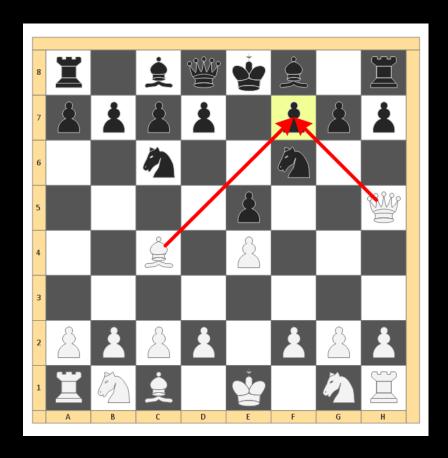


How do knights move?

David Na EN.685.648 FA21 Lab Group 4

Problem Statement

Can we predict a victory for white?



Target Variable

$$\hat{y} = \begin{cases} 0, \\ 1, \end{cases}$$

if white did not win if white wins

$$\hat{y} = \beta_0 + \beta_1 x$$

The main target variable will be whether white wins or not.

We must one hot encode our target variable

The logistic model will output how the probability of y changes as our x changes.

$$logistic(z) = logit^{-1}(z) = \frac{e^z}{1+e^z} = \frac{1}{1+e^{-z}}$$

In order to keep our variables to the range (0,1) we transform the variable using the logistic function.

(Module 9-10 Content)

Get

The Database: ChessDB.db

TABLES:

countries : Maps country to Two letter code

users : List of all scraped users

users_selected : List of all the users I select to scrape from

all_games_raw : List of all available games

all_games_country : List of all games with the country filled

all_games_country_selected : List of all games selected with country

all_games_countries_winstreak : NOT INCLUDED IN DATA

Extracting the data: Step 1



Extract Users from a Team: (Only able to query by username for games)

```
M from Extractor import *
API_URL = 'https://lichess.org/'
AccessToken = "lip_FdeTEN7DhU3ge3Eg8Shu"
API = LichessRequestor(Token = AccessToken, base_url = API_URL)

M path = f'api/team/agadmators-team/users'
data = API.get(path=path)

M users_raw = LichessRequestor.parse(data)

M user_list = LichessRequestor.parse_team(users_raw)
```

```
Select t1.id, t1.blitz games, t1.blitz_rating, t1.rapid_games, t1.rapid_rating, t1.bullet_games,
t1.bullet rating, t1.country
(SELECT
   id, blitz games, blitz rating, rapid games, rapid rating, bullet games, bullet rating,
   (CASE country
       WHEN "GB-ENG" THEN "UK"
       WHEN "GB-NIR" THEN "UK"
       WHEN "GB-WLS" THEN "UK"
       WHEN " united-nations" THEN "UK"
       WHEN "ES-CT" THEN "ES"
       WHEN "CA-QC" THEN "CA"
       ELSE country
   END) as country
FROM users
country not in ("No Country", " east-turkestan", " adygea", " earth", " belarus-wrw",
'_lichess", "_pirate", "_rainbow", "east-turkestan")
AND blitz games > 100
AND rapid games > 100
AND bullet games > 100) t1
```

Using the User list created above, I run a SQL query to "clean" the data. I also choose to only include users who have played at least 100 games in the three types of games I query for

Extracting the data: Step 2



```
## Random sampling from the user dataset
## Querying all the data would take 60 hours...
userlist cleaned = []
AllUsers = pd.DataFrame()
Ratingless800 = users[users['blitz_rating'] <= 800]
Rating800to1000 = users[(users['blitz rating'] > 800) & (users['blitz rating'] <= 1000)]</pre>
Rating1000to1200 = users[(users['blitz rating'] > 1000) & (users['blitz rating'] <= 1200)].sample(100)</pre>
Rating1200to1400 = users[(users['blitz_rating'] > 1000) & (users['blitz_rating'] <= 1200)].sample(100)
Rating1400to1600 = users[(users['blitz_rating'] > 1400) & (users['blitz_rating'] <= 1600)].sample(250)
Rating1600to1800 = users['users['blitz_rating'] > 1600) & (users['blitz_rating'] <= 1800)].sample(250)
Rating1800to2000 = users['users['blitz rating'] > 1800) & (users['blitz rating'] <= 2000)].sample(250)
Rating2000to2200 = users[(users['blitz rating'] > 2000) & (users['blitz rating'] <= 2200)].sample(250)
RatingAbove2200 = users[(users['blitz_rating'] > 2200)].sample(250)
userlist cleaned = [Ratingless800, Rating800to1000, Rating1000to1200, Rating1200to1400, Rating1200to1400
        Rating1400to1600, Rating1600to1800, Rating1800to2000, Rating2000to2200, RatingAbove2200]
UsersSelected = pd.concat(userlist cleaned, ignore index = True)
UsersSelected.to_csv("Users_Selected.csv")
```

