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**DEEP FACE RECOGNITION FOR ONLINE  
STUDENT IDENTIFICATION**

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# Acknowledgments

# Abstract

## Resumo

# Chapter 1

## Introduction

### 1.1 Context

The outbreak of the COVID-19 pandemic tested the entire world on several levels and changed the concept of what is "normal" thereafter. The devastating health, economic and social consequences that COVID caused, spanned a need to develop novel solutions, for almost every aspect of our lives, that facilitate the adaptation to the new world we're living in.

Educational systems were no exception. In the midst of the pandemic, governments around the world forced institutions to shut down and stop the customary in-person regimen of teaching. By April 2020, most universities transitioned to an adapted remote learning [112] that lacked proper support due to the unanticipated nature of the events, leading to new challenges, in particular, the legitimacy of moments of evaluation performed remotely. To counter this problem, different approaches can be taken, namely, changing the method of evaluation, suppressing it altogether [7] or, when possible, implement a continuous monitoring solution such as TrustID [ref?](#). However, there are still unresolved issues that must be addressed in order to implement an end-to-end solution capable of assuring the success of such systems.



One core aspect of them is the face verification task, therefore, the data obtained directly influences the performance. Due to the purpose of the application and expected devices to be used, what is obtained can be classified as from an unconstrained nature. Even though the capture of image is consensual, there is no way of controlling the conditions of capturing the visual data and consequent results. This can be attributed to the fact that it is anticipated that the system will be executed in a laptop or a smartphone, thus the capture device might not be ideal. The more probable input method will be a webcam or the smartphone's front facing camera, so a high variation in pose, resolution, illumination, etc. is not unforeseeable.

Another detail that must be regarded, is the processing power available to execute the system. It is common for the equipments used to have a deficiency of it<sup>1</sup>, which is not suitable for high-demanding applications, as its improved accuracy comes at the cost of increased computational overhead, which can make real-time continuous monitoring unfeasible.

In conclusion, the method of choice must take the aforesaid into consideration and be a trade-off between accuracy and computational strain, while also being invariant, to a certain degree, to the posed challenges of capturing the required data.

## 1.2 Objectives

## 1.3 Dissertation structure

This dissertation will be divided into different chapters that partitions themselves into sections and subsections. Chapter one relates to the introduction of the dissertation, it will present the context and motivation behind the problem

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<sup>1</sup> According to the February 2023 Steam hardware survey, roughly 5% of its users do not have a dedicated GPU.

and structure of the document. The document continues to the second chapter, it starts with an overview of the History of AI, carries out a survey about the topic's State-Of-The-Art, presented and summarized through the step-by-step analysis of the pipeline of a Face Recognition system, and ends with a comparison table of the discussed methods. In chapter number three, the implemented methods and experiments are described. The forth chapter will present and discuss the results. Finally, chapter five, will draw conclusions of the work achieved in the past several months and prospects for the future.

# Chapter 2

## State of The Art

### 2.1 History of AI

The following sections present a broad overview of the history of Artificial Intelligence (AI) by presenting important articles in order for the reader to be able to have a notion of the progress that has been made over the past decades, the hardships encountered and how important AI is in our lives.

#### **Philosophy**

On October 1950, in his article *Computing Machinery and Intelligence*, Alan Turing questioned: "Can machines think?" [100]. At the time, the question was too meaningless to answer since not only the theory but also the technology available weren't developed enough. Nonetheless, Turing still predicted that in the future there would be computers that could, effectively, display human-like intelligence and discernment under the conditions proposed on the aforementioned article.

#### **Relevant events to the birth of AI**

The breakthroughs of AI are predominant, and its importance in our everyday life is undeniable, but the theory behind it has several early roots. The interest in

the area grew immensely with, for example, all the Turing’s theoretical research, the proposal of the first mathematical Artificial Neuron model in 1943 by Warren McCulloch and Walter Pitts (based of binary inputs and output) [69] and in 1949 Donald Hebb revolutionized the way the artificial neurons were treated by proposing what is known as the Hebb’s rule<sup>1</sup>. Taking into consideration the latter two, but specially Hebb’s proposals, Belmont Farley and Westley Clark implemented in 1954 one of the first successful Artificial Neural Networks (ANN), also called Perceptron, composed of two layers of 128 artificial neurons with weighted inputs [31]. Over the span of approximately ten years, multiple researches were performed attempting to computerize the human brain. However, only in 1956, during the *Dartmouth Summer Research Project on Artificial Intelligence* [68], was the term ”Artificial Intelligence” firstly proposed by John McCarthy *et al.*, beginning what is now considered to be the birth of AI [123].

### **The fading of general interest**

The succeeding two decades following the Dartmouth conference were filled with important developments, with special emphasis in the works published in 1958 by Frank Rosenblatt (generalized the Farley and Clark training to multi-layer networks rather than only two) [86], the 1959 General Problem Solver implemented by Allen Newel *et al.* (a program intended to work as a universal problem solver that was capable of solving exercises such as the Towers of Hanoi<sup>2</sup>) [75] and the ELIZA a natural language processing tool program developed by Joseph Weizenbaum between 1964 and 1966 [109]. Unfortunately, part of the interest and development around AI met an unforeseen fade after criticisms about the exagger-

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<sup>1</sup> ”When an axon of cell A is near enough to excite a cell B and repeatedly or persistently takes part in firing it, some growth process or metabolic change takes place in one or both cells such that A’s efficiency, as one of the cells firing B, is increased.” [38], meaning that when two neurons fire together their relation is strengthened.

<sup>2</sup> *The Towers of Hanoi* is a game with 3 stacks of increasingly smaller disks. The goal is to stack them one at a time, so that they are arranged in a decreasing radius manner.

ated public funding [36] and the Marvin Minsky and Seymour Papert 1969 book *The Perceptron: A Probabilistic Model for Information Storage and Organization in the Brain* [71] that reported on the problems of the Perceptron network. The overall sentiments regarding this topic of research was of doubt and fear of no progress, mainly due to the spending and two issues raised by Minsky and Papert: the ANN couldn't solve linear inseparable problems<sup>3</sup> and there were limitations due to a lack of sufficient computing power to handle the processing of multi-layer large networks.

## A better approach

Minsky and Papert raised important questions, but it shouldn't have discouraged other researchers from further trying, since they failed to acknowledge alternative approaches that had already solved those exact problems. As previously stated, the model proposed by McCulloch and Pitts, later improved by the Farley-Clark implementation and, finally, Rosenblatt, couldn't handle linearly inseparable classes. A possible solution for cases like this started being studied in the 1960s [47, 87] and, although it didn't produce relevant results, in 1965 Alexey Ivakhnenko and Valentin Lapa [45] were, indeed, successful in implementing what is nowadays considered to be the first deep learning network of its kind [90]. In 1971 Ivakhnenko also published an article describing a deep learning network with 8 layers that was already able to create hierarchical internal representations [46].

The years progressed, in 1979 Kuniyuki Fukushima introduced the first Convolutional Neural Network (CNN) in a structural sense, due to its similarity to the architecture of modern ones of this category. Ten years later, Yann LeCun *et al.* applied to a CNN, for the first time, a revolutionizing algorithm called Back-propagation [56], creating what is now a pillar for most of the modern competition winning networks in computer vision [90] and employing the term "convolution"

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<sup>3</sup> That is, if two sets  $X$  and  $Y$  in  $\mathbb{R}^d$  can't be divided by a hyperplane such that the elements of  $X$  and  $Y$  stay on opposing sides, then we're dealing with linear inseparable classes [30]

for the first known time [61]. He also introduced the MNIST (**M**odified **N**ational **I**nstitute of **S**tandards and **T**echnology) dataset, a collection of handwritten digits [58], that to this day is still one of the most famous benchmarks in Machine Learning. Backpropagation can be traced back many decades, but the modern version was first described by Seppo Linnainmaa (1970) [62], implemented for the first time by Stuart Dreyfus (1973) [28] and, finally in 1986, David Rumelhart *et al.* popularized it in the Neural Network's (NN) domain by demonstrating the growing usefulness of internal representations [89].

