

ECE 345/ME 380: Introduction to Control Systems

Problem Set #4

1. Consider the lead controller $G(s) = \frac{s + 4}{s + 10}$.

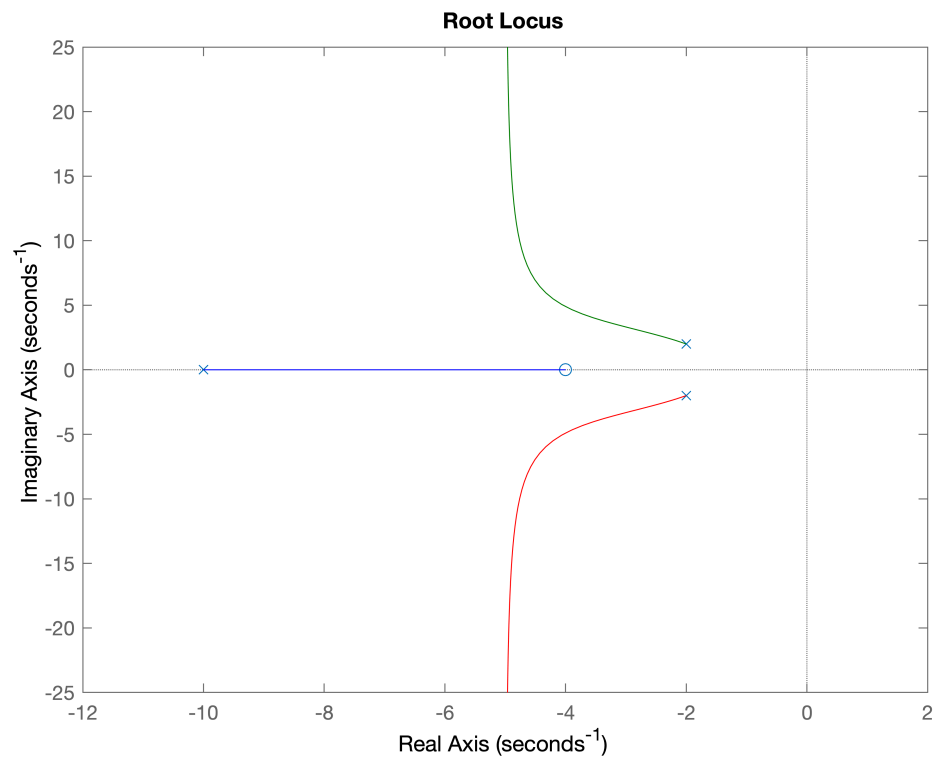
```
GcG1 = tf(8*[1 4],conv([1 10],[1 4 8]))
```

GcG1 =

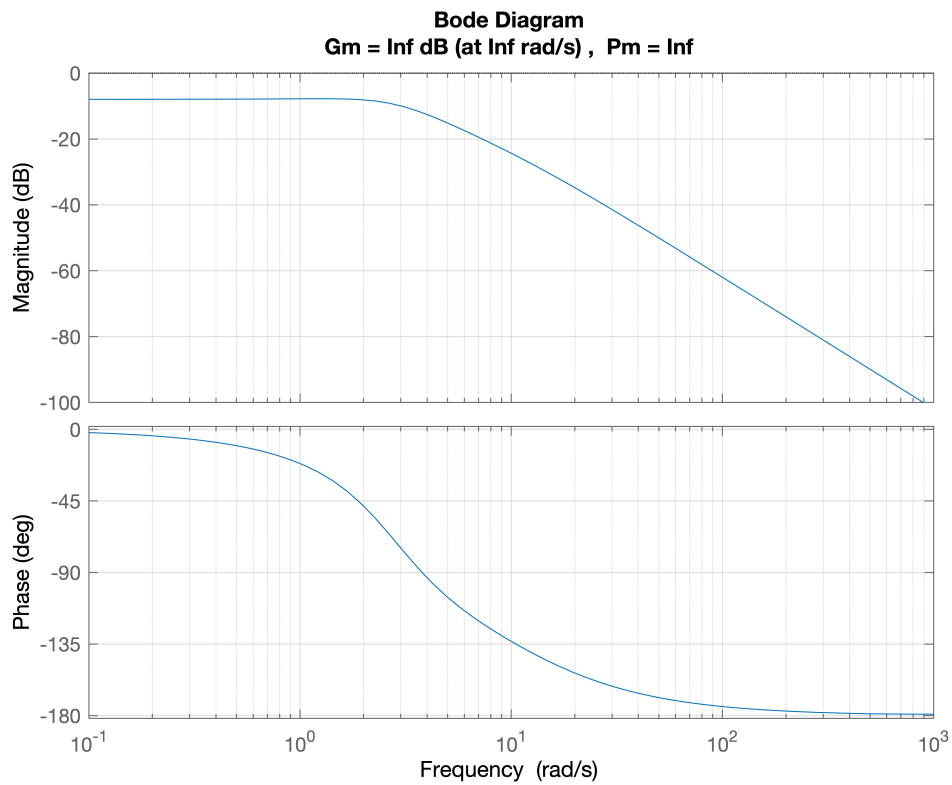
$$\frac{8s + 32}{s^3 + 14s^2 + 48s + 80}$$