Based on the cleaned set of users, I sample the dataset by rating bracket. I take users from every increment of 200 rating from 800 to 2200.

The lower ratings had less users – sample less

```
## Query games from user database
  all games = []
  all games df = pd.DataFrame()
  for i in range(len(UsersSelected)):
      print(i)
      params = {
           'max': 15.
           'rated': True,
           'perfType': 'blitz,rapid,bullet',
           'analysed': True,
           'evals': True.
           'opening': True,
      username = UsersSelected['id'][i]
      path = f'api/games/user/{username}
      games = API.get(path=path, params = params)
      games data = LichessRequestor.parse(games, convert=False)
      data = LichessRequestor.parse games(games data, LichessRequestor)
      all games.append(data)
   all games df = pd.concat(all games, ignore index = True)
all games df.to csv("all games.csv")
```

I run a for loop for each user in the user selected list provided above

I pull 15 games of type: blitz, rapid, bullet for each user

Data Dictionary



| gameid | The unique game id |
|--------------------|---|
| white_id | The unique player id for white |
| white_rating | The rating for white for specific game type |
| white_country | The country of origin for white |
| white_games | Then number of games played for white (of type = game_type) |
| white_win_last_10 | How many wins for white in last 10 games (omitted) |
| white_inaccuracies | Number of inaccuracies |
| white_mistakes | Number of mistakes |
| white_blunder | Number of blunders |
| white_acpl | Adjusted score of evaluation - Average Centipawn Loss |
| game_type | The type of the game: Blitz, Rapid, Bullet |
| opening | The opening played by white |
| winner | The winner (white or black or draw) |
| win_by | Outcome of the game (resign, draw, stalemate, etc.) |

The variables for white are also provided for black

Extracting the data: Step 3



```
## White details
api = LichessRequestor(Token = AccessToken, base_url = API_URL)
white_id = games_data['white_id'][index]
path_white = f'api/user/{white_id}'
white = LichessRequestor.parse(api.get(path=path_white))
if 'profile' in white[0]:
    if 'country' in white[0]['profile']:
        games_data['white_country'][index] = (white[0]['profile']['country'])
    else:
        games_data['white_country'][index] = ("No Country")

else:
    games_data['white_country'][index] = "No Country"

try:
    games_data['white_games'][index] = white[0]['perfs'][game_type]['games']
except:
    games_data['white_games'][index] = -1
    pass
```

For every game that we pulled, we run another API call step to pull the number of games played as well as the country of origin for the player

The API get request does not pull profile information with the game data.

Done for Black and White

Extracting the data: Step 4



```
params = {
    'max': 10,
    'until': game_time,
    'rated': True,
    'perfType': game_type,
    'tags': False,
    'moves': False,
    'clock': False
}
```

The next step of the API was to call the requestor again and parse the last ten games of the same game type played by the user.

We can pull the user games as we recorded each users' id

This step was taking over 24 hours to complete. I was able to run it successfully once, but then my python kernel died. I lost the metadata and was not able to rerun this step.

The Database: ChessDB.db

TABLES:

countries : Maps country to Two letter code

users : List of all scraped users

users_selected : List of all the users I select to scrape from

all_games_raw : List of all available games

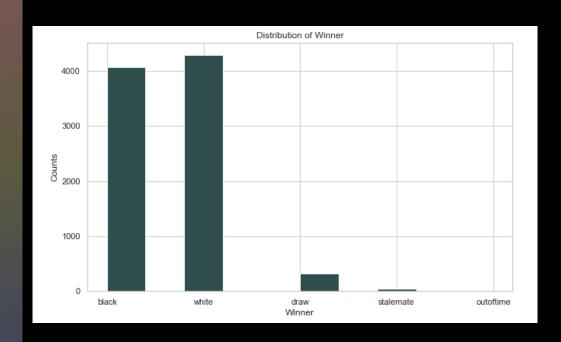
all_games_country : List of all games with the country filled

