

- Compile with gcc -o -lm

1. Program design

- 1) M bits of bloom filter & U updates are predefined
- 2) Program will calculate the suppose minimum number of hash function from $h = (\log_2)m/u$
- 3) Program will test the bloom filter with different number of hash function ranging from $h - 4$ to $h + 4$
- 4) In each test program will calculate the probability of false positive both from random generating data & $P(h) = (1 - (1 - 1/m)^{uh})^h$

```
// number of time to test false positive
#define TEST 100000
// number of bits in bloom filter
#define M 10001
// number of initial updates
#define U 1000
// number of hash functions
int H;

int main()
{
    // calculate minimum h in from theory
    double tH = log(2) * (double)M / (double)U;
    // test bloom filter with tH - 4 ~ tH + 4 hash functions
    for (H = start; H <= finish; H++)
    {
        // generate random integer insert into bloom filter
        for (int i = 0; i < U; i++)
            generate random data & addData();

        // generate random integer to test collision
        int falsePositive = 0;
        for (int i = 0; i < TEST; i++)
            if (collision)
                falsePositive++;

        // calculate P from theory & test
        p = (double>falsePositive / TEST * 100;
```

```

        tP = pow(t, U) * pow(1 - pow(t, U * H), H) * 100;
        print theory p & test p;
    }
    return 0;
}

// generate hash function using hash1 & hash2
unsigned int hash(int i, unsigned int key, int size)
{
    return (hash1(key, size) + hash2(key, size) * i) % size;
}