Continuous-time transfer function.

```
rlocus(GcG1)
```



```
margin(GcG1);grid on
```



2. Consider the lag controller $G(s) = \frac{s + 10}{s + 4}$.

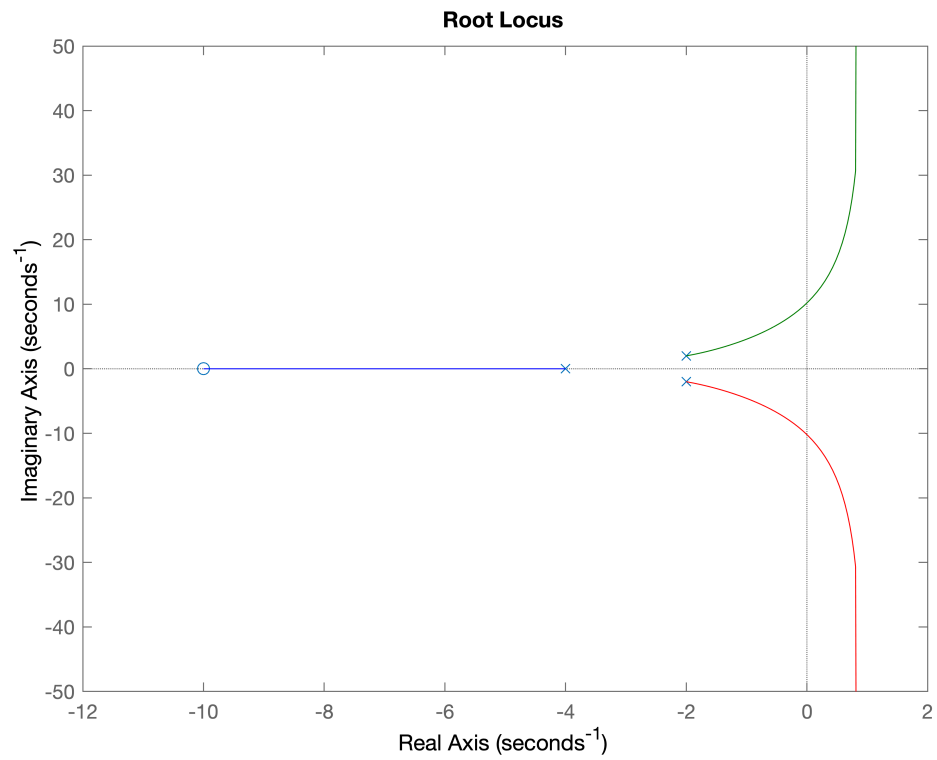
```
GcG2 = tf(8*[1 10],conv([1 4],[1 4 8]))
```

