

# Exercícios de Dedução Natural

## Lógica para Computação

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1.  $\vdash \forall x P(x) \rightarrow \neg \exists x \neg P(x)$
2.  $\vdash \neg \exists x \neg P(x) \rightarrow \forall x P(x)$
3.  $\vdash \exists x P(x) \rightarrow \neg \forall x \neg P(x)$
4.  $\vdash \neg \forall x \neg P(x) \rightarrow \exists x P(x)$
5.  $\vdash \forall x (P(x) \wedge Q(x)) \rightarrow (\forall x P(x) \wedge \forall x Q(x))$
6.  $\vdash \forall x \forall y P(x, y) \rightarrow \forall y \forall x P(x, y)$
7.  $\vdash \forall x (P \rightarrow Q(x)) \rightarrow (P \rightarrow \forall x Q(x))$ , onde  $x \notin VL(P)$
8.  $\vdash \exists x (P(x) \vee Q(x)) \rightarrow (\exists x P(x) \vee \exists x Q(x))$
9.  $\vdash \neg \forall x P(x) \rightarrow \exists x \neg P(x)$
10.  $\vdash \exists x \neg P(x) \rightarrow \neg \forall x P(x)$
11.  $\vdash \neg \exists x P(x) \rightarrow \forall x \neg P(x)$
12.  $\vdash \forall x \neg P(x) \rightarrow \neg \exists x P(x)$
13.  $\vdash \exists x (P(x) \wedge Q) \rightarrow (\exists x P(x) \wedge Q)$ , onde  $x \notin VL(Q)$
14.  $\vdash (\exists x P(x) \wedge Q) \rightarrow \exists x (P(x) \wedge Q)$ , onde  $x \notin VL(Q)$
15.  $\vdash \forall x (P(x) \vee Q) \rightarrow (\forall x P(x) \vee Q)$ , onde  $x \notin VL(Q)$
16.  $\vdash (\forall x P(x) \vee Q) \rightarrow \forall x (P(x) \vee Q)$ , onde  $x \notin VL(Q)$
17.  $\vdash \exists x (P(x) \rightarrow Q) \rightarrow (\forall x P(x) \rightarrow Q)$ , onde  $x \notin VL(Q)$
18.  $\vdash (\forall x P(x) \rightarrow Q) \rightarrow \exists x (P(x) \rightarrow Q)$ , onde  $x \notin VL(Q)$
19.  $\vdash \exists x (P \rightarrow Q(x)) \rightarrow (P \rightarrow \exists x Q(x))$ , onde  $x \notin VL(P)$
20.  $\vdash (P \rightarrow \exists x Q(x)) \rightarrow \exists x (P \rightarrow Q(x))$ , onde  $x \notin VL(P)$
21.  $\vdash \exists x (P(x) \rightarrow \forall x P(x))$
22.  $\forall x \neg (P(x) \wedge \neg Q(x)), \forall x P(x) \models \forall x M(x)$
23.  $\forall x \neg (P(x) \wedge \neg Q(x)), \neg \forall x Q(x) \models \neg \forall x P(x)$
24.  $\forall x \neg (P(x) \wedge \neg Q(x)), \exists x \neg Q(x) \models \neg \forall x P(x)$
25.  $\forall x \neg (P(x) \wedge \neg Q(x)), \exists x \neg Q(x) \models \exists x \neg P(x)$