## The importance of Convolutional Neural Networks

The study on Neural Networks continued and there were improvements on all types of architectures [39, 110] with special highlight to pioneering Neural Networks processed by GPUs<sup>4</sup> (standard NN in 2004 by [77] and CNN in 2006 by [14]). But there's a well deserved particular attention related to the developments of CNNs due to their great performance in image related tasks when compared to others networks, as proven by LeCun in his 1998 paper [58]. Some relevant examples: in 2003 the MNIST record was broken by Patrice Simard *et al.* [93], achieving an error rate of 0.4% (whereas a non-convolutional neural network by the same authors took the second place with 0.7%); three years later, the same benchmark had a new set low of 0.39% by Marc'Aurelio Ranzato *et al.* [84]; in 2009 a CNN by Yang *et al.* was the first network of this type to win an official international competition (TRECVID) [118]; a GPU implementation of a CNN [20] achieved superhuman vision performance in a competition (IJCNN 2011) in a *German Traffic Sign Recognition Benchmark* with a 0.56% error rate (0.78% for the best human performance, 1.69% for the second-best neural network contestant and 3.86% for the best non-neural method [95]). This last example conjoined with non-convolutional methods [82, 22] and the previously cited [14, 77], reinforces how fundamental GPUs were to further develop neural networks. To supplement

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<sup>4</sup> Graphics Processing Unit

even more the importance of CNNs and GPUs, only a year later, Alex Krizhevsky *et al.* proposed a Deep CNN trained by GPUs that was the first one to win the ImageNet Large Scale Visual Recognition Challenge (ILSVRC), achieving an error rate of 15.3% while the second place obtained 26.2% [54].

The year of 2012 was very important for Deep Learning, CNNs and Computer Vision, due to all the attention brought to many researches on this topic after several systems of this kind won image analysis competitions ([19, 21] and the very important previously mentioned [54]), beginning what's considered to be the start of the new wave, we're currently in, of interest in Artificial Intelligence, specially in the aforesaid topics [61].

## 2.2 Face Recognition

Face Recognition (FR) is a thoroughly debated and extensively researched task in the Computer Vision community for more than two decades [83], popularized in the early 1990s with the introduction of the Eigenfaces [101] or Fisherfaces [78] approaches. These methods projected faces in a low-dimensional subspace assuming certain distributions, but lacked the ability to handle uncontrolled facial changes that broke said assumptions, henceforth, bringing about face recognition approaches through local-features [18, 1] that, even though, presented considerable results, weren't distinctive or compact. Beginning in 2010, methods based on learnable filters arose [120, 59], but unfortunately revealed limitations when nonlinear variations were at stake.

Earlier methods for FR worked appropriately when the data was handpicked or generated on a constrained environment, however, they didn't scale adequately in the real world where there are large fluctuations in, particularly, pose, age, illumination, background scenario, the presence of facial occlusion [83] and many unimaginable more [cite ijb-s 2, 4, 23](#). These shortcomings can be dealt with by using Deep Learning, a framework of techniques that solves the nonlinear inseparable classes problem [ref.](#), more specifically a structure called Convolutional Neural Network (CNN) [105].

CNNs are an Artificial Neural Network (ANN) that exhibit a better performance on image or video-based tasks compared to other methods [58]. They were greatly hailed in 2012, after the AlexNet [54] victory, by a great margin, in the ImageNet Large Scale Visual Recognition Challenge (ILSVRC). Just two years later, DeepFace [96] revolutionized the benchmarks scores by achieving state-of-the-art results that approached human performance, reinforcing even further the importance of Deep Learning and shifting the research path to be taken [105].

Given what has been stated so far and the proven robustness, performance, and overall results in computer vision [ref. won competitions](#), the methods discussed



in this dissertation will therefore deal exclusively with Deep Learning approaches. For more information on other methods, please refer to [55].

## 2.3 A Face Recognition System

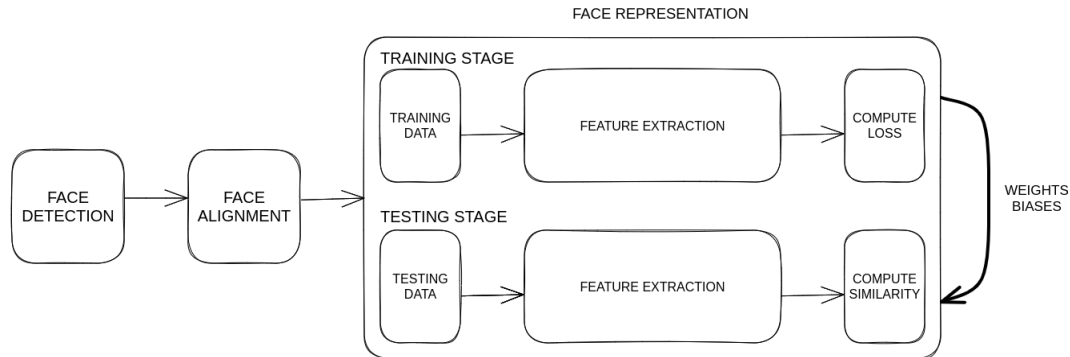


Figure 1: A typical face recognition pipeline, guided by the approach in [105].

According to Ranjan *et al.* [83], the goal of a FR system is to find, process and learn from a face, gathering as much information as possible, and as a result, it is one of the most widely implemented biometric system solutions in light of its versatility when facing real world application [29], such as **military, public security and daily life**.

By and large, all end-to-end automatic face recognition systems follow a sequential and modular<sup>5</sup> pipeline (Figure 1) composed of three pillar stages [105]: face detection, face alignment and face representation. First an image or video feed is used as an input then, as the name suggests, the **face detection** module is responsible for finding a face. Next, the **face alignment** phase applies spatial transformations to the data in order to normalize the faces' pictures (or frames, in the case where a video is used) to a standardized view. Finally, the **face representation** stage, makes use of deep learning techniques to learn discriminative features that will allow the recognition. A feature is nothing more than a characteristic inherent to the input image, it can be "something" or a collection of, that has been measured or processed, and presented as a result [33].

<sup>5</sup> Sequential because each stage relies on the output from the previous ones, and modular in the sense that each stage employs its own method and it can be modified to better adapt to specific tasks.

All three stages have their individual importance and methods of implementation<sup>6</sup>. **Face detection** is achievable through classical approaches [103, 9] or deep methods, among them is [27] and the widely applied [126]. **Face alignment**, once again, can be accomplished through traditional measures [23, 66] or more modern ones, namely [43] or the aforementioned [126] which concurrently performs detection and alignment. To conclude, the **face representation** module is no exception, and can also be divided in two groups, regarding the methodology used. Some conventional systems were already mentioned, such as [78, 101], and the deep learning ones are the object of discussion of this dissertation and will be reviewed along the following sections, therefore, the focus will be on describing, with particular interest, the face representation stage.

### 2.3.1 Face Detection

Face detection is the first step in any automatic facial recognition system. Given an input image to a face detector module, it is in charge of detecting every face in the picture and returning bounding-boxes coordinates, for each one, with a certain confidence score [29, 83].