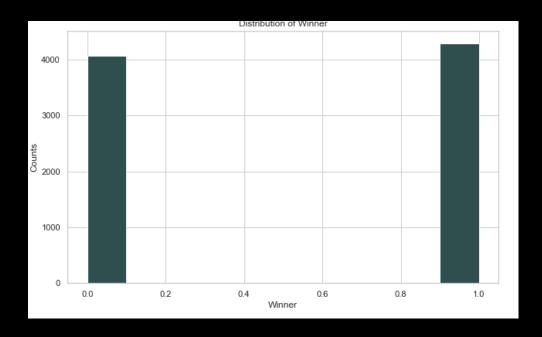
all_games_country_selected : List of all games selected with country

all_games_countries_winstreak : NOT INCLUDED IN DATA

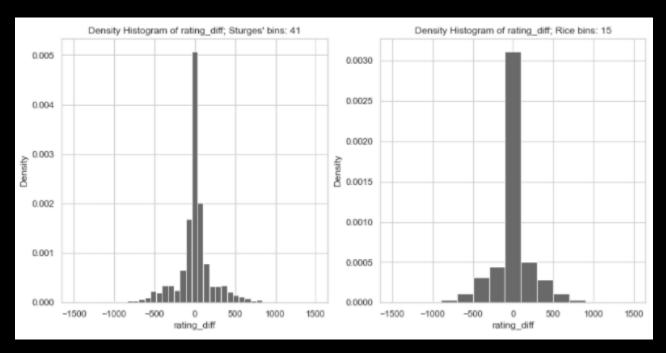
Explore

Target Variable: Winner





Rating – Taking the Difference

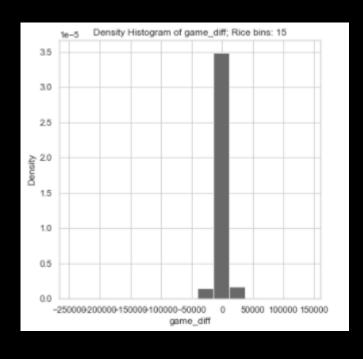


When Rating Diff is 0 1984 2274 When Rating Diff is 100 686 900 Rating Diff is 200 476 525 Rating Diff is 300 409 367 When Rating Diff is 400 193 240

When Rating Diff is 500
96
169
When Rating Diff is 600
43
104
When Rating Diff is 700
13
62
When Rating Diff is 800
5
39
When Rating Diff is 900
2
24

White wins with the higher rating White wins with the lower rating

Number of Games - Difference

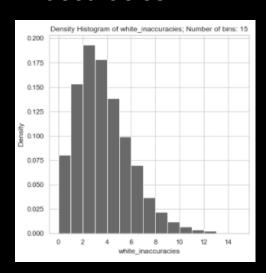


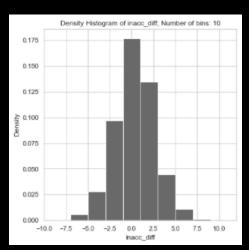
Still disparity in win probability despite high differences in game counts.

| | white_games | black_games | winner |
|------|-------------|-------------|--------|
| 2135 | 61.0 | 103123.0 | 1 |
| 2136 | 103123.0 | 52.0 | 0 |
| 2137 | 22.0 | 103123.0 | 1 |
| 2138 | 247.0 | 103123.0 | 1 |
| 2139 | 416.0 | 103123.0 | 1 |
| 2140 | 103123.0 | 496.0 | 1 |
| 2377 | 127085.0 | 765.0 | 0 |
| 2564 | 2978.0 | 116036.0 | 1 |
| 3010 | 2044.0 | 115046.0 | 1 |
| 3569 | 24001.0 | 270321.0 | 1 |
| 3583 | 1657.0 | 105070.0 | 0 |
| 3638 | 116752.0 | 956.0 | 1 |
| 3952 | 118440.0 | 4089.0 | 1 |
| 5038 | 2694.0 | 128454.0 | 0 |
| 7241 | 146377.0 | 5598.0 | 1 |
| 8148 | 118977.0 | 2603.0 | 1 |

