

Fermat's Christmas Theorem

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Fermat's Christmas Theorem [1] is a beautiful and simply stated theorem. It is called Fermat's Christmas Theorem because Fermat announced a proof of the theorem in a letter to Mersenne dated December 25, 1640.

The prime numbers p for which the theorem is true are called Pythagorean primes. See [2] for more on Pythagorean primes.

Fermat's Christmas Theorem (aka Fermat's theorem on sums of two squares) states that an odd prime number p can be expressed as

$$p = r^2 + s^2$$

where $r, s \in \mathbb{N}$, if and only if $p \equiv 1 \pmod{4}$.

References

- [1] Wikipedia contributors. Fermat's theorem on sums of two squares — Wikipedia, the free encyclopedia. https://en.wikipedia.org/w/index.php?title=Fermat%27s_theorem_on_sums_of_two_squares&oldid=990575323, 2020. [Online; accessed 26-December-2020].
- [2] Wikipedia contributors. Pythagorean prime — Wikipedia, the free encyclopedia. https://en.wikipedia.org/w/index.php?title=Pythagorean_prime&oldid=985939468, 2020. [Online; accessed 26-December-2020].