

2021 - PHY 981 - Homework set 10 (due Mar 28)

1. link to lecture notes
link to nushellx.zip
link to toi.zip link to mingw-w64.zip
2. Read Chapters 22-23.
3. Derive Eqs. 22.26 and 22.27.
4. Use Eq. 22.31 to obtain an expression for $\langle C | \hat{F} | C \rangle$.
5. Use the second-quantization method to reduce the following many-particle matrix elements to a sum of single-particle matrix elements for the states (a, b, c, d) . (1111) means they are all filled, etc.
 $\langle (1100) | \hat{F} | (1100) \rangle$, $\langle (1100) | \hat{F} | (1010) \rangle$, $\langle (1100) | \hat{F} | (0101) \rangle$,
 $\langle (1100) | \hat{F} | (0011) \rangle$.
6. For the last problem replace \hat{F} with the number operator of Eq. 22.33.
7. Calculate the B(E2) for the $1/2^+$ to $5/2^+$ transitions in ^{17}F and ^{17}O assuming these states are represented by $1s_{1/2}$ and $0d_{5/2}$. single-particle states outside of a ^{16}O closed shell. Use harmonic-oscillator radial wavefunctions with $\hbar\omega = 14$ MeV. Use can use the *rme* program for the matrix elements. Compare to experiment.
8. What are all possible (ℓ, S, T) values for each of the following:
a) a $J^\pi = 3^-$ resonance of the two-neutron system.
b) a $J^\pi = 2^-$ resonance of the two-nucleon system with $T_z = 1$.
c) a $J^\pi = 2^+$ resonance of the two-nucleon system with $T_z = 0$.
9. For the configuration $(0f_{7/2})^2$ for two neutrons what are the allowed J values?
10. For the configuration $(0f_{7/2}, 1p_{3/2})$ for two neutrons what are the allowed J values?
11. For the configuration $(0f_{7/2})^2$ for two nucleons what are the allowed combinations of (J, T) values?