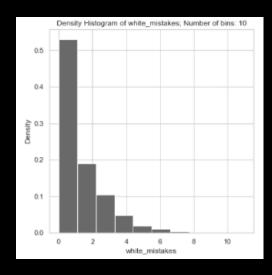
Inaccuracies, mistakes and blunders density histograms

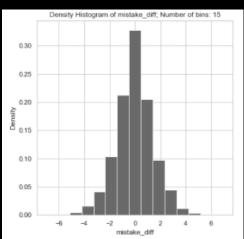
Inaccuracies



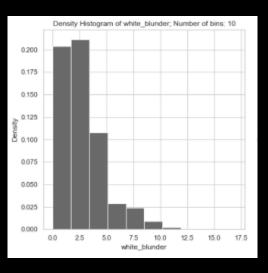


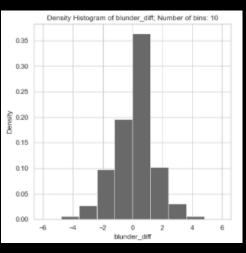
Mistakes





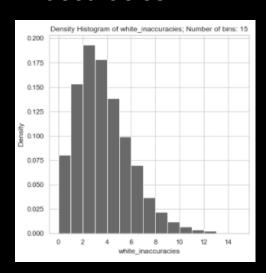
Blunders

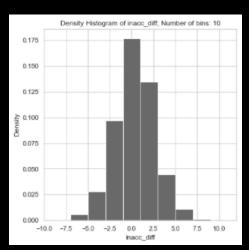




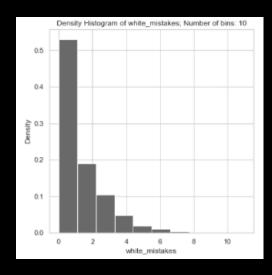
Inaccuracies, mistakes and blunders density histograms

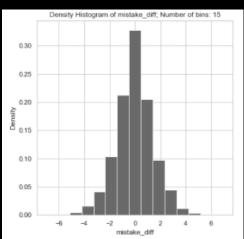
Inaccuracies



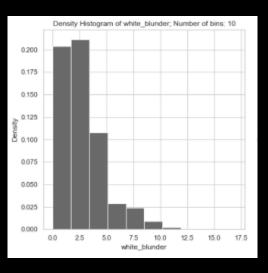


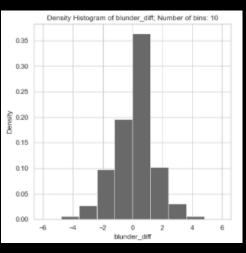
Mistakes



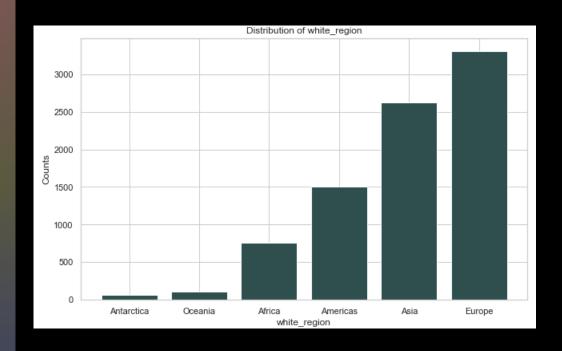


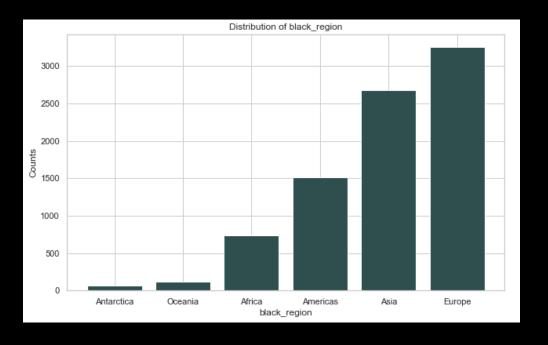
Blunders



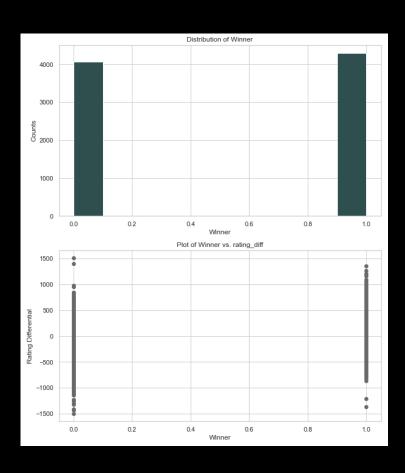


Country to Continent





Winner vs. Rating



Data seems to be relatively uniform between wins and losses

There seems to be some change in the win rate as the rating differential increases.

