NAME:

Due at the beginning of class on 22 April 2024

- Your answers should be neatly written and logically organized.
- You may collaborate on solving the problems, but the solutions you turn in should be your own.
- You may use any resource you find online (or elsewhere), but you must cite any resource you use.

Reading: [Mal23, Sections 6.1 and 6.2].

- (1) Let $F \dashv G$ be an adjoint pair of functors between monoidal categories.
 - (a) Show that if F is strong symmetric monoidal, then G is lax symmetric monoidal.
 - (b) If G is lax symmetric monoidal, can you say anything about F? Give a proof or counterexample.
- (2) Every spectrum X is an S-module. Describe the π_* S-action on π_* X.
- (3) Let R be a commutative ring spectrum.
 - (a) Show that the forgetful functor from the category of R-module spectra to symmetric (or orthogonal) spectra has a left adjoint.
 - (b) Let M be an R-module spectrum such that π_*M is free as a graded π_*R -module. Show that M is stably equivalent to a wedge sum of shifts of copies of R.

REFERENCES

- [Mal23] Cary Malkiewich. Spectra and stable homotopy theory. http://people.math.binghamton.edu/malkiewich/spectra_book_draft.pdf, October 2023.
- [Sch07] Stefan Schwede. An untitled book project about symmetric spectra. http://www.math.uni-bonn.de/people/schwede/SymSpec.pdf, 2007.