

Digital Lab

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Abstract

For this lab, we covered a wide range of topics relevant to digital radio. I don't know what the hell they were yet though.

1 Introduction

The foremost, most fundamental piece of physics relevant to digital signal sampling is the Nyquist criterion. A signal is a continuously-varying quantity, but a computer can only read its value a finite number of times. The Nyquist criterion states that in order to get sample data that approximates the actual shape of the signal, one must sample at at least twice the frequency of the signal.

Another piece of physics often relevant to digital radio is signal mixing. To mix signals, one uses a signal mixer. The mixer takes as input two signals and outputs their product in the time domain. This turns out to be their convolution in the frequency domain by the Convolution Theorem. A mixer can be either Single Side Band (SSB) or Double Side Band (DSB). Digital shit is pretty sweet!!

2 Experiments, Observations, Analysis and Interpretation

2.1 The Nyquist Frequency

The first thing we did in this lab was try to understand and visualize the Nyquist criterion. To do this, we sampled a signal at frequencies ranging from 0.1 times the Nyquist frequency to 3 times the Nyquist frequency and compared how effectively they seemed to illustrate the underlying sinusoid. First we sampled at less than the Nyquist frequency: the resulting graphs appear in Figure 1. Then, we sampled at the Nyquist frequency and triple the Nyquist frequency: the resulting graphs appear in Figure 2. As you can see, the samples at less than the Nyquist frequency are periodic, but it is not easy to see that the underlying signal is a sinusoid or determine its amplitude or frequency. At the Nyquist frequency, the signal is clearly sinusoidal, and its amplitude and frequency can be easily determined. Finally, at triple the Nyquist frequency, the picture smooths out even further and looks almost like a continuous waveform.

2.2 Mixing

In the second week of the lab, we used analog and digital mixers to combine waveforms generated by SRS generators and compared the outputs. First, we used an analog DSB to combine signals of