Winner vs. Inaccuracies, mistakes, and blunders

| winner | 0 | 1 |
|--------|-------------|-------------|
| count | 4066.000000 | 4295.000000 |
| mean | 0.382932 | -0.654482 |
| std | 2.266759 | 2.239671 |
| min | -9.000000 | -9.000000 |
| 25% | -1.000000 | -2.000000 |
| 50% | 0.000000 | -1.000000 |
| 75% | 2.000000 | 1.000000 |
| max | 9.000000 | 11.000000 |

Delta Inaccuracies

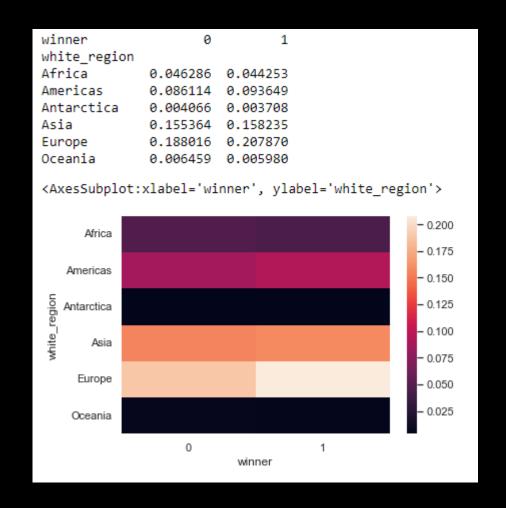
| winner | 0 | 1 |
|--------|-------------|-------------|
| count | 4066.000000 | 4295.000000 |
| mean | 0.228234 | -0.269616 |
| std | 1.605663 | 1.549057 |
| min | -6.000000 | -7.000000 |
| 25% | -1.000000 | -1.000000 |
| 50% | 0.000000 | 0.000000 |
| 75% | 1.000000 | 1.000000 |
| max | 7.000000 | 6.000000 |
| | | |

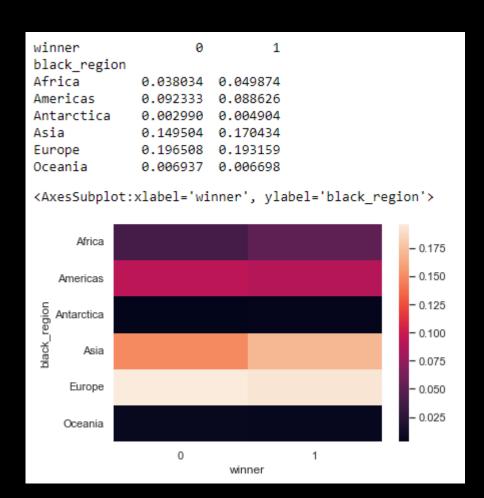
Delta Mistakes

winner 4066,000000 4295.000000 0.933104 -0.864261 mean 1,222734 1.285725 std -6.000000 min -6.000000 25% -2.000000 0.000000 50% -1.000000 1.000000 75% 0.000000 2.000000 6.000000 5.000000 max

Delta Blunders

Winner vs. Region Black and White





Winner vs. Same region, Same Country

0 0.603158
1 0.396842
Name: same region, dtype: float64

winner 0 1 same_region 0 0.299725 0.303433 1 0.186581 0.210262 0 0.862935
1 0.137065
Name: same country, dtype: float64

winner 0 1 same_country 0 0.423155 0.439780 1 0.063150 0.073915

Results seem to indicate that there may be some change caused by two players being from the same region but not from the same country

Model

Null Model

Baseline Model: Bernoulli Distribution

For the Bernoulli model, we learned that we could predict with a single parameter.

p = the probability of "success"

p = The probability of white winning the next game

Given:

$$\hat{y} = \begin{cases} 0, & \text{if white did not win} \\ 1, & \text{if white loses} \end{cases}$$

Our Null Model:

$$p = mean(\hat{y})$$
$$p = 51.37\%$$

There is a 51.37% chance that white wins the next chess match.

