



**SMIT** SIKKIM  
MANIPAL  
UNIVERSITY  
SIKKIM MANIPAL INSTITUTE OF TECHNOLOGY

# **Engineering Mathematics III**

# **Discrete Mathematics**

## **Lecture 20**

### **Free and Bound Variables**

This course is taught to Computer Science Engineering students in SMIT, India during Jun-Dec, 2019.

for (i in Range(n)):  
    Bound variable to some thing. } → Scope

Print (i)

— ( )

—

this

def

isEven(x)

if (x % 2 == 0):

Return Even

else:

Return odd.

Free variable — Bound variable.

$\exists x$  such that  $x \in A$

$x$ -variable

Scope of  $x$  is the quantifier " $\exists$ "

$\rightarrow$  if  $(x=2)$  print 1234.

$\forall x, x$  is a student

Scope of  $x$  is  
the quantifier " $\forall$ "

for ( $i$  in some) {

}

if (x = 2):

for (i in range(10)):

print i+x

elif (x = 1):

for (i in range(10)):

print i<sup>2</sup>

$\exists x$  such that

$x = 2 \wedge \forall i \in \{1, 2, \dots, 10\}$

$i+x$  is available

Free variable  
under the  
scope of  $x$ .

$\exists$

$\forall$

$\downarrow$

Bound variable within  
the scope of  $\exists$

$\lambda M(x)$

$M(n) : x \text{ is a writer}$

$\downarrow$   
scope of  $x$  is  $M(n)$ .

$\exists x, M(x) \wedge N(n)$

scope of the quantifier  $\exists = M(x) \wedge N(n)$

$M(n) \wedge (\exists x, N(n))$

scope of  $n$  is  $M(n)$   $\rightarrow$  scope of  $\exists = N(n)$   
scope of  $x = N(n)$