Improving Astronomy Image Quality Through Real-time Wavefront Estimation

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Abstract

We present a new framework for detecting telescope optics aberrations in real-time. The framework divides the problem into two subproblems that are highly amenable to machine learning and optimization. The first involves making local wavefront estimates with a convolutional neural network. The second involves interpolating the optics wavefront from all the local estimates by minimizing a convex loss function. We test our framework with simulations of the Vera Rubin Observatory. In a realistic mini-survey, the algorithm reduces the total magnitude of the optics wavefront by 66%, the optics PSF FWHM by 27%, and increases the Strehl ratio by a factor of 6. The resulting sharper images have the potential to boost the scientific payload for astrophysics and cosmology.

1. Introduction

The signal to noise ratio of most astronomical analyses critically depends on image quality. To maintain optimal image quality during operation, wide-field telescopes deploy active optics systems, which sense aberrations in the optics and correct them in realtime. The primary challenge for these systems is distinguishing the correctable aberrations due to the optics from the dominant and incorrectable aberrations due to atmospheric turbulence. Here we present a new machine learning framework that is capable of extracting the optics aberrations and improving image quality.

While the immediate application is improving image quality in present and future ground-based telescopes, there are also emerging use cases in space. The simultaneous demands for higher quality images and lighter payloads from space telescopes make large foldable mirrors attractive. These large, lightweight mirrors are more susceptible to environmental disturbances and would benefit from active optics control. Prototypes are already being explored [18, 17, 7, 33, 31, 28]. In this work we demonstrate that our method is capable of improving image quality in the challenging ground-based environment. We suspect its performance will improve in the space environment where at-

mospheric turbulence is absent.

The upcoming ground-based Vera Rubin Observatory (Rubin) has a 3.5 degree field of view and high dimensional optical model that make it the ideal stress test for our framework [12, 1]. The large scientific community behind the Rubin Observatory has developed a mature suite of simulation codes [25, 21, 6] which we used to train and test our model in realistic scenarios. The unlimited supply of virtual telescopes and observations allowed us to assess our method in a more comprehensive range of conditions than would be possible with a real instrument.

The input to our model comes from 4 curvature wavefront sensors in the corner of the Rubin focal plane, shown in Figure 1. Each of these sensors is split into two halfchips which are purposefully offset out of focus. The stars that fall on these sensors produce large ring-like "donut" images. The goal of our algorithm is to constrain optics aberrations attributed to the entrance pupil from the intensity patterns in all the donut images throughout the observation, which can number into the thousands. One of the key challenges is interpolating the optics wavefront across the entire focal plane from donut images in four concentrated regions which collectively cover less than 2% of the total focal plane.

The key breakthrough in our work is the realization that the wavefront sensing problem can be divided into two subproblems that are highly amenable to machine learning and optimization. The first problem is to estimate the local wavefronts, characterized by 18 Zernike coefficients, from individual donut images. The second problem is to interpolate the global optics wavefront, characterized by 56 double Zernike coefficients, from all the local estimates by minimizing a simple convex loss function. The main contributions of this work are:

- We present a new mathematical framework for extracting the optics wavefront across the field of view.
- We demonstrate that a convolutional neural network can make reasonable estimates of the local wavefront from donut images.

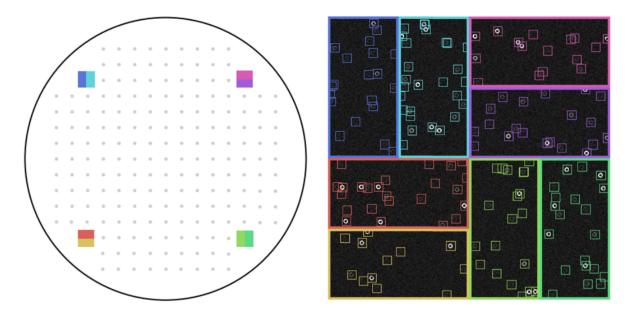


Figure 1. **The Rubin Observatory focal plane and wavefront sensor images.** *Left:* the Rubin Observatory focal plane. The eight solid boxes show the positions of the eight wavefront sensor half-chips and the gray dots show the centers of the remaining 189 science sensors. *Right:* example wavefront sensor images from each of the eight half-chips. The boundary color matches with the region they correspond to on the focal plane. The colored boxes show the donuts on each half-chip.

