Reg.No	
Name	

[10]



Final Assessment Test - April 2022

Programme	e: Integrated M.Tech.	Semester : Win 2021-22	
Course	: Applications of Differential and Difference	Code : MAT2002	
	Equations	Slot : B2+TB2	
Faculty	: Dr. Dhanasekar, Dr. V. Parthiban, Dr. Manivannan, Dr. David Raj Micheal,	Class Nbr : CH2021222300226, 227,228, 229	
Time	: 180 Minutes	Max.Marks: 120	\Box

Part – A $(5 \times 10 = 50)$ Answer all the Questions

1. Find the Fourier series expansion of
$$f(x) = \begin{cases} 0 & 0 \le x \le \pi \\ \cos x & \pi \le x \le 2\pi \end{cases}$$
. [10]

2. Determine the first two harmonics of the Fourier series for the following data:

3. Find
$$P$$
 such that $P^{-1}AP = D$, where D is a diagonal matrix for $A = \begin{bmatrix} -1 & 1 & 0 \\ 0 & 2 & -1 \\ 0 & 0 & 3 \end{bmatrix}$. [10]

4. (a) Let
$$A = \begin{bmatrix} 3 & 3 & 0 \\ 0 & 2 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$
 and $x^3 - 6x^2 + 11x - 6 = 0$ be the characteristic equation of A . [5] Find A^{-1} using Cayley-Hamilton theorem.

(b) i. Subpart 01 [3]

ii. Subpart 02 [2]

5. Solve $y'' - 2y' = e^x \sin x + 5$ using the method of undetermined coefficients. [10]

$Part - B (5 \times 10 = 50)$

Answer any FIVE Questions

6. Solve
$$(3x+2)^2y'' + 3(3x+2)y' - 36y = 3x^2 + 4x + 1$$
. [10]

7. A particle is moving along a plane curve, the co-ordinate (x, y) at time t is given by,

$$\frac{dy}{dt} + x - 2y = \cos 2t$$
$$\frac{dx}{dt} + 2x - y = \sin 2t$$

[10]

[5]

[10]

for t > 0. If at t = 0, x = 1 and y = 0, use Laplace transform to find the curve (x(t), y(t)) on which the particle is moving.

8. Find the power series solution about x = 0 of the following differential equation equation [10]

$$(x^2 + 2x - 1)y'' + 3y' = 0.$$

9. (a) Find the Eigen functions of the Strum-Liouville problem

$$y'' + \lambda y = 0$$
, $y(0) = 0$, $y(\pi) = 0$

and verify their orthogonality.

- (b) Use Convolution theorem to find the inverse Z-transform of $\left(\frac{z}{z-a}\right)^2$ and hence deduce [5] for $\left(\frac{2z}{2z-1}\right)^2$.
- 10. Find the Z-transform of the following:

(a)
$$2n + 4\sin\frac{n\pi}{2} - 4a^4$$

(b)
$$e^{-2n}\cos n\theta$$
 [3]

(c)
$$\frac{n}{(n+2)!}$$

11. Solve the recurrence relation [10]

$$a_n = 4a_{n-1} - 4a_{n-2} + (n+1)2^n$$

given that $a_0 = 1$ and $a_1 = 2$.

12. Use Z-transform to solve the difference equation

$$u_{n+2} - 4u_{n+1} + 3u_n = 5^n.$$

Programme : Integrated M.Tech.

Exam Date & Time : 30/08/2022 9.00 AM to 10.30 AM

Room Number : DB-108

Course Code : MAT2002

Course Name : Applications of Differential and Difference Equations

Class Id & Slot : CH2021222300226 & B2+TB2

Total QP Alloted : 9+2

Faculty & Emp. Id: Dr. David Raj Micheal (51942)

Faculty Mobile No : +91 99999 00000

Programme : Integrated M.Tech.

Exam Date & Time: 30/08/2022 9.00 AM to 10.30 AM

Room Number : DB-203

Course Code : MAT2002

Course Name : Applications of Differential and Difference Equations

Class Id & Slot : CH2021222300226 & B2+TB2

Total QP Alloted : 36+2

Faculty & Emp. Id: Dr. David Raj Micheal (51942)

Faculty Mobile No : +91 99999 00000

Programme : Integrated M.Tech.

Exam Date & Time: 30/08/2022 9.00 AM to 10.30 AM

Room Number : DB-204

Course Code : MAT2002

Course Name : Applications of Differential and Difference Equations

Class Id & Slot : CH2021222300226 & B2+TB2

Total QP Alloted : 25+2

Faculty & Emp. Id: Dr. David Raj Micheal (51942)

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