Previously employed traditional face detectors [cite here](#) are incapable of detecting facial information when faced with challenges such as variants in image resolution, age, pose, illumination, race, occlusions or accessories (masks, glasses, makeup) [29, 83]. The progress in deep learning and increasing GPU power led DCNNs to become a viable and reliable option that solves said problems in face detection.

These techniques can be included in different categories. A more analytical perspective [29] distributes the methods, depending upon their architecture or pur-

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<sup>6</sup> For a deeper and extensive study, please refer to: [121] in the case of classic face detection approaches and [70] for deep learning based methods; [107] addresses traditional face alignment methods and is complemented with [29] for more up-to-date techniques; and [55] tackles classic face representation [\(add the following if needed\)](#) while [X supplements the deep learning ones](#).

pose of application, over seven categories: multi-stage, single-stage, anchor-based, anchor-free, multi-task learning, CPU real-time and, finally, problem-oriented. Additionally, being as the face detection problem can be seen as a specific task in a general object detection situation, it is no surprise that several works inherit from them and, therefore, some bases are referenced throughout the next list.

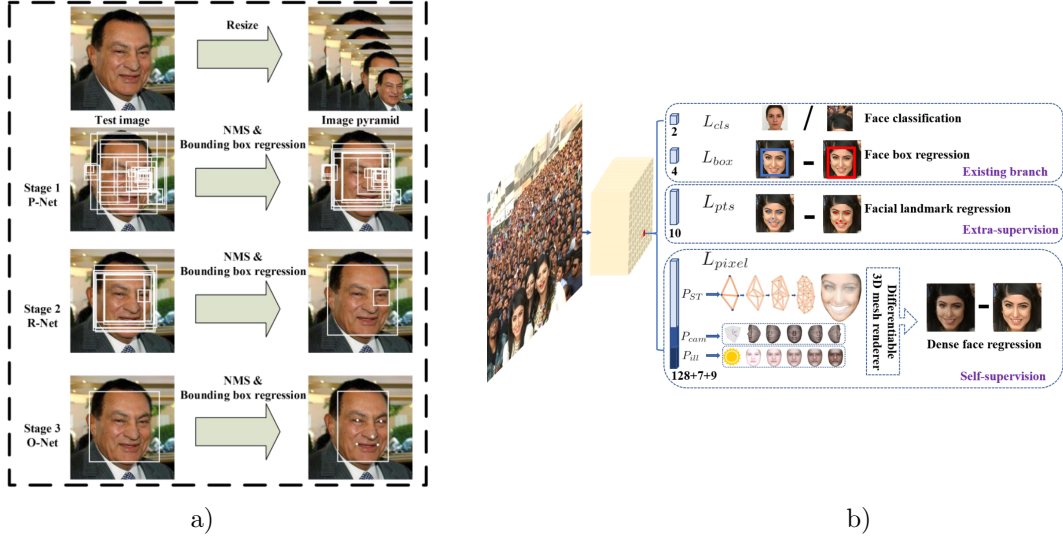


Figure 2: Comparison between **a)** MTCNN: multi-stage, CPU real-time and multi-task learning, and **b)** RetinaFace: single-stage, anchor-based, CPU real-time and multi-task learning. MTCNN [126] proposes a series of bounding boxes then, through a series of refinement stages, the best solution and landmarks are found. RetinaFace [27] accomplishes, in a single-stage, face classification and bounding box regression by evaluating anchors, landmark localization and dense 3D projection for facial correspondence.

→ **Multi-stage** methods [27] include all the coarse-to-fine facial detectors that work in similar manner to the following two phases. First, bounding box proposals are generated by sliding a window through the input. Then, over one or several subsequent stages, false positives are rejected and the approved bounding boxes are refined. To complement, one widely applied object detection protocol that inspired face detection methods and perfectly describes the steps mentioned above is Faster R-CNN [85]. However, these methods can be slower and have a more complex way of training [116].

→ **Single-stage** approaches [27] are the ones that perform classification and bounding box regression without the necessity of a proposal stage, producing highly dense face locations and scales. This structure takes inspiration, once again, from general object detectors, for example, the Single Shot MultiBox detector, commonly referred to as SSD [64]. Finally, the methods included in this class are more efficient, but can incur in compromised accuracy, when compared to multi-stage.

→ **Anchor-based** techniques [65, 27, 124] detect faces by predefining anchors with different settings (scales, strides, number, etc.) on the feature maps, then performing classification and bounding box regression on them until an acceptable output is found. As proven by Liu and Tang *et al.* [65], the choice of anchors highly influences the results of prediction. Hence, it is necessary to fine-tune them on a situation-by-situation basis, otherwise, there is a limitation in generalization. Furthermore, higher densities of anchors directly generate an increase in computational overhead.

→ **Anchor-free** procedures, obviously, do not need predefined anchors in order to find faces. Alternatively, these methods address the face detection by using different techniques. For example, DenseBox [42] which attempts to predict faces by processing each pixel as a bounding box, or CenterFace [116] that treats face detection as a key-point estimation problem by predicting the center of the face and bounding boxes. Even so, relating to the accuracy of anchor-free approaches, there's still room for improvement for false positives and stability in the training stage [29].

→ **Multi-task learning** are all the methodologies that conjointly performs other tasks, namely facial landmark<sup>7</sup> localization, during face classification and bounding

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<sup>7</sup> A facial landmark is a key-point in a face that contributes with important geometric information, namely the eyes, nose, mouth, etc. [32]

box regression [29]. CenterFace [116] is one example, and so it is the widely implemented MTCNN [126], which correlated bounding boxes and face landmarks. RetinaFace [27] is another state-of-the-art approach, it mutually detects faces, respective landmarks and performs dense 3D face regression.

→ **CPU real-time** methods, as the name suggests, include the detectors that can run on a single CPU core, in real-time, for VGA-resolution input images. A face detector can achieve great results in terms of accuracy, but for real world applications, its use can be too computational heavy, therefore, can't be deployed in real time (specially in devices that do not have a GPU) [29]. MTCNN [126], Faceboxes [127], CenterFace [116] or RetinaFace [27] are examples of this category.

→ **Problem-oriented** is a category that includes the detectors that are projected to resolve a wide range of specific problems, for example, faces that are tiny, partially occluded, blurred or scale-invariant face detection [29]. PyramidBox [98] is an example that solves the partial occluded and blurry faces, and HR [40] tackles the tiny faces challenge.

Although this distribution can create some overlap among the categories, it is superior due to the simplicity of inferring what defines each category and being a more fine-grained way of classifying techniques when compared to others, namely the dual categorical division by [83] that groups the methods in region<sup>8</sup> or sliding-window<sup>9</sup> based.

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<sup>8</sup> Region-based approaches creates thousands of generic object-proposals for every image, and subsequently, a DCNN classifies if a face is present in any of them.

<sup>9</sup> Sliding-window approaches centers on using a DCNN to compute a face detection score and bounding box at every location in a feature map.

### 2.3.2 Face Alignment

Face Alignment, or facial landmark detection [13], is the second stage of the face recognition pipeline, and has the objective of calibrating the detected face to a canonical layout, through landmark-based or landmark-free approaches, in order to leverage the core final stage of face representation [29].

Despite the fact that traditional face alignment methods are very accurate, that only occurs in constrained circumstances. Therefore, once again, to address that issue, deep learning-based methods are the solution to perform an accurate facial landmark localization that realistically scales to real world scenarios [32].

Furthermore, face alignment, can be accomplished through two categories of methods: landmark-based and landmark-free.