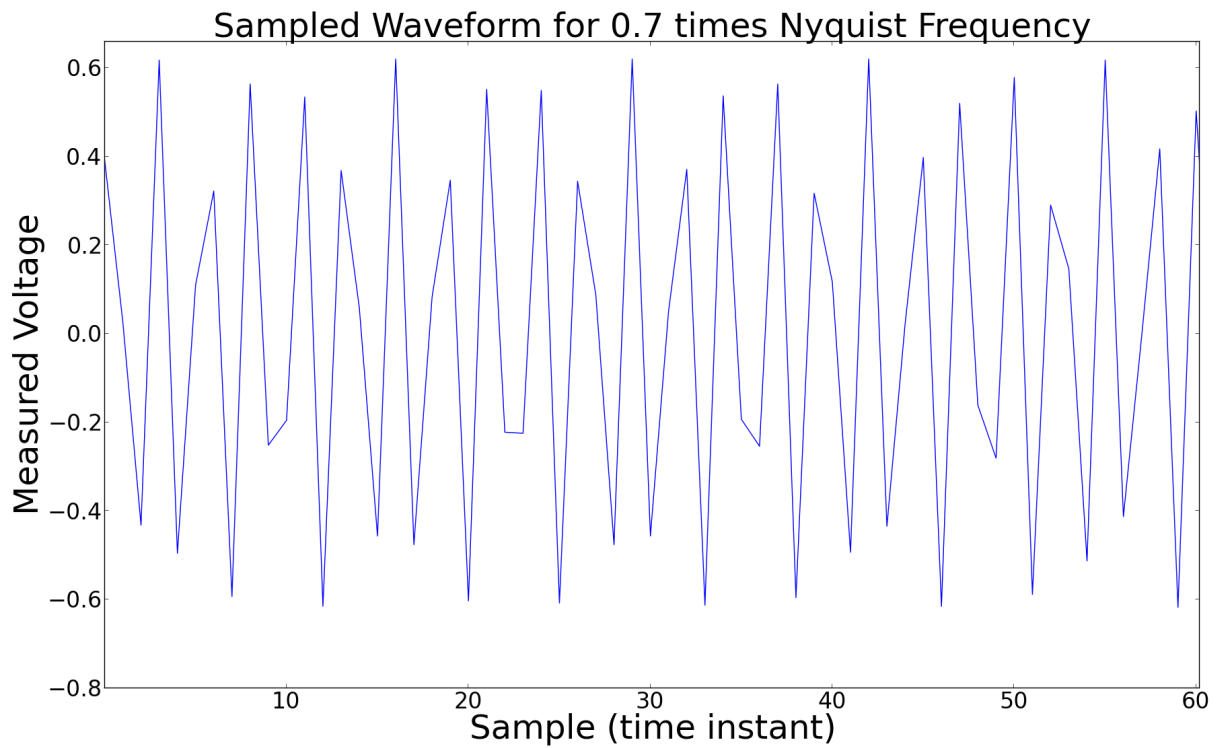
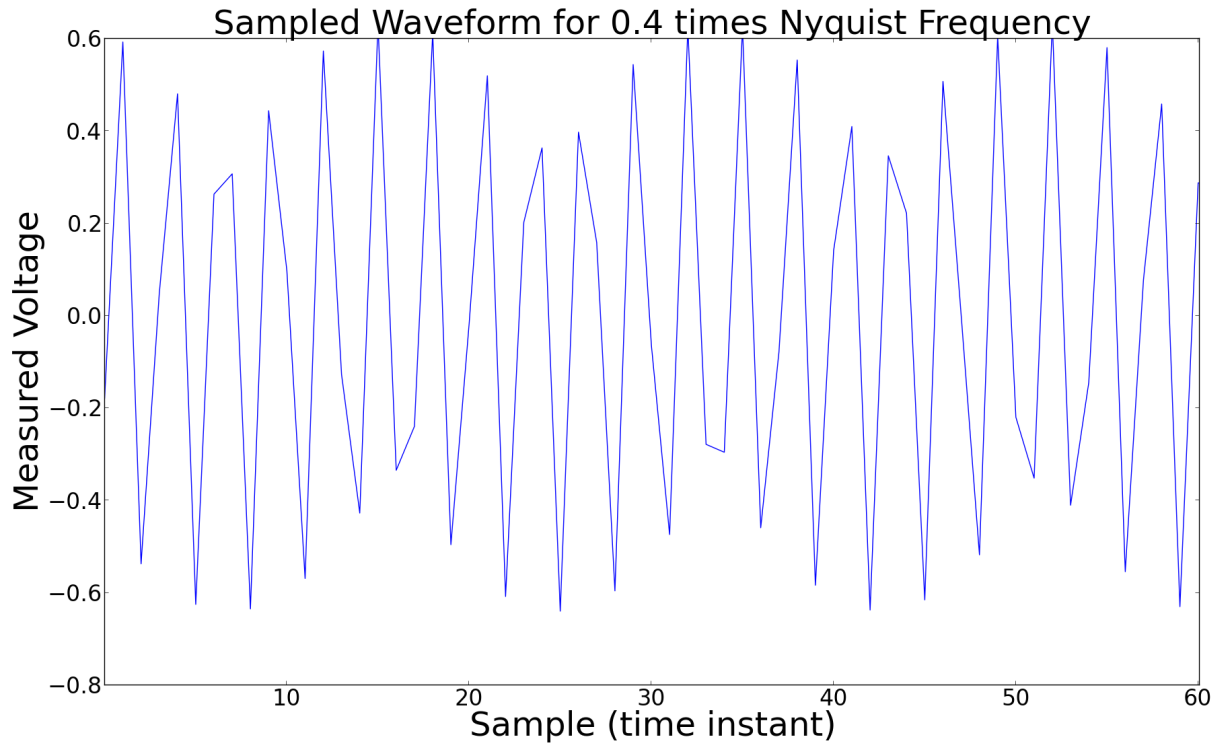


Figure 1: Sinusoidal signal sampled at 0.4 and 0.7 times Nyquist frequency.

