)
title('Positions vs. Time','FontWeight','Normal','FontSize',18)
xticks(0:0.5:tend)
xtickformat('%.1f')
yticks(xtics)
ytickformat('%.3f')

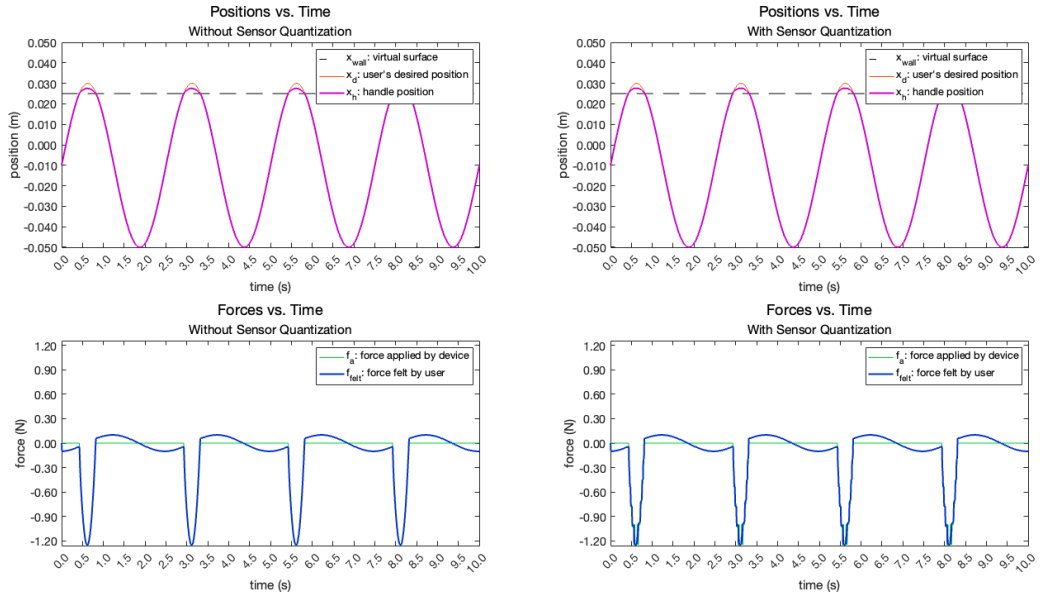
% forces without effect
subplot(2,2,3)
h = plot(t, fdata1);
set(h(1),'Color',[0 .8 .2],'LineWidth',1)
set(h(2),'Color',[0 .2 .8],'LineWidth',2)
xlabel('time (s)')
ylabel('force (N)')
legend('f_a: force applied by device','f_{felt}: force felt by user')
subtitle(append('Without ',effect))
axis([tstart tend -fmax fmax])
set(gca,'FontSize',14)
title('Forces vs. Time','FontWeight','Normal','FontSize',18)
xticks(0:0.5:tend)
xtickformat('%.1f')
yticks(ftics)
ytickformat('%.2f')

% forces with effect
subplot(2,2,4)
h = plot(t, fdata2);
set(h(1),'Color',[0 .8 .2],'LineWidth',1)
set(h(2),'Color',[0 .2 .8],'LineWidth',2)
xlabel('time (s)')
ylabel('force (N)')
legend('f_a: force applied by device','f_{felt}: force felt by user')
subtitle(append('With ',effect))
axis([tstart tend -fmax fmax])
set(gca,'FontSize',14)
title('Forces vs. Time','FontWeight','Normal','FontSize',18)
xticks(0:0.5:tend)
xtickformat('%.1f')
yticks(ftics)
ytickformat('%.2f')

sgtitle([append('Dynamic Simulation of a Haptic Interface: ',label); append('
With and Without ',effect)], 'FontSize',18,'FontWeight','Bold')

```

**Dynamic Simulation of a Haptic Interface: Nominal System Parameters
With and Without Sensor Quantization**



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