→ **Landmark-based alignment** is a category of methods that exploits the facial landmarks with the aim of, through spatial transformations, calibrating the face to an established layout [29]. This can be accomplished through: coordinate regression, heatmap regression or 3D Model Fitting. **Coordinate regression-based** methodologies [32, 63, 126] consider the landmark localization as a numerical objective, i.e. a regression, thus an image is fed to a DCNN and it will output a vector of landmark coordinates. **Heatmap Regression** [25, 114, 15] is different from coordinate regression because, although it is a numerical objective task, the output is not a coordinate vector, but a map of likelihood of landmarks' locations. Finally, **3D Model Fitting** [8, 13, 115] is the category that integrates methods that consider the relation between 2D facial landmarks and the 3D shape of a generic face. The particularity of them is the reconstruction of the 3D face from a 2D face image that is then projected over a plane in order to obtain the landmarks.

→ **Landmark-free alignment**, on the other hand, integrates the approaches that do not rely on landmarks as a reference to align the face, in contrast, these type of methods incorporate the alignment into a DCNN that gives, as a result, an

aligned face [29]. An example of an end-to-end method that does not depend on facial landmarks is RDCFace [128], and it rectifies distortions, applies alignment transformations and executes face representation. Hayat et al. [37] proposes a method that deals with extreme head poses. The process to register faces in an image with high pose variance can be quite challenging and often demands complex pre-processing, namely landmark localization, therefore, to address that, a DCNN is employed that does not rely on landmark localization and concomitantly register and represent faces.

As can be seen from the previous section, this step in the face recognition process can be accomplished, very sporadically, through standalone methods that process the detected face from the previous stage, but generally joint detection and alignment methods (and sometimes even face representation), previously referenced in the multi-task learning definition, are the optimal choice [13].

### 2.3.3 Face Representation

Finally, Face Representation is the last stage of the Face Recognition process. It is responsible for processing the aligned face from the previous stage and mapping the produced feature representation to a feature space, in which features from the same person are closer together and those that are different stand further apart from each other [29].

According to the literature [29, 60, 83, 91, 105], there's a consensus about how Face Recognition can be performed in two settings of operation: face verification and face identification. This distinction is only made possible due to the approaches available in the Face Representation stage that can leverage one, the other or both.

→ **Face verification**, also referred to as **face authentication**, is a one-to-one match, and it's the action of verifying if the query face matches the identity that's



being claimed. These principles are used in biometric systems such as self-service immigration clearance using E-passport. [60]

→ **Face identification**, also called **face recognition**, is a one-to-many correlation process that compares a query face to a database of faces and associates it to the corresponding match (or matches). A typical use case is to identify someone in a watchlist or surveillance videos. [60]

The overall pipeline comes to a conclusion in this module, however, in reality, it goes further than that. As can be seen in (Figure 1), due to its importance for the face recognition problem, it's highlighted the inherent pipeline of the Face Representation stage, henceforth, it shall be discussed in depth in the next section.

Explain the probe and gallery sets (tinyface) and the open vs closed set identification problem

## 2.4 Face Representation Pipeline

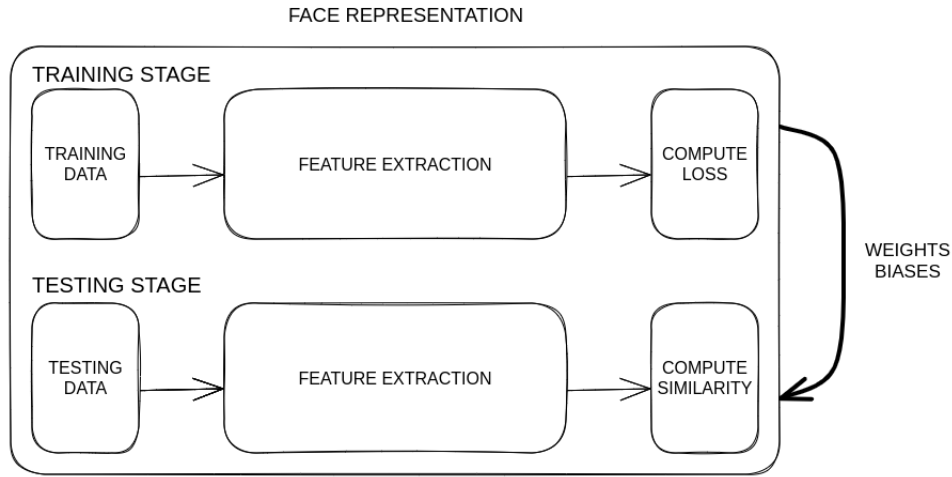


Figure 3: Face Representation pipeline, guided by the approach in [105].

As shown in (Figure 3), Face Representation is a two-step module composed of a training and testing stage. So as to be capable of performing face recognition, in either a verification or identification manner, a face representation system needs to learn robust, invariant and discriminative features that can distinguish identities [83].

To meet these requirements, the feature extractor must first be trained properly by taking data from previous stages and outputting a feature representation that's compared to the desired value using a loss function<sup>10</sup> [57, 105]. After that, everything is ready for the testing stage, where the face recognition *per se* occurs by calculating a similarity score for the feature representation produced by the trained feature extractor, and dictating if the identity belongs to the same person (face verification) or if it matches any identity (face identification) [83].

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<sup>10</sup> Also referred to as a cost or objective function. [57]

### 2.4.1 Datasets: Training and Testing Data

As been discussed throughout this dissertation, Deep Learning techniques can solve the problem of handling unconstrained scenarios, where there are variations in pose, illumination, occlusion, and so forth. To support this, in the past few years, datasets have been developed with this in mind so to be able to provide a large and diverse set of both training data, allowing for adequate regularization to unseen circumstances, and testing data that benchmarks the face recognition system in, as similar as possible, unconstrained real world scenarios [29].

In the following pages, a mix of training datasets, of overall relevance and more geared towards the purpose of this dissertation, will be reviewed.

## Training Data

When developing a deep face recognition system it's essential to keep in mind its necessity to adapt, and that's where the dataset used for training comes at play. Large training datasets are essential for face recognition [79], but large-scale is not enough. There must be a balance between the depth (number of unique identities) and the breadth/width (number of images per identity) [6, 11], and it will lead to different effects.

On one hand, a training dataset that is deep will help the face recognition system to produce more discriminative feature representations, since it will have a great number of identities to learn from. On the other hand, a wider set will have more images per identity, therefore, variations in pose, expressions, illuminations, occlusions, background clutter, image quality, accessories, and so forth [5] can be introduced and ultimately lead to feature representations more robust to them.

→ **CASIA-WebFace** [119], composed of 494,414 face images and 10,575 identities, was proposed as a novel dataset to overcome the problem of data dependence in face recognition and improve comparability across different methods. By train-

ing on the same dataset, methods can be better evaluated and compared.

→ **VGGFace** [79] was published alongside a homonymous face recognition method and, once again, with the objective of combating the lack of available large scale public datasets. It contains 2,6 million images and 2,622 different identities and a curated version, where incorrect image labels were hand-removed by humans, has 800,000 images for the same amount of identities.

→ **MS-Celeb-1M**'s [35] first intention was to provide a novel benchmark to identify celebrities that solves name ambiguities by linking a face with an entity key in a knowledge base. Second, it aimed at solving the gap in available large-scale datasets by providing a training set with, approximately, 10 million images and 100 thousand identities. Unfortunately, it is a dataset known for the presence of noisy labels.

→ **MegaFace** [74] introduced a benchmark for million-scale face recognition and provided a public large-scale training dataset that integrated 4,753,320 faces over 672,057 identities. The main difference compared to the previously mentioned datasets is that MegaFace does not use celebrities as subjects, in contrast it leverages the photographs released by Flickr under the Creative Commons license.