- 3) We show that fitting the global wavefront from a multitude of local wavefront estimates can suppress the atmospheric contribution.
- 4) We run our framework on a realistic mini-survey where it reduces the total magnitude of the optics wavefront by 66%, the optics PSF FWHM by 27%, and increases the Strehl by a factor of 6.

Finally, we emphasize that while this work focuses on the context of the Rubin Observatory, our framework extends to all wide-field telescopes with curvature wavefront sensors, and potentially to future space telescopes.

2. Related Work

The potential for neural networks to learn the non-linear mapping between intensity patterns and aberrations in the pupil plane was first recognized in 1990 [4]. Shortly afterwards this potential was realized as neural networks were deployed to detect turbulence induced distortion on the Multiple Mirror Telescope [27] and to detect aberrations in the primary mirror of the Hubble Space Telescope [5]. Others expanded this concept to predict more wavefront components [13], incorporate temporal history [20, 22], compare reconstruction methods [9], and better characterize atmospheric turbulence [32].

In the past decade, convolutional neural networks (CNN) [19] have re-emerged and spurred dramatic advances in computer vision [15, 29, 26, 11]. This has opened up new

possibilities for wavefront sensing in astronomy. CNNs can complement conventional iterative estimation approaches by providing good starting estimates [24]. They can even solve the full estimation problem in various scenarios [23, 10, 30]. Combining these networks with CMOS sensors opens up the possibility that guide stars could be used for adaptive optics on 2-4m class telescopes [3]. They also have the potential to sense and correct low-order wavefront aberrations for high-contrast astronomical imaging [2].

Most previous work focuses on sensing the dominant source of wavefront error, atmospheric turbulence or simple distortions, on short timescales, typically 10s of milliseconds. In this work, we study the harder problem of sensing subdominant sources of wavefront error, small alignment and mirror surface perturbations, from images integrated over an entire 15 second exposure. This presents new challenges such as how to best aggregate intensity information from throughout the field of view to suppress the dominant and spatially correlated atmospheric turbulence contribution.

3. Wavefront Estimation Framework

The optics wavefront $W_{\rm opt}$ is a function of two separate planes: the pupil plane parameterized by (u,v) and the focal plane parameterized by (x,y). We use the double Zernike polynomial basis [16] to represent the optics

wavefront,

$$W_{\text{opt}}(u, v, x, y) = \sum_{i=1}^{k} \sum_{j=1}^{m} \beta_{ij} Z_i(u, v) Z_j(x, y)$$
 (1)

where β_{ij} are the coefficients, Z_i are annular Zernike polynomials over the pupil, and Z_j are circular Zernike polynomials over the focal plane. The goal of wavefront sensing is to estimate these coefficients β_{ij} from the n donut images D_i positioned across the wavefront sensors (see Figure 1). Let the position of donut i be x_i, y_i and the defocus offset of the corresponding sensor be z_i . The wavefront sensing problem is to find f such that

$$\beta = f((D_1, x_1, y_1, z_1), \dots, (D_n, x_n, y_n, z_n))$$
 (2)

We break this into two subproblems.

3.1. Estimating Local Wavefronts

In the first subproblem, we estimate the total local wavefront $w_{\rm tot}(u,v)$ from donut D_i at position x_i,y_i,z_i . The intensity in the donut image is related to the total local wavefront by the Fraunhoffer diffraction integral,

$$D \propto |\mathcal{F}\left\{P(u, v) \exp(2\pi i w_{\text{tot}}(u, v)/\lambda)\right\}|^2 \tag{3}$$

where \mathcal{F} is the Fourier transform, P(u, v) is the pupil mask, and λ is the wavelength. We represent the local wavefront in a basis of annular Zernike polynomials over the pupil, such that the total local wavefront for donut i at position x_i, y_i is

$$w_{\text{tot}}(u, v) = \sum_{j} \alpha_{ij} Z_j(u, v) \tag{4}$$

Convolutional neural networks (CNNs) are particularly well suited for processing images and learning nonlinear mappings. We develop a CNN φ to solve the inverse problem of estimating α_i from (D_i, x_i, y_i, z_i) . In Section 4 we describe the implementation of this model in detail.

