

Homework 6, Problem 2

Practice Exercise 8.1 (h)

David Lim

A16398479

02/25/25

```
clear  
syms theta1 theta2 m1 m2 L1 I1 I2 'real'
```

Mass matrix:

```
M = [m1*L1^2+m2*theta2^2+I1+I2 0; 0 m2]
```

M =

$$\begin{pmatrix} m_1 L_1^2 + m_2 \theta_2^2 + I_1 + I_2 & 0 \\ 0 & m_2 \end{pmatrix}$$

Jacobian:

```
J = [-theta2*sin(theta1) cos(theta1); theta2*cos(theta1)  
sin(theta1)]
```

J =

$$\begin{pmatrix} -\theta_2 \sin(\theta_1) & \cos(\theta_1) \\ \theta_2 \cos(\theta_1) & \sin(\theta_1) \end{pmatrix}$$

End-effector mass matrix:

```
Lambda = simplify(J'\M/J)
```

Lambda =

$$\begin{pmatrix} \frac{m_2 \theta_2^2 + I_1 \sin(\theta_1)^2 + I_2 \sin(\theta_1)^2 + \sigma_2}{\theta_2^2} & \sigma_1 \\ \sigma_1 & \frac{I_1 + I_2 + L_1^2 m_1 + m_2 \theta_2^2 - I_1 \sin(\theta_1)^2 - I_2 \sin(\theta_1)^2 - \sigma_2}{\theta_2^2} \end{pmatrix}$$

where

$$\sigma_1 = -\frac{\sin(2\theta_1) (m_1 L_1^2 + I_1 + I_2)}{2\theta_2^2}$$

$$\sigma_2 = L_1^2 m_1 \sin(\theta_1)^2$$

For $\theta_1 = 0$:

```
subs(Lambda,theta1,0)
```

ans =

$$\begin{pmatrix} m_2 & 0 \\ 0 & \frac{m_1 L_1^2 + m_2 \theta_2^2 + I_1 + I_2}{\theta_2^2} \end{pmatrix}$$