```

2. Sample output

m = 10001 u = 2000 h = 1 ~ 7 test 100000 times

theory min h = 3.466

h = 1

theory false positive rate : 14.841%

test false positive rate : 18.080%

h = 2

theory false positive rate : 8.898%

test false positive rate : 11.137%

h = 3

theory false positive rate : 7.519%

test false positive rate : 9.078%

h = 4

theory false positive rate : 7.528%

test false positive rate : 9.634%

h = 5

theory false positive rate : 8.262%

test false positive rate : 10.252%

h = 6

theory false positive rate : 9.533%

test false positive rate : 11.047%

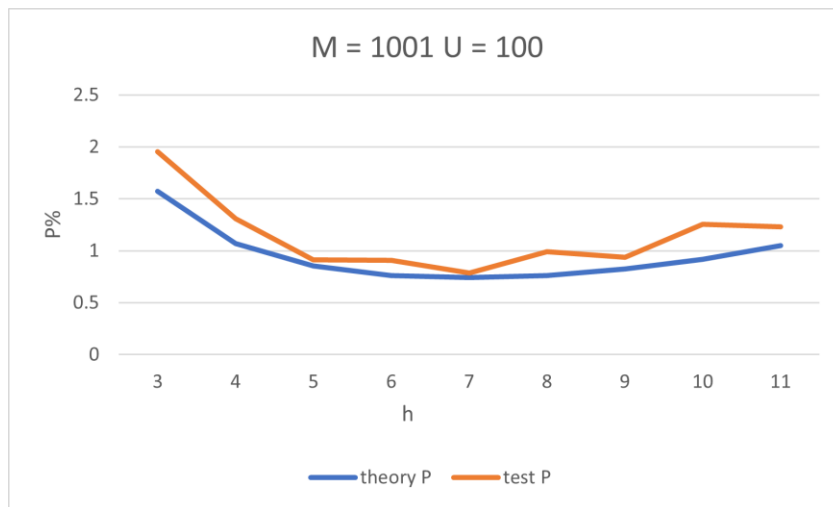
h = 7

theory false positive rate : 11.279%

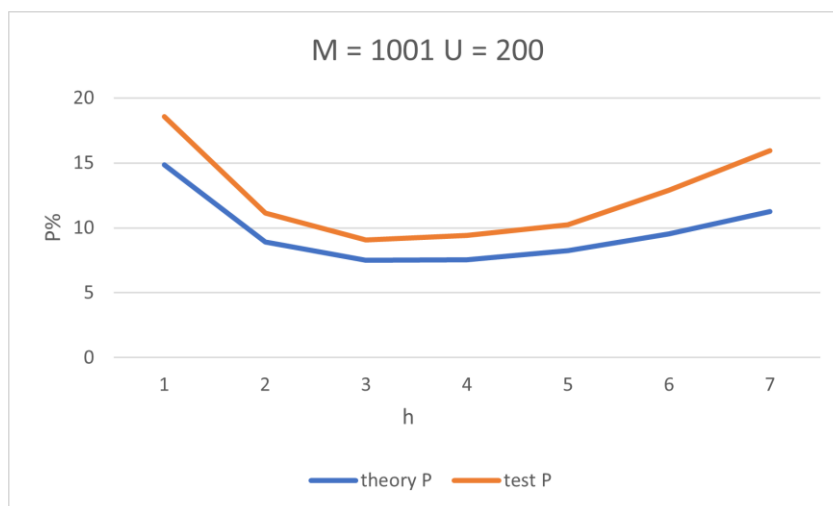
test false positive rate : 14.232%

3. Analysis

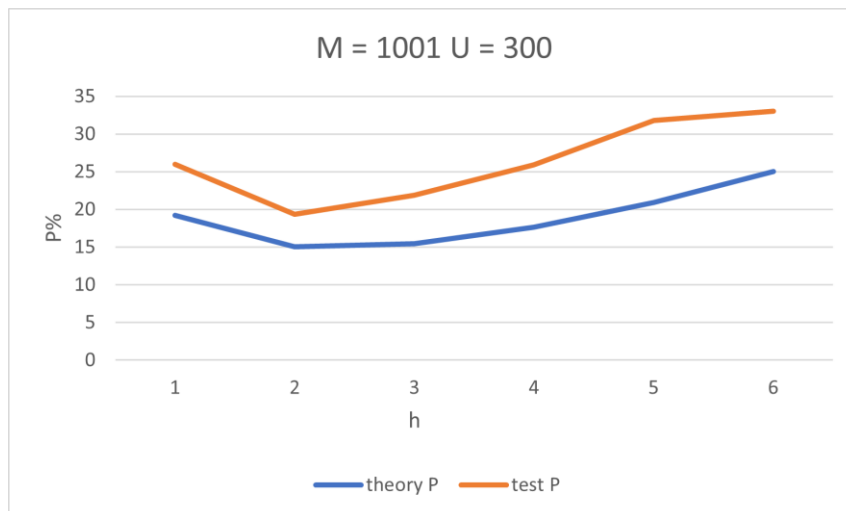
Theory min $h = 6.938$

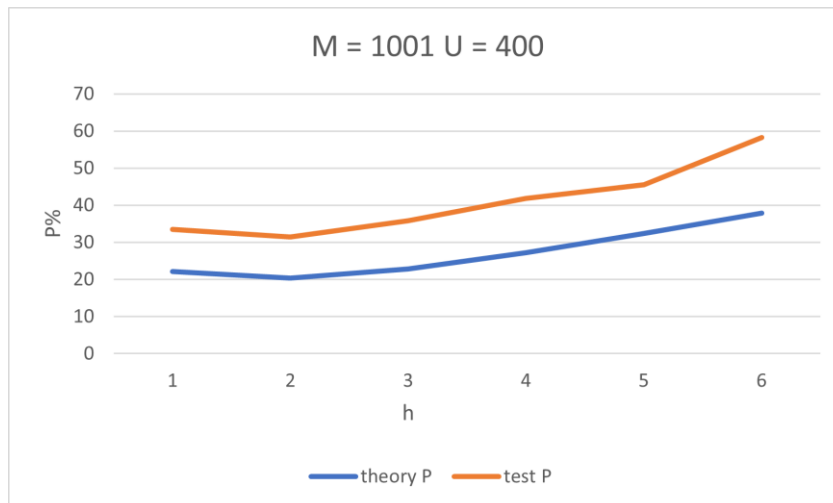


Theory min $h = 3.469$

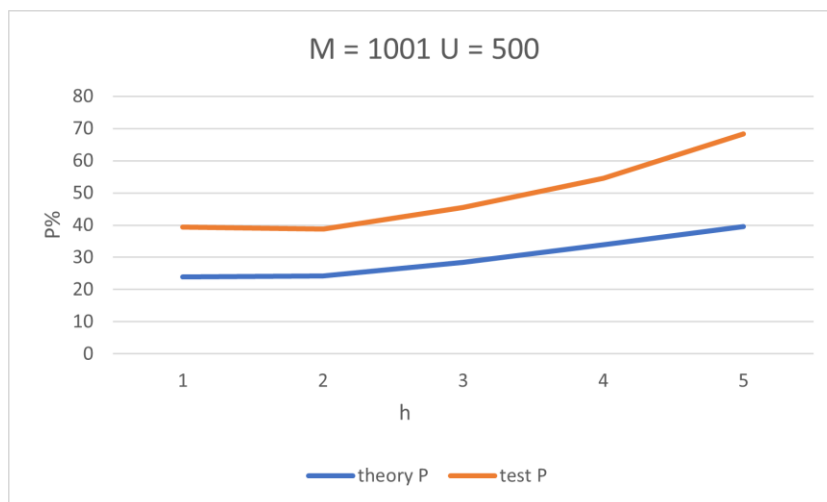


Theory min $h = 2.313$





Theory min $h = 1.735$



Theory min $h = 1.388$

Observe:

- 1) Test P seems to form local minimum at $h = \text{theory min } h$
- 2) Test P curve looks like the theory P curve with a slight shift up the y-axis

Conclusion:

- 1) $P(u)$ exist at $h = (\log_2)m/u$
- 2) the distance between two curve probably cause by ununiform distribution of the hash function