→ **VGGFace2** [11] is another large-scale dataset, and its main goals are: 1) covering numerous identities, 2) reduce labeling noise through automatic and manual filtering and, finally, 3) represent more realistic unconstrained scenarios due to a novel dataset generation pipeline that gathers images with a broad range of poses, age, illumination and ethnicity. All in all, this resulted in a dataset comprised of 3,31 million faces of 9131 subjects.

→ **UMDFaces-Videos** [6] is a video-based dataset composed of 22,075 videos of 3,107 subjects with 3,735,476 human annotated frames with great variation in image quality, pose, expressions and lightning. It was proposed during a study how

the performance of a face verification models is impacted by the effects of: 1) the type of media used for training (only videos or still images vs a mixture of both), 2) the width and depth of a dataset, 3) the label’s noise and 4) the alignment of the faces.

→ **Celeb-500k** [10] is another large-scale proposed with two issues in mind: the disparity in the scale of public datasets when compared with private ones, and determining the impact in performance from intra- and inter-class variations. That being so, Celeb-500k, consisting of 50 million images from 500 thousand persons, and Celeb-500k-2R, a cleaned version of the previous, comprised of 25 million aligned faces of 245 thousand identities, are released.

→ **IMDb-Face** [104] proposes a new dataset with based on a manually cleaned revision of MS-Celeb-1M and MegaFace. The growing demand for large-scale datasets introduced a new variable to take into consideration: the time available to annotate the data. Datasets that are well-annotated and have an enormous amount of data are notably expensive and time-consuming to develop. Therefore, automatic measures to clean the data were used, so it’s expected for a certain degree of noise to be introduced in a dataset. After selecting a subset from both the originals datasets, 2 million images were manually cleaned and resulted in 1,7 million images of 59 thousand celebrities.

→ **MS1MV2** [24] is another well know dataset. It was proposed in the ArcFace face recognition method paper and consists of a semi-automatic refinement of the previously mentioned MS-Celeb-1M, resulting in 5,8 million images of 85 thousand identities.

→ **MS1M-RetinaFace** [26] is a semi-automatically refined version of MS-Celeb-1M using the ArcFace method with ethnicity-specific annotators. This resulted in 5,1M faces of 93k identities.

→ **RMFRD** [108] is presented in the context of the need of using a mask, mandated by the COVID-19 pandemic, and that greatly reduces the effectiveness of conventional face recognition methods. Therefore, there was a need to improve their performance and for that a dataset that provides masked faces is needed. RMFRD pioneered this need by publishing a dataset consisting of 5 thousand masked and 90 thousand unmasked faces from 525 celebrities.

→ **Glnt360K** [4] is a training set presented in the Partial FC method paper. It was generated by merging and cleaning the aforementioned Celeb-500K and MS1MV2 datasets, which resulted in 17 million images of 360 thousand individuals.

→ **WebFace260M** [133] takes a giant leap in closing the gap between public available datasets and private ones. Partnered with a time-constrained face recognition protocol, the original paper presented an enormous 260 million faces and 4 million identities noisy dataset, an automatically cleaned, high quality training set with 42 million faces over 2 million identities (WebFace42M), and a smaller scale training dataset derived from the WebFace42M that has 10% of its data (WebFace4M).

→ **DigiFace-1M** [5] is a novel approach that revolutionizes the way of training face recognition models. It is a fully synthetic dataset that proposes mitigating three very relevant problems present in the majority of the conventional datasets: 1) ethical issues, 2) label noise and 3) data bias. The dataset is divided in two parts: part one contains 720 thousand images from 10 thousand identities and part two has 500 thousand images with 100 thousand identities, for a total of 1,22 million images and 110 thousand unique identities.

Dataset	Year	Availability	Images/videos	Depth	Avg. Breadth	Distribution	Description
CASIA-WebFace [119]	2014	Discontinued	494,414/-	10,575	46.7	Public	First public face recognition dataset.
Facebook [97]	2015	-	500M/-	10M	50	Private	Facebook's private dataset used to test different properties in face identification.
Google [91]	2015	-	200M/-	8M	25	Private	Private dataset used to train the FaceNet method.
VGGFace [79]	2015	Discontinued	2.6M/-	2,622	991.6	Public	High width public dataset released alongside VGGFace method.
MS-Celeb-1M [35]	2016	Discontinued	10M/-	100k	100	Public	Large-scale celebrities dataset.
MegaFace [74]	2016	temp	4,753,320/-	672,057	7.1	Public	Non-celebrity dataset.
VGGFace2 [11]	2017	temp	3.31M/-	9131	362.5	Public	High characteristics variation dataset.
UMDFaces-Videos [6]	2017	temp	~/22,075	3,107	7.1	Public	Video-based dataset with great variations.
Celeb-500k [10]	2018	temp	50M/-	500k	100	Public	Noisy celebrities dataset.
Celeb-500k-2R [10]	2018	temp	25M/-	245k	102	Public	Cleaned version.
IMDb-Face [104]	2018	temp	1.7M/-	59k	28.8	Public	Manually cleaned revision of MS-Celeb-1M and MegaFace.
MS1MV2 [24]	2019	temp	5.8M/-	85k	68.2	Public	Semi-automatic cleaned version of MS-Celeb-1M.
MS1M-RetinaFace [26]	2019	temp	5.1M/-	93k	54.8	Public	Semi-automatic cleaned version of MS-Celeb-1M.
RMFRD [108]	2020	temp	95k/-	525	180.9	Public	Dataset of masked and unmasked celebrities.
Glint360k [4]	2021	temp	17M/-	360k	47.2	Public	Cleaned version of the Celeb-500k AND MS1MV2 datasets.
WebFace260M [133]	2021	temp	260M/-	4M	65	Public	Largest publicly available dataset of celebrities faces (noisy).
WebFace42M [133]	2021	temp	42M/-	2M	21	Public	Cleaned and smaller version.
WebFace4M [133]	2021	temp	4.2M/-	200k	21	Public	Smaller version.
DigiFace-1M [5]	2022	Available	1,22M/-	110k	11.1	Public	Large-scale, fully synthetic dataset.

Table 1: Oof

## Testing Data

After the training is completed the performance of the system needs to be evaluated on different challenges to properly assess if it scales (or generalizes or applies or performs in) to real-world scenarios. A test dataset can be chosen for specific hurdles, for instance, cross-pose, cross-age, racial variations, quality assessment, and so forth [29].

→ **LFW** [41] is the most well-known face verification dataset. It was first released in 2007 as a way of evaluating the performance of face recognition methods, in a verification or pair matching manner, under unconstrained scenarios. LFW divides the dataset in 2 views. View 1 is designed for development, and in the training set contains 1100 pairs of mismatched images and 1100 pairs of matched ones, while the test set has 500 pairs of matched and 500 pairs of unmatched faces. View 2 is intended for performance reporting and splits the data over 10 separate sets, to facilitate 10-fold cross validation, where each one has 300 positive pairs (same identity) and 300 negative pairs (different person), resulting in 6000 pairs. Overall, the dataset has 13,233 face images and 5749 identities (only 1680 persons have two or more images).

→ **YTF** [113] is a video-based benchmark that leverages the greater amount of information provided by a video in comparison to still images. By collecting videos from *Youtube* there isn't an opportunity to control the conditions, hence the footage will support a wider range of characteristic's variation, namely lighting conditions, difficult poses, motion blur, compression artifacts, etc. This resulted in 3425 videos from 1595 identities and a benchmark protocol inspired in the LFW. To evaluate performance, a pair-matching test is designed. From the database, 5000 video pairs are collected, where half are matches and the other half are not, to be divided to allow 10-fold cross validation.

