What is hiding inside the number 3?

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So what is hiding inside the number 3? Well, consider:

$$3 = \sqrt{9}$$

$$= \sqrt{1+8}$$

$$= \sqrt{1+2*4}$$

$$= \sqrt{1+2\sqrt{16}}$$

$$= \sqrt{1+2\sqrt{1+15}}$$

$$= \sqrt{1+2\sqrt{1+3*5}}$$

$$= \sqrt{1+2\sqrt{1+3*5}}$$

$$= \sqrt{1+2\sqrt{1+3\sqrt{25}}}$$

$$= \sqrt{1+2\sqrt{1+3\sqrt{1+24}}}$$

$$= \sqrt{1+2\sqrt{1+3\sqrt{1+4*6}}}$$

$$= \sqrt{1+2\sqrt{1+3\sqrt{1+4*6}}}$$

$$= \sqrt{1+2\sqrt{1+3\sqrt{1+4\sqrt{1+35}}}}$$

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$$= \sqrt{1+2\sqrt{1+3\sqrt{1+4\sqrt{1+35}}}}$$

$$= \sqrt{1+2\sqrt{1+3\sqrt{1+4\sqrt{1+5*7}}}}$$

$$= \sqrt{1+2\sqrt{1+3\sqrt{1+4\sqrt{1+5\sqrt{49}}}}}$$

$$= \cdots$$

$$\# 49 = 1+48, 48 = 6*8, 8 = \sqrt{64}, \dots$$

and so apparently
$$3 = \sqrt{1 + 2\sqrt{1 + 3\sqrt{1 + 4\sqrt{1 + 5\sqrt{1 + 6\sqrt{64}}}}} \cdots$$