

```
# MLR Model
```

```
# Install the required packages
```

```
install.packages("UsingR")
```

```
library(UsingR)
```

```
install.packages("lmtest")
```

```
library(lmtest)
```

```
install.packages("datarium")
```

```
library(datarium)
```

```
marketing
```

```
head(marketing)
```

```
names(marketing)
```

```
model_1=lm(sales~youtube+facebook+newspaper,data=marketing)
```

```
model_1
```

```
summary(model_1)
```

```
# Test for significance of regression using ANOVA
```

```
f=summary(model_1)$fstatistic
```

```
f
```

```
f_table=qf(.95, df1=f[2], df2=f[3])
```

```
f_table
```

```
if(f[1]>f_table)print("reject the null hypothesis that the co-efficient of the predictors is zero") else print("accept the null hypothesis")
```

```
# Test of Individual regression coefficient (beta1)
```

```
teststat=coef(summary(model_1))[2,1]/coef(summary(model_1))[2,2]
```

```
teststat
```

```
n=nrow(marketing)
```

```
n
```

```
alpha=0.05
```

```
# p values of coefficients
```

```
Prob_values=coef(summary(model_1))[, "Pr(>|t|)"]
```

```
Prob_values
```

```
p_value=2*pt(abs(teststat),n-4,lower.tail=F)
```

```
p_value
```

```
if(p_value<0.05) print("reject the null hypothesis that the coefficient of the predictor is zero")
```

```
else print("accept the null hypothesis")
```

```
# t-test
```

```
t_table=qt((alpha/2),n-4,lower.tail = F)
```

```
t_table
```

```
if(teststat>t_table) print("reject the null hypothesis that the coefficient of the predictor is zero")
```

```
else print("accept the null hypothesis")
```

```
# Test for intercept (beta0)
```

```
teststat1=coef(summary(model_1))[1,1]/coef(summary(model_1))[1,2]
```

```
teststat1
```

```
# p values of coefficients
```

```
Prob_values=coef(summary(model_1))[, "Pr(>|t|)"]
```

```
Prob_values
```

```
p_value=2*pt(abs(teststat1),n-4,lower.tail=F)
```

```
p_value
```

```
if(p_value<0.05) print("reject the null hypothesis that the intercept is zero") else
```

```
  print("accept the null hypothesis")
```

```
# t-test
```

```
t_table=qt((alpha/2),n-4,lower.tail = F)
```

```
t_table
```

```
if(teststat1>t_table) print("reject the null hypothesis that the intercept is zero") else
```

```
  print("accept the null hypothesis")
```

```
# Extract Model Components
```

```
obs_val=marketing$sales
```

```
obs_val
```

```
fitted_val=fitted(model_1)
```

```
fitted_val
```

```
residuals=resid(model_1)
```

```
residuals
```

```
# Residual Analysis
```

```
# Residuals vs Fitted Plot
```

```
plot(fitted_val,residuals,
```

```
    xlab = "Fitted Values",
    ylab = "Residuals",
    main = "Residuals vs Fitted Values")
abline(h=0,lty=2,col="red")

# Random scatter around zero → model is appropriate
# Funnel shape → heteroscedasticity
# Curved pattern → non linearity


# Breusch-Pagan Test(Homoscedasticity)
bp_test=bptest(model_1)
bp_test
# Decision
#  $p > 0.05$  → homoscedasticity satisfied


# Normal Q-Q Plot
qqnorm(residuals)
qqline(residuals, col = "red")


# Shapiro-Wilk Normality Test
shapiro_test=shapiro.test(residuals)
shapiro_test
# Decision rule
#  $p > 0.05$  → residuals are approximately normal
# Since p-value ( $3.939e-09$ )  $< 0.05$ , we reject  $H_0$ 
# Statistical inference may be compromised (p-values, confidence intervals)


# Durbin-Watson Test(Independence of Residuals)
```

```
dw_test=dwtest(model_1)
```

```
dw_test
```

```
# Conclusion
```

```
# The Durbin-Watson statistic will always have a value ranging between 0 and 4.
```

```
# A value of 2.0 indicates there is no autocorrelation detected in the sample.
```

```
# Values from 0 to less than 2 point to positive autocorrelation.
```

```
# Values from 2 to 4 mean negative autocorrelation.
```

```
# Cook's Distance (Influential Observations)
```

```
# Influential points can distort regression coefficients
```

```
# They may Inflate or deflate slope estimates
```

```
# Affect hypothesis tests
```

```
# Reduce forecast accuracy
```

```
plot(cooks.distance(model_1),
```

```
type = "h",
```

```
main = "Cook's Distance")
```

```
abline(h = 4/length(residuals), lty = 2, col = "red")
```

```
# In a Cook's Distance plot:
```

```
# Each vertical line represents one observation
```

```
# A horizontal reference line is drawn at  $4 / n$ 
```

```
# Points above the line deserve further investigation
```

```
# Decision
```

```
#  $D_i < 1$           Observation is not influential
```

```
#  $D_i \geq 1$           Observation is highly influential
```

```
#  $D_i > 4/n$  Potentially influential (commonly used rule)
```

```
new_values=data.frame(youtube=122.34,facebook=59.59,newspaper=29.18)
```

```
new_values
```

```
pred_y=predict(model_1,new_values,interval="predict")
```

```
pred_y
```

```
conf_y=predict(model_1,new_values,interval="confidence")
```

```
conf_y
```

```
#####  
#####
```

```
# The condition number is the maximum condition index.
```

```
# Multicollinearity is present when the VIF is higher than 5 to 10 or
```

```
# the condition indices are higher than 10 to 30.
```

```
#Check for Multicollinearity in R
```

```
#Using Correlation Matrix
```

```
install.packages("corrplot")
```

```
library("corrplot")
```

```
corrplot(cor(marketing),method="number")
```

```
#Using VIFs
```

```
install.packages("olsrr")
```

```
library("olsrr")
```

```
ols_vif_tol(model_1)
```

```
# Using Eigenvalues and Condition Index
```

```
ols_eigen_cindex(model_1)
```