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10º Trabalho - Lista 5

76) Encontrar valor aproximado

$$f) \sqrt{(4,03)^2 + (2,9)^2}$$

$$\Rightarrow f(x, y) = \sqrt{x^2 + y^2}$$

Utilizando valores inteiros.

$$F(4;3) = \sqrt{4^2 + 3^2} = 5$$

$$\Delta x = 4,03 - 4 = 0,03$$

$$\Delta y = 2,9 - 3 = -0,1$$

$$\Delta y = 2,9 - 3 = -0,1$$

Desta forma:

$$dz \approx \Delta z$$

$$dz \approx F(4,03; 2,9) - F(4;3)$$

$$F(4,03; 2,9) = F(4;3) + dz$$

$$\Rightarrow F(4,03; 2,9) = F(4;3) + dz$$

$$* f_x(x,y) = (2x) \left(\frac{1}{2\sqrt{x^2+y^2}} \right) = \frac{x}{\sqrt{x^2+y^2}}$$

$$* f_y(x,y) = \frac{y}{\sqrt{x^2+y^2}}$$

$$\hookrightarrow f_x(4;3) = 4/5$$

$$\hookrightarrow f_y(4;3) = 3/5$$

$$\rightarrow F(4,03; 2,9) \approx 5 + \int_x(4;3) dx + \int_y(4;3) dy$$

$$\rightarrow F(4,03; 2,9) \approx 5 + \left(\frac{4}{5}\right)(0,03) + \left(\frac{3}{5}\right)(-0,1)$$

$$\rightarrow F(4,03; 2,9) \approx 4,964$$

$$\therefore \sqrt{(4,03)^2 + (2,9)^2} \approx 4,964$$