```
\begin{array}{lll} e^{ix} & = & i\cos x + i\sin x & \# \text{ Euler's formula} \\ & \Rightarrow & e^{i\frac{\pi}{2}} = \cos\frac{\pi}{2} + i\sin\frac{\pi}{2} & \# \text{ set } x = \frac{\pi}{2} \\ & \Rightarrow & e^{i\frac{\pi}{2}} = 0 + i & \# \text{ trig} \\ & \Rightarrow & (e^{i\frac{\pi}{2}})^i = i^i & \# \text{ raise both sides to } i \\ & \Rightarrow & e^{i\frac{\pi}{2}} = i^i & \# \text{ algebra} \\ & \Rightarrow & e^{-\frac{\pi}{2}} = i^i & \# i^2 = -1 \\ & \Rightarrow & e^{-\frac{\pi}{2}} \text{ is real } \Rightarrow i^i \text{ is a real number} \end{array}
```