

2021 - PHY 981 - Homework set 15 (final exam) (due May 2)

link to lecture notes

link to nushellx.zip

link to toi.zip link to mingw-w64.zip

There are 8 problems.

1. The 0^+ state at 3.067 MeV in ^{20}Na has a proton decay width of 36 keV. It decays to the $1/2^+$ ground state of ^{19}Ne . Obtain the experimental spectroscopic factor for this decay by using the wspot app to calculate the single-particle proton decay width.
2. This 0^+ state in ^{20}Na is calculated to decay the 1^+ state at 0.984 MeV with a $B(M1) = 1.85 \mu_N^2$. If the proton decay and this gamma decay are the only modes of decay, what is the branching ratio for the gamma decay?
3. In the $0f_{7/2}$ model space for the calcium isotopes, (a) what is the spectroscopic factor for $^{45}\text{Ca } 7/2^-$ to $^{44}\text{Ca } 0^+$? (b) What is the sum over all states in ^{44}Ca ?
4. What are the maximum J and T values allowed for ^{46}V in the $(0f1p)$ model space?
5. What are the spatial tensor ranks of the following operators (put “none” if it is not a tensor)?
 - a) The creation operator a_k^+ for the proton orbital $\alpha = (n, \ell, j) = (0, 2, 5/2)$.
 - b) The destruction operator a_k for proton orbital $\alpha = (n, \ell, j) = (0, 2, 5/2)$.
 - c) The two-body isospin operator $\tau_{zi}\tau_{zj}$.
 - d) The δ function interaction between two nucleons.
 - e) The two-body Coulomb interaction.
 - f) The magnetic moment operator.
6. What are the isospin tensor ranks for the above (put “none” if it is not a tensor)?

7. Reduce the following many-body wavefunction matrix elements of a one-body operator to a sum of single-particle terms. (a, b, c, d) represent different occupied m states. (a) $\langle a, b | \hat{F} | a, b \rangle$; (b) $\langle a, b | \hat{F} | a, c \rangle$; (c) $\langle a, b | \hat{F} | c, d \rangle$.

8. The magnetic moment of the $9/2^+$ ground state of ^{91}Nb is $+6.521 \mu_N$. Assuming that this is a $0g_{9/2}$ single-particle state, calculate the magnetic moment of the 8^+ state of ^{92}Mo assuming that it has a $(0g_{9/2})^2$ configuration. Compare to experiment.