3.2. Interpolating the Optics Wavefront

In the second subproblem, we aggregate the local estimates from the first subproblem to constrain β . The total local wavefront at position x_i, y_i is related to the optics wavefront via

$$w_{\text{tot}}(u, v) = W_{\text{opt}}(u, v | x_i, y_i) + \epsilon(u, v | x_i, y_i)$$
 (5)

where ϵ represents the atmospheric turbulence contribution to the wavefront. Let \mathcal{Z} be defined such that $\mathcal{Z}_{ij} = Z_j(x_i, y_i)$. Then for $i = 1, \ldots, m$ we have

$$\alpha e_i = \mathcal{Z}\beta e_i + \epsilon \tag{6}$$

where e_i is the *i*th unit vector. Then combining the α from the previous subproblem, and computing the corresponding \mathcal{Z} , allows us to solve for β ,

$$\beta = \operatorname{argmin}_{\beta} \left\{ \sum_{i=1}^{m} \ell(\alpha e_i, \mathcal{Z}\beta e_i) \right\}$$
 (7)

where ℓ is a convex loss function. The full psuedocode is given in Algorithm 1.

Algorithm 1: estimates the optics wavefront from donuts images.

The dominant source of error is the atmospheric turbulence contribution to the wavefront. This error is correlated on scales of arcminutes. By processing donuts with reasonable separation and between different wavefront sensors we are able to suppress this error by roughly a factor of $1/\sqrt{n}$.

There are two parameters of our algorithm that must be set based on the telescope: the number of Zernike coefficients to use for the pupil m, and the number of Zernike coefficients to use for the focal plane k. For the Rubin Observatory we use Zernikes Z_4 through Z_{21} for the pupil plane. The first three coefficients do not impact image quality, so we exclude them. We use Z_1 through Z_3 for the focal plane. Our simulations show that 90% of the optics wavefront is contained in this truncated basis.

There are two benefits to dividing the wavefront estimation problem into these two subproblems that are worth highlighting. The first is the useful intermediate data products. The local wavefront coefficients α , which are estimated in the first subproblem, are physically meaningful. Telescope operators can track them during operations and gain further insight into the system. This adds an additional layer of transparency and robustness.

The second benefit is that it makes deep learning approaches feasible. Deep neural networks must be trained on

large datasets to avoid overfitting. The input to the original problem is 4 wavefront sensor images, or up to thousands of donut images. The raytracing necessary to simulate even a single input sample is extremely computationally expensive. In our first subproblem however, the input is only a single donut image. The computation required to simulate a training sample is reduced by three orders of magnitude. This makes it possible to generate simulated datasets that are sufficient for training deep neural networks. In the next section, we highlight the power of these models.

4. Experiments and Analysis

4.1. Datasets

Individual Donuts: comprised of 600,147 simulated 256×256 pixel Rubin Observatory donut images (see Figure 3). Each donut image has a corresponding position and true local wavefront label. This dataset is used to train the neural network to estimate the local wavefront.

The sources are chosen to be as realistic as possible. We started by drawing 5,000 r-band observations from a simulated Rubin Observatory observing schedule [6]. For each of these observations we queried the Gaia DR2 catalog for sources that would fall on the wavefront sensors [8]. Then we sampled 200 stars, with replacement, to simulate from each observation. We simulated an additional 100,147 blends - donut images with multiple stars overlapping - so that the network could learn to handle these complicated cases as well.

The simulations start by drawing photons from a blackbody distribution based on the star temperature and magnitude from the catalog. We then propagate these through the atmosphere with the help of the GalSim Python package [25]. We use frozen phase screens to represent low spatial frequency turbulence and apply a randomly drawn second kick to account for high frequency turbulence. We use the Batoid Python raytracing package to generate Rubin telescope instances and trace the photons into the detector [21]. We randomly perturb 50 different degrees of freedom for each telescope instance in a manner that is consistent with what the telescope is expected to face in operations. These random perturbations are drawn from distributions that represent what we expect the Rubin telescope will face in operations. Finally, we use the GalSim to model the sensor readout. We incorporate custom functions throughout this pipeline to account for additional physical effects such as: chromatic seeing, differential chromatic refraction, charge diffusion in the sensors, bad pixels, and astrometric errors.