→ **IJB-A** [52] aims at straying further from the saturation in recognition benchmarks by proposing more challenging benchmarks (specifically by including wider geographic distribution and full pose variation) for both verification and identification. It consists of a mix of 5712 images and 2085 videos from 500 individuals, with manual bounding boxes, facial landmarks and, most importantly, labels. IJB-A supports two protocols: search (face identification) and compare (face verification). For both the protocols, the specifications are the same, i.e., ten random training and testing splits are generated using all 500 identities then used to perform sample bootstrapping (instead of cross validation) in order to enhance the number of testing subjects. For each split, 333 subjects are randomly distributed in the training set and the remainder 167 are placed in the testing set.

→ **CFP** [92] studies the effect of extreme pose variations, such as a profile view of a face, in face verification. During collection gender and profession balance, as well as racial diversity, were considered. A number of frontal and profile view images was also set as 10 and 4, respectively. Therefore, after cleaning the initial data, it resulted in 7000 images from 500 subjects. The experimental protocol divided the 500 identities over 10 splits (facilitating 10-fold cross validation) and randomly generated 7 matched pairs and 7 unmatched pairs per identity, resulting in a total of 7000 pairs of faces.



→ **MegaFace2** [74] has already been mentioned in the Training Data section, with exception to detailing the benchmarking protocol. The MegaFace2 is used to train the model that will be tested in 3 datasets: a one million Flickr distraction set, FaceScrub [76] and FG-Net. The first dataset is intended to supply the model with identities that are not to be found (hence being called a distraction set), while the last two contain the known identities to be tested.

→ **CPLFW** [130] is another dataset that tackles the overly optimistic accuracy saturation in classic benchmarks, such as the previously mentioned LFW. To this end, evaluating performance for cross-pose faces of LFW subjects is the matter of study. It contains the same number of 13,233 images of 5749 identities like LFW and the benchmark protocol performance is the LFW *View 2* with some differences: 1) negative pairs are from people of the same race and gender, 2) class imbalance and limited positive pair’s diversity is resolved by assuring that each identity has at least 2 images.

→ **CALFW** [131] has the same principles as CPLFW but applied to the age of the subjects (including the negative pairs selection and the class imbalance problem).

→ **Age-DB** [72], similarly to CALFW, is a dataset that considers the subject’s age. It distances itself from other databases by solving the noisy labelling, induced by automatic or semi-automatic methods, by doing so manually. Age-DB has 16,488 images and 568 subjects used in 4 evaluation protocols, similar to LFW’s *View 2*, where the main difference between them is the age difference between pairs (5, 10, 20 and 30 years).

→ **IJB-B** [111] builds upon IJB-A and proposes solving flaws that were verified in the previous dataset. First, the improved IJB-B dataset is larger, consisting of 21,798 images and 7,011 videos from 1,845 subjects, with a more uniform racial distribution. Second, the protocols are upgraded due to a greater number of possible

comparisons between images and possible identities.

→ **TinyFace** [16] was presented to fill in the gap of low-resolution face recognition benchmarks with genuine images and not downsampled ones. It is designed for face identification, and is composed of 15,975 labelled images and 153,428 distractors, totalling 169,403 low resolution images, from 5139 identities. The evaluation protocol is similar to the one used by MegaFace: 1) half of the identities are randomly sampled by the probe set and the other half by the gallery set, and 2) the distractor images are added to the gallery incorporating further complexity to the identification process.

→ **IJB-C** [67] adds 1661 new identities to IJB-B and new end-to-end protocols (to evaluate face detection, identification, verification, clustering) in order to better mimic real-world unconstrained recognition. They have increased diversity, both in geographic location and profession, and occlusion scenarios. IJB-C has 31,334 images and 11,779 videos from 3531 subjects.

→ **IJB-S** [48] is a manually annotated benchmark constructed by collecting images and surveillance videos that presents a challenging face recognition problem. It is a dataset with several challenging variations, namely, full pose, resolution, presence of motion blur and visual artifacts. The aforesaid are tested during 6 different face detection and identification protocols. IJB-S consists of 350 surveillance videos, 202 enrollment videos and 5656 images.

→ **RFW** [106] is a proposed benchmark dataset to evaluate the racial bias of face verification solutions. It is divided in 4 subsets regarding the race of the subjects, where each contains, approximately, 10 thousand images and 3 thousand identities, totaling 40,607 images from 11,429 subjects. The evaluation protocol is the same as the LFW one, but the negative pairs were mined to be difficult and avoid easily saturated performance.

→ **QMUL-SurvFace** [17] is a dataset introduced as a benchmark in the *Surveillance Face recognition Challenge* for face recognition in a surveillance context, and it contains both face verification and identification protocols. By data-mining 17 public person re-identification datasets, it achieves 463,507 facial images of 15,573 identities collected in uncooperative surveillance scenarios. Consequently, it presents a high variance in resolution, motion blur, pose, occlusion, illumination and background clutter.

→ **MDMFR** [102] is brought about in light of the COVID-19 impact, where wearing a mask became mandatory and rendered unusable the traditional face recognition methods. Therefore, in conjunction with DeepMaskNet, MDMFR was released. It is a large-scale benchmark dataset designed to evaluate the performance of both masked face recognition and masked face detection algorithms. The recognition protocol contains 2896 images from 226 identities, intended to benchmark masked face recognition models.

→ **XQLFW** [53] revisits the LFW and modifies it to better evaluate cross-resolution face recognition problems. The evaluation protocol, number of images and identities remains the same (13,233 and 5749, respectively), but the negative pairs are sampled in the same manner as CPLFW [130] and CALFW [131].

→ **CAFR** [129] was introduced in 2022, in the revised paper of the AIM (Age-Invariant Model) as a large-scale benchmark dataset to advance the development of face recognition models invariant to age. It consists of 1,446,500 images from 25,000 subjects and spans a range of ages from 1 to 99 years old. The evaluation protocol divides the data in 10 splits of 2500 pair-wise disjoint subjects, where each one has associated to it 5 matched pairs and 5 unmatched, resulting in a total of 25,000 pairs per split.

→ **FaVCI2D** [81] is face verification benchmark dataset that proposes to address

three relevant flaws : 1) the pairs selected are not challenging enough, 2) the demographics of other datasets are not representative enough of the real world diversity and 3) legal and ethical questions concerning the data used. It is composed of 64,879 images and 52,411 unique identities, where 12,468 are used to create genuine matched identity pairs with balanced gender and geographic distribution.

Dataset	Year	Availability	Images/videos	Depth	Avg. Breadth	Distribution	Description
LFW [41]	2007	Discontinued	494,414/-	10,575	46.7	Public	temp
YTF [113]	2011	-	500M/-	10M	50	Private	temp
IJB-A [52]	2015	-	200M/-	8M	25	Private	temp
CFP [92]	2016	Discontinued	2,6M/-	2,622	991.6	Public	temp
MegaFace2* [74]	2016	Discontinued	10M/-	100k	100	Public	temp
CPLFW [130]	2017	temp	4,753,320/-	672,057	7.1	Public	temp
CALFW [131]	2017	temp	3,31M/-	9131	362.5	Public	temp
AgeDB [72]	2017	temp	-/22,075	3,107	7.1	Public	temp
IJB-B [111]	2017	temp	50M/-	500k	100	Public	temp
TinyFace [16]	2018	temp	25M/-	245k	102	Public	temp
IJB-C [67]	2018	temp	1,7M/-	59k	28.8	Public	temp
IJB-S [48]	2018	temp	5,8M/-	85k	68.2	Public	temp
RFW [106]	2018	temp	95k/-	525	180.9	Public	temp
QMUL-SurvFace [17]	2018	temp	95k/-	525	180.9	Public	temp
MDMFR [102]	2021	temp	95k/-	525	180.9	Public	temp
XQLFW [53]	2021	temp	17M/-	360k	47.2	Public	temp
CAFR [129]	2022	temp	95k/-	525	180.9	Public	temp
FaVCI2D [81]	2022	temp	260M/-	4M	65	Public	temp

Table 2

Although some of the previously referenced datasets do have a benchmarking component and are described as such, they can also be generally employed to train algorithms. When it is desired to fine-tune<sup>11</sup> a model for a specific challenge that, usually, can be better achieved by employing a "benchmark" dataset that was purposefully developed to evaluate a model's performance on that exact challenge.