GcG2 =

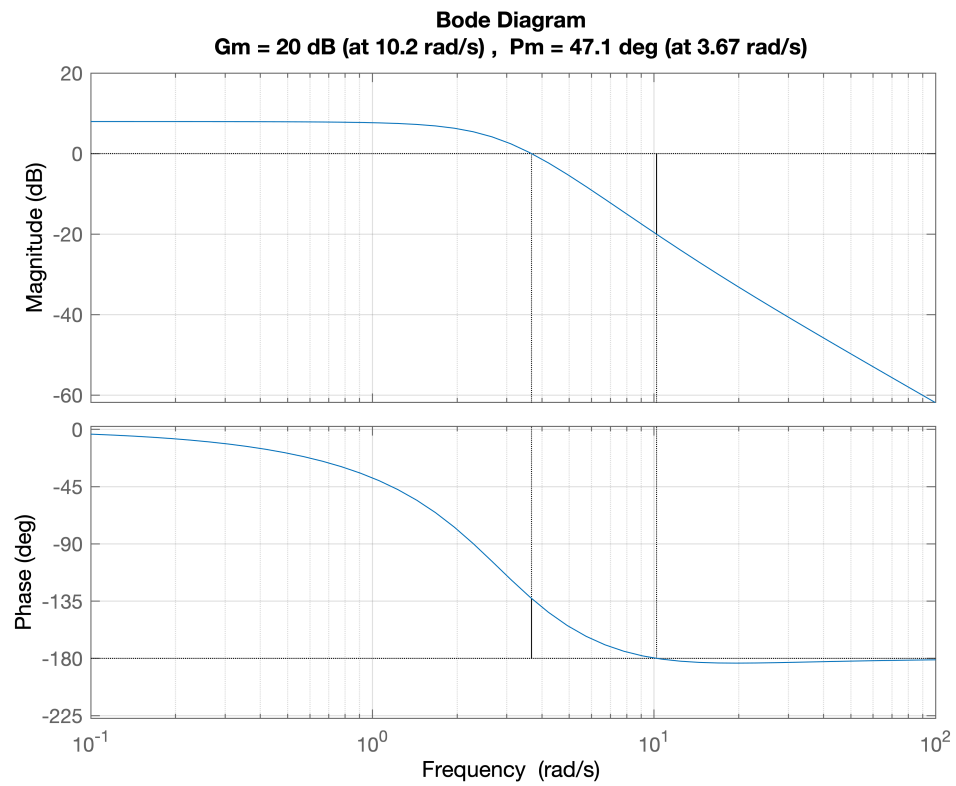
$$\frac{8s + 80}{s^3 + 8s^2 + 24s + 32}$$

Continuous-time transfer function.

```
rlocus(GcG2)
```



```
margin(GcG2);grid on
```



4. Consider the effect of a Proportional-Integral-Derivative (PID) controller

$$G_c(s) = K \frac{(s+4)(s+10)}{s} = 14K + \frac{40K}{s} + Ks.$$

```
GcG3 = tf(8*[conv([1 10],[1 4]),conv([1 0],[1 4 8])])
```

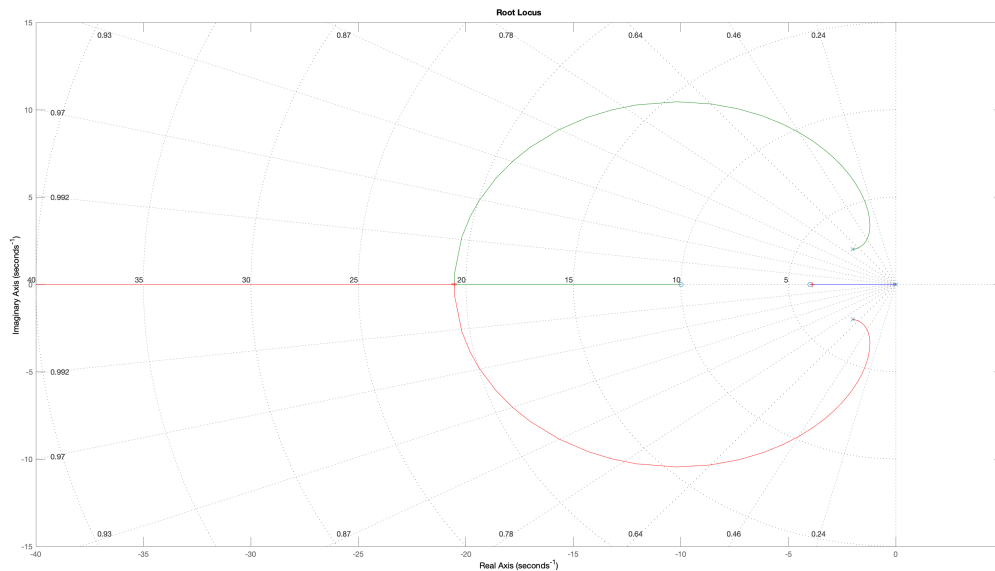
GcG3 =

$$\frac{8s^2 + 112s + 320}{s^3 + 4s^2 + 8s}$$

Continuous-time transfer function.

```
rlocus(GcG3);grid on  
rlocfind(GcG3)
```

Select a point in the graphics window



```
selected_point = -20.5262 + 0.0322i  
ans = 5.1213
```