The local wavefront labels are calculated with Batoid. For each perturbed telescope instance, a grid of rays are traced from the entrance pupil through the corresponding field position to the exit pupil. Then Zernike polynomials are fit to the optical path differences between the rays.

	Count		MSE	
Sources	Train	Test	Train	Test
Stars	498,071	1,708	4.5 ± 3.2	4.4 ± 3.5
Blends	100,028	340	9.5 ± 20.0	9.6 ± 22.0

Table 1. Train and test results on stars and blends. The mean-squared-error (MSE) is in units of thousandths of waves.

These coefficients are the entries of the labels.

Full Observations: consists of 497 Rubin observations, each containing hundreds to thousands of simulated donuts. This dataset is used for testing the full framework, which ingests all the donuts in a given observation and produces an optics wavefront estimate.

All the donuts in an observation are simulated with the same atmosphere and sky background. The observations are drawn from Rubin Observatory scheduler simulations and the sources correspond to Gaia queries. Each star in the observation is simulated in the manner described above. In addition to the positions and local wavefront labels for each donut, there is also an optics wavefront for the entire observation. We use the batoid package to compute the relevant double Zernike coefficients from each telescope instance.

4.2. Architecture and Training

The input to the neural network is a 256×256 pixel donut image and position r=(x,y,z). The network, shown in Figure 2, has two components: an image component and a position component. The image component reduces the donut image to a 1024 dimensional vector. The position component combines this vector with the position input and estimates the 18 local wavefront coefficients.

The image component is comprised of eight repeated convolution blocks which decrease the tensor height and width and increase the depth, all by a factor of two. The convolution block has a convolution skip connection followed by the downsampling convolution. The position component is comprised of three linear layers which each reduce the dimensionality of the tensor. All convolution and linear layers are followed by ReLU and batchnorm layers, except the final linear layer.

We use the mean-squared-error (MSE) between the estimated and true wavefront coefficient as the loss function. We train the model for 8 epochs over 598,099 training samples with the Adam optimizer [14]. Then we evaluate the model on a held out test set of 2,048 samples. The almost identical MSE on the training and test sets, shown in Table 1, suggests it is not overfitting.

4.3. Local Wavefront Results

Explain figure samps.

Question: is the network memorizing, or learning? Train-test similarity and qualitative test suggests it is actu-

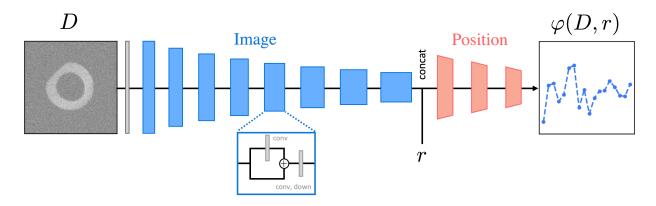


Figure 2. **Network architecture.** The layers of the image component, which reduces the donut image into a 1024 length vector, are in blue and the layers of the position component, which concatenates the position and makes the wavefront estimate, are in red.

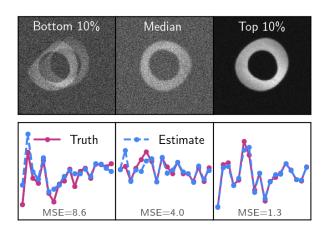


Figure 3. Foo.

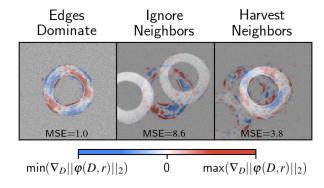


Figure 4. Foo.

ally	learning.