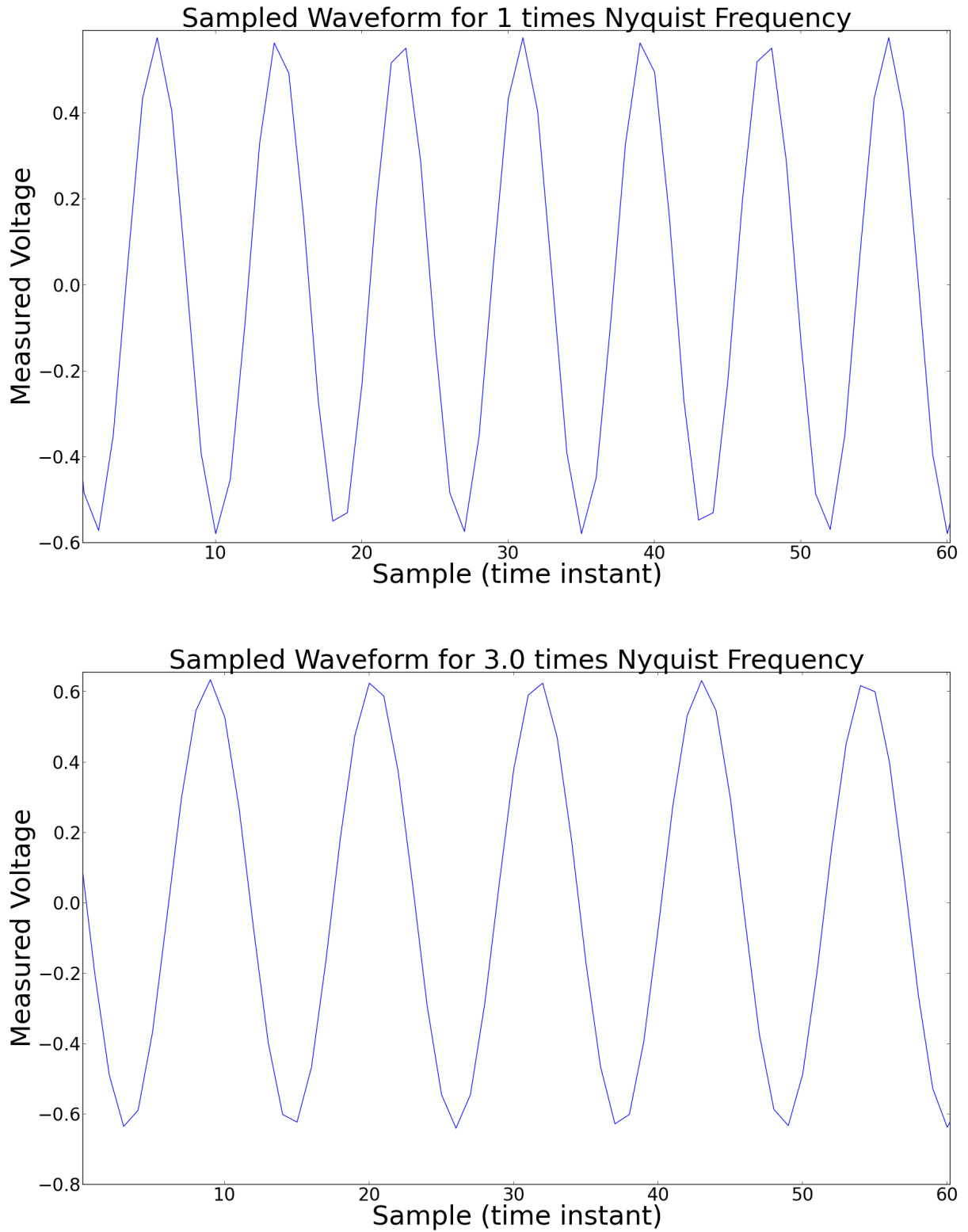


Figure 2: Sinusoidal signal sampled at 1 and 3 times Nyquist frequency.