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<sup>11</sup> An approach to transfer learning (producing a new model by using a pre-trained as a starting point) [134]. More details on this topic in the section Transfer Learning.

A common denominator throughout the machine learning domain, and more specifically deep learning, is a general difficulty in separating concepts with a single line. This is a non-linear science in its nature.

### 2.4.2 Feature Extractor

A feature extractor is present in both the training and testing stage of the Face Representation process, and comprehends a fundamental part of it, as it is what allows the visual data to be processed and transformed to be evaluated, by transforming the input into low dimensional representations [58]. It is also what distinguishes a Conventional Machine Learning approach from a Deep Learning one.

Being that the following methods are all based in deep learning, therefore, the *modus operandi* abides by the same principles and can be outlined as follows: 1) the feature extractor is a deep neural network, more specifically a Convolutional Neural Network (CNN), that is trained with a loss function, 2) the trained feature extractor contains prior knowledge and is applied on unseen test data and 3) the results are used to compute 1:N similarity (face identification - "who is this person?") or 1:1 similarity (face verification - "are these persons the same?").

The following section will be divided as follows: first, the general architecture and training process of a CNN will be described, then, a brief overview of loss functions and how similarity is computed in face recognition, and finally, related works regarding face recognition are reviewed.

## Convolutional Neural Networks

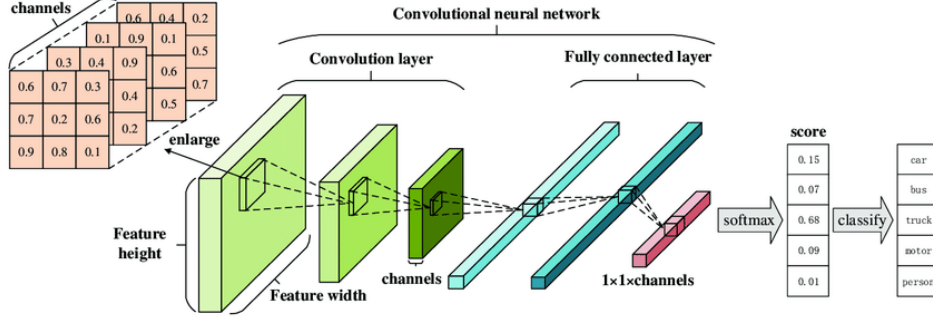


Figure 4: Architecture of a Convolutional Neural Network [49].

There are several types of Neural Networks architectures, but Convolutional Neural Networks (CNNs or Convnets) are probably the most widely implemented model overall [117, 61]. Using CNNs for Computer Vision tasks [54, 96, 99, 125], in this specific case, Face Recognition, is not an arbitrary choice, but due to the fact that the network design benefits from the intrinsic characteristics of the input data: images have an array-like structure [117], and local groups of values are correlated (motifs or patterns) and invariant to spatial location [57, 12]. Furthermore, when compared to fully connected networks, CNNs are superior due to 4 key features: 1) Shared weights between the same features in different locations reduce the number of parameters [61], 2) sparse connections [3], 3) pooling layers and 4) automatically identifies the relevant features without any human supervision [3, 61].

In the CNN category itself there are different variants, but they all abide the fundamental structure of a feedforward hierarchical multi-layer network (Figure 4). Feedforward because the information only flows in a singular direction without cycling [122], hierarchical because the higher complexity internal representations are learned from lower ones [57, 132] and multi-layer because it is composed of a series of stages, blocks or layers. The raw data is fed to an input layer, forwarded to a sequence of intercalating convolutional and pooling layers, transmitted to a stage of one or more fully-connected layers [57, 34, 3].

## Convolutional Layer

The convolutional layer aims at extracting feature representations from the inputs, and is formed by a set of learnable filters called **kernels** and an **activation function** [34, 117].

-1	0	+1
-2	0	+2
-1	0	+1

**Gx**

+1	+2	+1
0	0	0
-1	-2	-1

**Gy**

Figure 5: 3x3 Kernels of the Sobel-Feldman operator used for edge detection [94].

A **kernel**<sup>12</sup> (Figure 5), is a grid-like structure of fixed dimensions  $[W \times H \times D]$ , where  $W$  is the width and  $H$  is the height. The dimension  $D$  relates to the depth of the kernel and is used to multichannel images, such as RGB ones (3 channels). Each of its elements is a learnable weight that is adjusted during training to extract significant features [3].

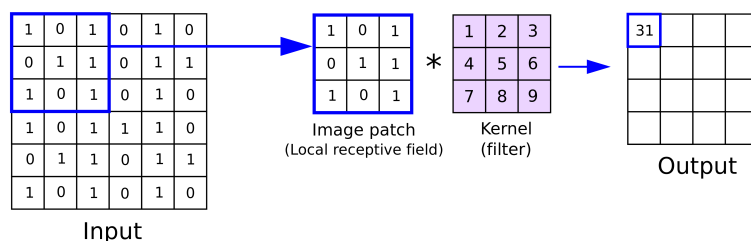


Figure 6: Convolution

With a predetermined **stride**, the kernel scans its receptive field [50], horizontally and vertically, through the input data, and produces the feature map<sup>13</sup> [57, 3] by performing an element-wise product, called **convolution** (Figure 6), that

<sup>12</sup> Or feature detector [2].

<sup>13</sup> Also referred to as feature representation [61] or activation map [2].

can be described as follows [50]:

$$f_l^k(p, q) = \sum_c \sum_{x, y} i_c(x, y) \cdot w_l^k(u, v)$$

where  $f_l^k(p, q)$  is an element at line  $p$  and column  $q$  in the feature map from the  $k$ -th kernel in the  $l$ -th layer,  $i_c(x, y)$  is the element at line  $x$  and row  $y$  in the input data, and  $w_l^k(u, v)$  is the weight at line  $u$  and column  $v$  from the  $k$ -th kernel of the  $l$ -th layer.

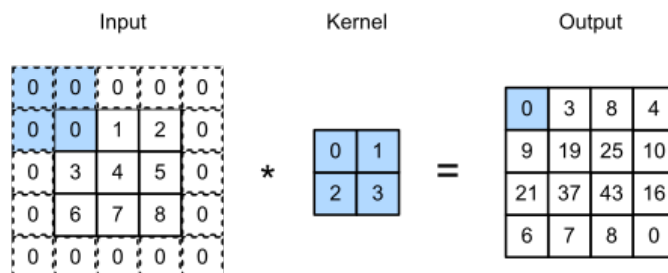


Figure 7: Convolution

At the edge of the input, it's not possible to overlap the whole kernel over all the elements, reaching a point where it can't shift anymore, so the dimensions of the feature map would be unintentionally reduced and information would be lost. Therefore, as seen in (Figure 7), usually **zero padding** is employed to solve the aforesaid problems [117].