Sources	Loss	$ \mathcal{G}^r _1 < \mathcal{G}^t _1$	$ \mathcal{G}^r _1/ \mathcal{G}^t _1$
5001005		99.6	0.482 ± 0.126
a .	ℓ_1		
Stars	$\mid \ell_2 \mid$	99.8	0.488 ± 0.124
and	$\ell_{ m huber}$	100.0	0.480 ± 0.120
Blends	$\ell_{1, \text{median}}$	97.8	0.670 ± 0.138
	$\ell_{2, ext{median}}$	100.0	0.464 ± 0.121
	ℓ_1	99.8	0.435 ± 0.111
	ℓ_2	100.0	0.430 ± 0.100
Stars	$\ell_{ m huber}$	100.0	0.430 ± 0.103
	$\ell_{1, \text{median}}$	97.2	0.635 ± 0.135
	$\ell_{2, \text{median}}$	99.8	0.414 ± 0.105
	ℓ_1	99.6	0.369 ± 0.127
Brightest	ℓ_2	100.0	0.342 ± 0.120
Stars	$\ell_{ m huber}$	100.0	0.343 ± 0.122
	$\ell_{1, ext{median}}$	97.2	0.599 ± 0.156
	$\ell_{2, ext{median}}$	100.0	0.348 ± 0.121
	ℓ_1	100.0	0.127 ± 0.053
Labels	ℓ_2	100.0	0.060 ± 0.018
	$\ell_{ m huber}$	100.0	0.079 ± 0.037

Table 2. Train and test results on stars and blends. The mean-squared-error (MSE) is in units of thousandths of waves.

State	Position	FWHM	Strehl
Before	Center	0.288 ± 0.034	0.093 ± 0.39
After	Center	0.211 ± 0.005	0.555 ± 0.207
Before	Corner	0.314 ± 0.045	0.074 ± 0.32
After	Corner	0.215 ± 0.009	0.400 ± 0.184

Table 3. Todo.

4.4. Optics Wavefront Results

5. Conclusion

The exceptional simplicity and robustness of our approach make it well suited for space, where robustness and

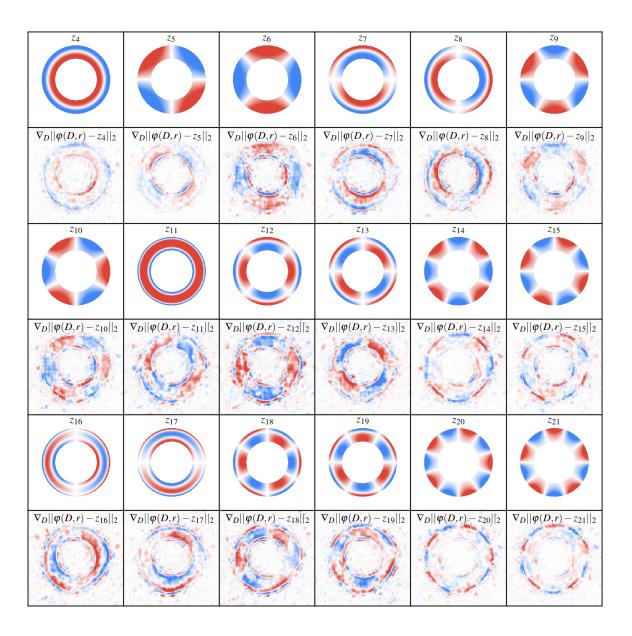


Figure 5. Foo.

reliability are at a premium.

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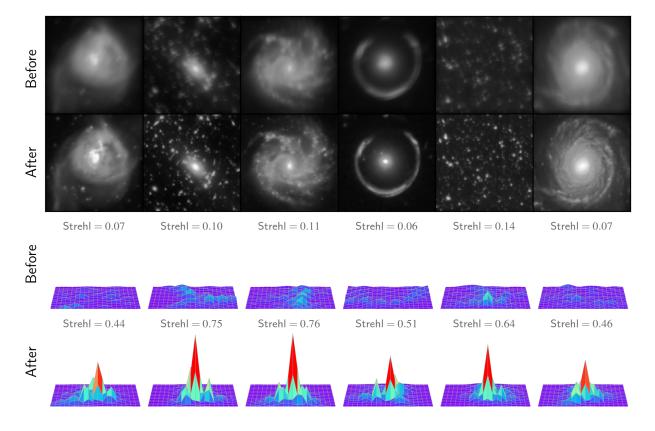


Figure 6. Example of a short caption, which should be centered.

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