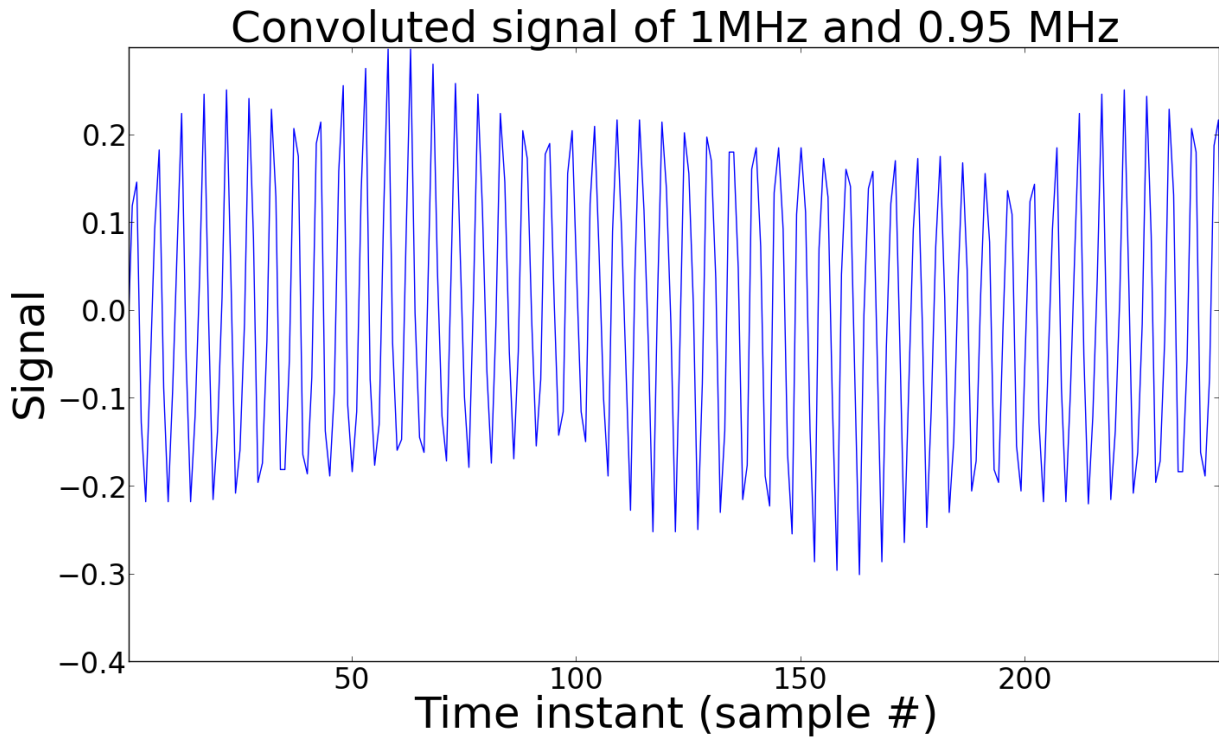


Figure 3: Convoluted signal of a 0.95 MHz wave and a 1.0 MHz wave

0.95 and 1.0 MHz as well as signals of 1.05 and 1.0 MHz. The waveform for the first case appears in Figure 3.

From the waveform, we calculated the power spectrum using a Fourier transform: the results appear in Figure 4.

As you can see, the power amplitude coefficients strongly peak around 2 MHz, because that is roughly the sum of the frequencies we mixed. Looking closely, one can see that the highest peak of the mixture of 0.95 MHz and 1.0 MHz is at slightly less than 2 MHz, while the highest peak of the mixture of 1.05 and 1.0 MHz is slightly greater than 2 MHz, as expected. In addition, you can see the “lower sideband”, the small collection of non-negligible frequencies centered around 0, and the “upper sideband”, the small collection of non-negligible frequencies centered around 4. These frequencies appear as artifacts of the mixing process. In addition, the whole distribution is reproduced on the negative side of the x-axis, because actual waveforms are complex exponentials, so the sine wave we mixed with is actually represented by $\sin x = 1/2 * i * (e^{-ix} - e^{ix})$, so we ended up convolving our 1.0 MHz local oscillator with waves of frequency 0.95 and -0.95 MHz in the first case, and 1.05 and -1.05 MHz in the second case.