The overall architecture of CNNs are inspired by the visual perception [44], so a direct parallelism can be made to better define the **activation function**. The kernels can be seen as receptors, or artificial neurons, that respond to different features, whereas the activation function is a simulation of the threshold function that dictates if the next neuron is activated or not. Additionally, the convolution operation is linear, consequently, if no nonlinear activation function was used, the input of the next layer would be a linear output of the previous layer. The introduction of nonlinearity, such as ReLU (Rectified Linear Unite) [73], allows deep neural networks to approximate any function, enhancing the ability to fit to any data [61].



## Pooling Layer

After the features are extracted, the spatial location of them become less relevant for the following layers. Introducing a pooling layer with the purpose of reducing the spatial size of the feature maps by joining identical features [57, 34], then only the dominant response will prevail. This downsampling operation has two important advantages that help reduce the overfitting problem [2, 61]. First, it reduces the number of learnable features, which requires less memory to train the network. Second, it enhances feature extraction invariance to shifts and rotations by emphasizing only the relevant features.

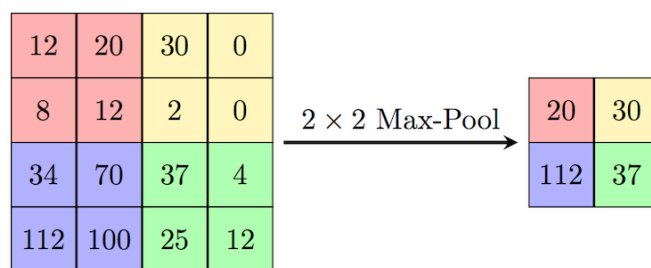


Figure 8: Max pool

There are many ways of downsampling the feature map through pooling such as min pooling, average pooling or stochastic pooling, however max pooling is by far the most popular one. As pictured in (Figure 8), this operation divides the feature map in sections and computes the maximum value in each while discarding the other ones.

## Fully Connected Layer (?)

The fully connected (FC) layer is located at the end of the network. It is a dense, feedforward neural network in which every neuron is connected to all other neurons [117, 3]. The final feature map is flattened and transformed in a one-dimensional feature vector and the purpose of the FC layer is using this vector as an input, and act as the CNN classifier by performing high logic reasoning [34].

## Training

Training a network in the context of CNNs is the process of finding the optimal kernel weights' values. The training data is passed through the model, the predictions asserted and the distance between them and the expected ones is measured by a loss function. LeCun *et al.* [58] presents the problem as follows:

$$E^p = \mathcal{D}(D^p, Y^p)$$

The loss function,  $E^p$ , is a measure of error. It computes the difference between the expected result,  $D^p$ , and the predicted result  $Y^p$ , where  $Y^p = F(Z^p, W)$  is a function of the  $p$ -th training example,  $Z^p$ , for a determined weight  $W$ . Additionally,  $E_{train}(W)$ , is the average of all the errors calculated in a training set  $\{(Z^x, D^x), \dots (Z^p, D^p)\}$ . Training the network is nothing more than a function minimization problem, and for that there are several techniques, the **optimizers**.

## Optimizers

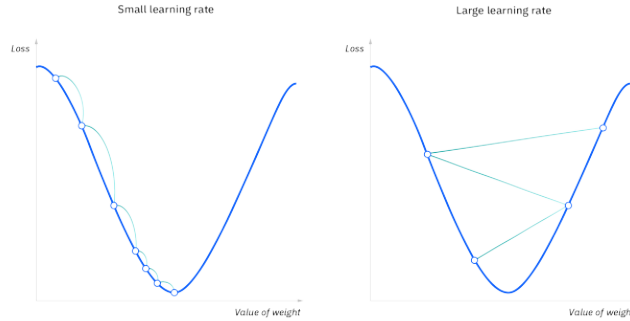


Figure 9: Gradient descent

By computing the gradient of the loss function in respect to the learnable parameters it allows studying how said parameters influence the loss function and how it can be more efficiently minimized. This algorithm is called **gradient descent** [88], and is the simplest minimization technique. By definition, the gradient

of a function is the direction of the steepest ascent, henceforth, the learnable parameters are updated once every epoch in the opposite direction to reduce the error:

$$W_k = W_{k-1} - \epsilon \frac{\delta E(W)}{\delta W}$$

where  $\epsilon$  is a constant called **learning rate** that controls how much the parameters are updated and has an immense impact in the performance of a neural network (Figure 9). According to Goodfellow *et al.* [33], if the learning rate is set too low, training will be much slower and can become permanently stuck with a high training error. On the other hand, if the learning rate is too high, the gradient descent can increase the training error instead of reducing it.

**Stochastic Gradient Descent** (SGD) [3] is the algorithm of choice to optimize the loss function and its main difference is that the parameters updating routine. First, training samples are randomly sampled in every epoch, then the gradient is calculated for each at a time, and, finally, the parameters are updated accordingly. This is an efficient algorithm in terms of memory usage, but, since the updates occur once at every sample, the convergence can be noisy. Other optimizers worth of mentioning are: **1) Mini-batch Gradient Descent** - divides the training data into non-overlapping batches and the parameters are updated on each one of them; **2) Momentum** [80] - introduces a new hyperparameter to the network called momentum, that accumulates previous gradients, that accelerates the optimizer in the correct direction of minimization and reduces error's oscillation during optimization; **3) Adam (Adaptive moment estimation)** [51] - uses the first and second moments of the gradients (gradient's mean and variance, respectively) to better optimize the parameters.

## Backpropagation

Regardless of the optimizer selected, computing an analytical expression for the gradient is trivial, but evaluating it is a computational heavy task when the aim is to find a minimum with respect to all the parameters in the network. To

this extent, the backpropagation (or backprop) algorithm is a solution to do so efficiently [56]. Backprop is usually referred to as a training algorithm, but that is not true. **Backpropagation is not a training algorithm**, it is simply the method of computing the gradient using a fixed sequence, efficient application of the *Chain Rule of Calculus*  $\left(\frac{dz}{dx} = \frac{dz}{dy} \frac{dy}{dx}\right)$ , considering that it starts at the final layer, and proceeding backwards[33].

## Transfer Learning

Developing a Deep Learning system requires data in large scale [79], specially labeled one. In a general sense, gathering information can be very difficult, but if the domain of study is too specific or not widespread enough, that poses an even bigger challenge. To overcome this solution, based on the psychologist C.H. Judd's theory, a technique called Transfer Learning takes place. It is defined by Zhuang *et al.* [134] as: given a source and target domain, transfer learning is the act of utilizing the knowledge acquired in the source to further improve the performance of the learned decision functions on the target domain. A classic example is the case of learning how to ride a motorcycle. It will be easier for someone who has already learned how to ride a bicycle than it is to someone starting from scratch.

In the context of CNNs, there are 2 ways of approaching the aforesaid problem. By taking a pre-trained CNN and either use it as a fixed feature extractor or fine-tune it. In the first case, an already trained CNN is used, however, the final few layers or the fully connected one is discarded and retrained to a specific task, while the rest of the network is frozen and used as the feature extractor that will feed the classifier input. The second approach is referred to as fine-tuning a network and, as the name suggests, the source network's parameters are used as a starting point and is entirely retrained using the desired data. It is also common to freeze the first layers since they are responsible to extract the more general, universal features (edges or patterns).

### **2.4.3 Loss**

### **2.4.4 Similarity**

Define hyperparameter, epoch

# Chapter 3

## Methodology

### 3.1 Joint Face Detection and Alignment

### 3.2 Face Representation

# Chapter 4

## Results

## Chapter 5

## Conclusion



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