Logistic Regression

Model With All Variables

| | | | 95% BCI | | |
|------------------------|--------------------|-------|---------|-------|--------|
| Coefficients | | Mean | Lo | Hi | P(y=1) |
| | $oldsymbol{eta}_0$ | -0.00 | -0.05 | -0.00 | 0.50 |
| white_rating | β_1 | -0.00 | -0.00 | -0.00 | -0.00 |
| white_games | β_2 | 0.00 | -0.00 | 0.00 | 0.00 |
| rating_diff | β_3 | 0.00 | 0.00 | 0.00 | 0.00 |
| game_diff | β_4 | 0.00 | 0.00 | 0.00 | 0.00 |
| inacc_diff | ρ_5 | 0.00 | -0.01 | 0.09 | 0.00 |
| mistake_diff | β_6 | 0.00 | -0.01 | 0.14 | 0.00 |
| blunder_diff | β_7 | 0.00 | 0.00 | 0.30 | 0.00 |
| acpl_diff | β_8 | 0.10 | 0.09 | 0.11 | 0.03 |
| same_region_yes | β_9 | 0.00 | -0.00 | 0.08 | 0.00 |
| blitz | β_{10} | 0.00 | -0.07 | 0.00 | 0.00 |
| rapid | β_{11} | -0.00 | -0.01 | 0.02 | -0.00 |
| Metrics | Mean | Lo | Hi | | |
| | | | | | |
| Error (%) | 7.99 | 7.22 | 8.60 | | |
| Efron's R ² | 0.74 | 0.72 | 0.76 | | |

Model With All Variables (3 sd)

| | 95% BCI | | | | | | | |
|-----------------|------------------------|--------|--------|--------|--------|--|--|--|
| Coefficients | | Mean | Lo | Hi | P(y=1) | | | |
| | $oldsymbol{eta}_0$ | -0.000 | -0.047 | -0.000 | 0.500 | | | |
| white_rating | $\boldsymbol{\beta}_1$ | -0.000 | -0.000 | -0.000 | -0.000 | | | |
| white_games | β_2 | 0.000 | 0.000 | 0.000 | 0.000 | | | |
| rating_diff | β_3 | 0.001 | 0.001 | 0.001 | 0.000 | | | |
| game_diff | β_4 | 0.000 | 0.000 | 0.000 | 0.000 | | | |
| inacc_diff | ρ_5 | 0.002 | -0.006 | 0.090 | 0.000 | | | |
| mistake_diff | β_6 | 0.001 | -0.009 | 0.184 | 0.000 | | | |
| blunder_diff | ρ_7 | 0.003 | 0.003 | 0.297 | 0.001 | | | |
| acpl_diff | β_8 | 0.104 | 0.089 | 0.108 | 0.026 | | | |
| same_region_yes | β_9 | 0.000 | 0.000 | 0.082 | 0.000 | | | |
| blitz | β_{10} | 0.000 | -0.056 | 0.000 | 0.000 | | | |
| rapid | β_{11} | -0.000 | -0.007 | 0.030 | -0.000 | | | |
| Metrics | Mean | Lo | Hi | | | | | |
| Error (%) | 7.989 | 7.401 | 8.519 | | | | | |
| Efron's R^2 | 0.739 | 0.723 | 0.758 | | | | | |

Mean Centering

Mean centering helps to scale our data. We want 0 values to be meaningful

```
white rating centered
Unit Difference: -0.0198
white_games_centered
Unit Difference: -0.0001
rating_diff_centered
Unit Difference: -0.0
game_diff_centered
Unit Difference: -0.0003
inacc_diff_centered
Unit Difference: -0.0
mistake_diff_centered
Unit Difference: -0.0182
blunder_diff_centered
Unit Difference: -0.0055
acpl_diff_centered
Unit Difference: -0.0397
same_region_yes
Unit Difference: 0.0242
blitz
Unit Difference: 0.0176
rapid
Unit Difference: 0.0043
```