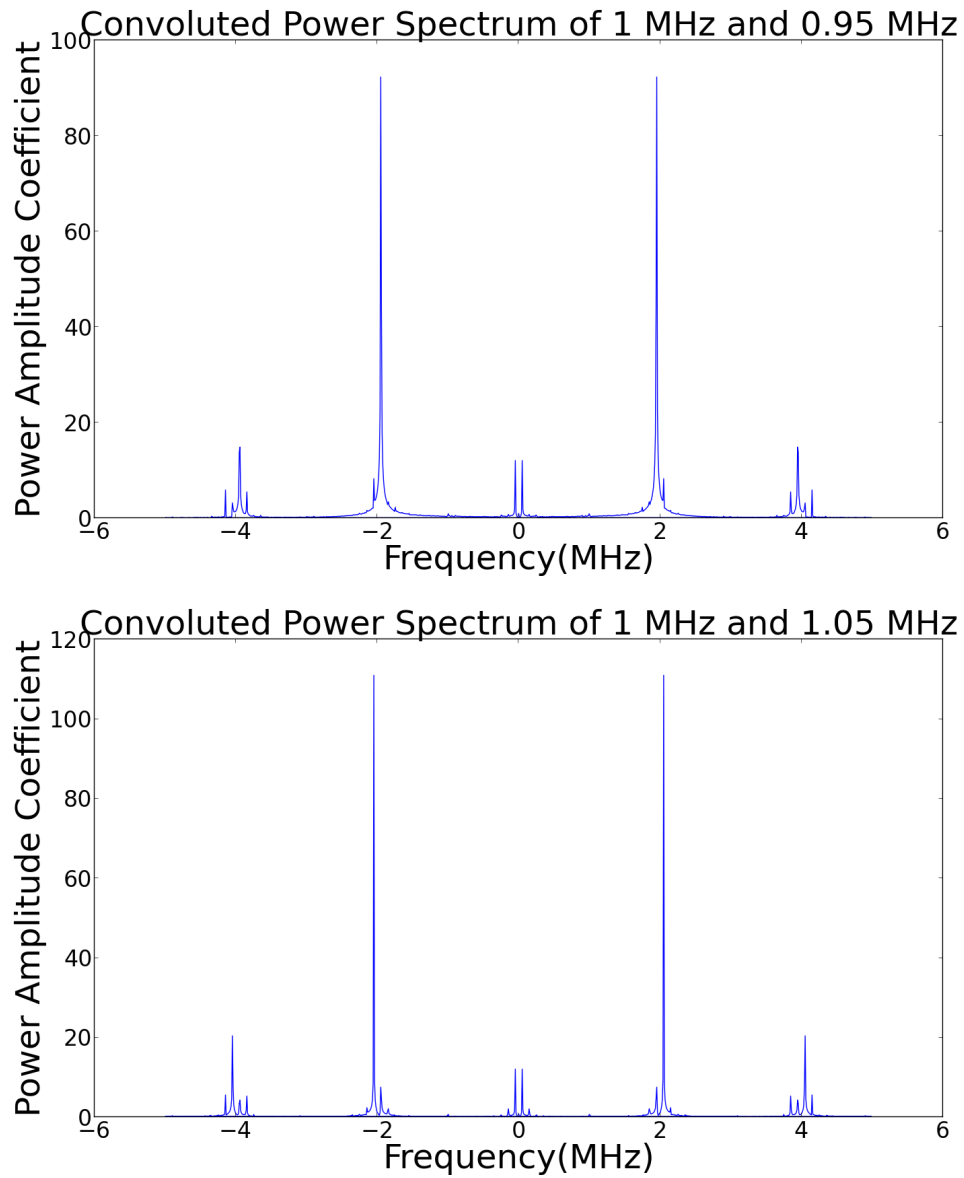


Figure 4: Analog DSB convolution power spectra of 0.95 MHz and 1.0 MHz (top), and 1.05 MHz and 1.0 MHz (bottom).