Mean-Centered Model (3 sd)

| | | | 95% BCI | | |
|------------------------|--------------------|-------|---------|-------|--------|
| Coefficients | | Mean | Lo | Hi | P(y=1) |
| | $oldsymbol{eta}_0$ | 0.080 | 0.000 | 0.121 | 0.520 |
| white_rating_centered | β_1 | 0.000 | 0.000 | 0.001 | 0.000 |
| white_games_centered | β_2 | 0.000 | -0.000 | 0.000 | 0.000 |
| rating_diff_centered | β_3 | 0.001 | 0.001 | 0.002 | 0.000 |
| game_diff_centered | β_4 | 0.000 | 0.000 | 0.000 | 0.000 |
| inacc_diff_centered | ρ_5 | 0.073 | 0.002 | 0.091 | 0.018 |
| mistake_diff_centered | $oldsymbol{eta_6}$ | 0.022 | -0.017 | 0.111 | 0.005 |
| blunder_diff_centered | β_7 | 0.160 | 0.003 | 0.276 | 0.040 |
| acpl_diff_centered | β_8 | 0.097 | 0.092 | 0.109 | 0.024 |
| same_region_yes | β_9 | 0.071 | 0.000 | 0.106 | 0.018 |
| blitz | β_{10} | 0.017 | -0.019 | 0.045 | 0.004 |
| rapid | β_{11} | 0.032 | -0.000 | 0.056 | 0.008 |
| Metrics | Mean | Lo | Hi | | |
| Error (%) | 7.954 | 7.349 | 8.482 | | |
| Efron's R ² | 0.740 | 0.721 | 0.757 | | |

Unit Change for the initial model

As we know that a unit change may necessarily be different per variable, we change the per unit change for the variables to get a more accurate picture.

white_rating_centered100 Unit Difference: -0.0265 white games centered1000 Unit Difference: -0.0091 rating diff centered100 Unit Difference: -0.003 game diff centered1000 Unit Difference: -0.0291 inacc diff centered Unit Difference: -0.0073 mistake diff centered Unit Difference: -0.0135 blunder diff centered Unit Difference: -0.0222 acpl diff centered10 Unit Difference: -0.0561 same region yes Unit Difference: 0.2312 blitz Unit Difference: 0.062 rapid Unit Difference: -0.0375

| | | | 95% BCI | | |
|------------------------|--------------|-------|---------|-------|--------|
| Coefficients | | Mean | 55% BCI | Hi | P(y=1) |
| Coefficients | β_0 | 0.080 | 0.000 | 0.121 | 0.520 |
| | | | | | |
| white_rating_centered | β_1 | 0.000 | 0.000 | 0.001 | 0.000 |
| white_games_centered | β_2 | 0.000 | -0.000 | 0.000 | 0.000 |
| rating_diff_centered | β_3 | 0.001 | 0.001 | 0.002 | 0.000 |
| game_diff_centered | β_4 | 0.000 | 0.000 | 0.000 | 0.000 |
| inacc_diff_centered | β_5 | 0.073 | 0.002 | 0.091 | 0.018 |
| mistake_diff_centered | β_6 | 0.022 | -0.017 | 0.111 | 0.005 |
| blunder_diff_centered | β_7 | 0.160 | 0.003 | 0.276 | 0.040 |
| acpl_diff_centered | β_8 | 0.097 | 0.092 | 0.109 | 0.024 |
| same_region_yes | β_9 | 0.071 | 0.000 | 0.106 | 0.018 |
| blitz | β_{10} | 0.017 | -0.019 | 0.045 | 0.004 |
| rapid | β_{11} | 0.032 | -0.000 | 0.056 | 0.008 |
| •••• | | | , | | |
| Metrics | Mean | Lo | Hi | | |
| Error (%) | 7.954 | 7.349 | 8.482 | | |
| Efron's R ² | 0.740 | 0.721 | 0.757 | | |

Something fishy...

| | | | 95% BCI | | |
|-----------------------|------------------------|-------|---------|-------|--------|
| Coefficients | | Mean | Lo | Hi | P(y=1) |
| | $ ot\!\!\!/ \rho_0$ | 0.129 | 0.054 | 0.206 | 0.532 |
| inacc_diff_centered | $\boldsymbol{\beta}_1$ | 0.044 | 0.014 | 0.071 | 0.011 |
| mistake_diff_centered | β_2 | 0.078 | 0.026 | 0.136 | 0.020 |
| blunder_diff_centered | ρ_3 | 0.210 | 0.116 | 0.297 | 0.053 |
| acpl_diff_centered10 | β_4 | 0.913 | 0.854 | 0.960 | 0.228 |
| Metrics | Mean | Lo | Hi | | |
| Wetrics | Weari | LO | п | | |
| Error (%) | 7.954 | 7.401 | 8.566 | | |
| Efron's ${\it R}^2$ | 0.737 | 0.715 | 0.755 | | |
| | | | | | |

I knew it...

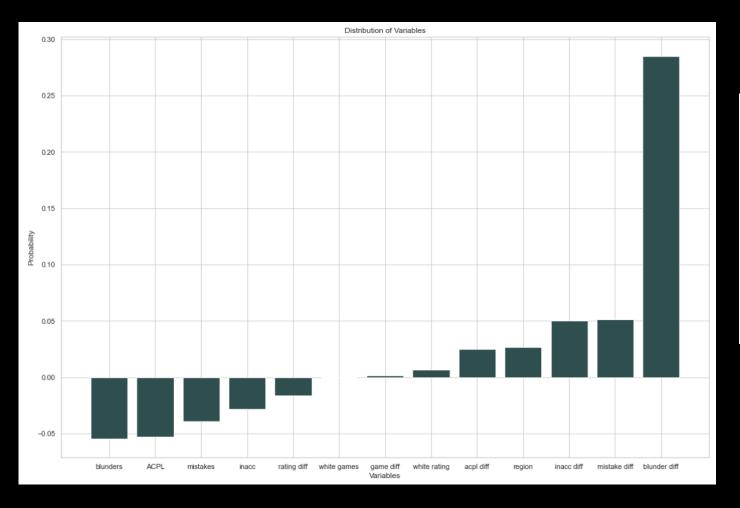
There was something off about the model. It seemed that the probability was being predicted solely by these four variables.

Now we know if we can predict the future and know exactly the moves white would make, we could predict his win...

Obviously, this isn't helpful for our model answering the problem...

Backtracking...

Its time to look at each of the variables



| blunder_diff_centered | 0.285229 |
|-----------------------------|-----------|
| inacc_diff | 0.051539 |
| mistake_diff_centered | 0.050369 |
| same_region_yes | 0.026748 |
| acpl_diff_centered | 0.025284 |
| white_rating_centered100 | 0.006442 |
| game_diff_centered1000 | 0.001465 |
| white_games_centered1000 | -0.000677 |
| rating_diff_centered100 | -0.016399 |
| white_inaccuracies_centered | -0.028104 |
| white_mistakes_centered | -0.038923 |
| white_acpl_centered10 | -0.052568 |
| white_blunder_centered | -0.054338 |

Our bad model

| | | | 95% BCI | | |
|--------------------------|------------------------|--------|---------|-------|--------|
| Coefficients | | Mean | Lo | Hi | P(y=1) |
| | $ ho_0$ | 0.031 | -0.046 | 0.097 | 0.508 |
| game_diff_centered1000 | $\boldsymbol{\beta}_1$ | 0.010 | 0.005 | 0.016 | 0.003 |
| white_rating_centered100 | β_2 | 0.017 | 0.003 | 0.033 | 0.004 |
| blunder_diff_centered | $\boldsymbol{\beta}_3$ | 1.143 | 1.089 | 1.194 | 0.286 |
| same_region_yes | β_4 | 0.117 | 0.033 | 0.211 | 0.029 |
| Metrics | Mean | Lo | Hi | | |
| Error (%) | 21.373 | 20.510 | 22.325 | | |
| Efron's R^2 | 0.385 | 0.366 | 0.408 | | |

game_diff_centered1000
Unit Difference: -0.0078
white_rating_centered100
Unit Difference: -0.0026
blunder_diff_centered
Unit Difference: -0.0043
same_region_yes

Unit Difference: 0.2776

Validation

Validation Metrics:

Accuracy

Error Rate

Accuracy 95% CI: [0.53635766 0.6005622]

Mean: 0.5662390267511943

Null Mean: 0.5136945341466331

Accuracy 95% CI: [0.3994378 0.46364234]

Error Rate: 0.43376097324880575 Null Error: 0.48630546585336687

Compared to our null model, our model performed slightly better.

Future Additions

- Different type of model
- Additional Variables/More robust data to train on
- More time to make more modified API calls to get better data