



# Transmission Lines and Antennas, 2012-3

## Exercises on Load Matching

### 1 Pozar, 5.1

The arrangement of two lumped elements, series-shunt or shunt-series receives the name of L-section due to the L-shape these arrangements present. Using the Smith Chart, design lossless L-section matching networks for the following normalized load impedances:

1.  $z_L = 1.5 - j2.0$
2.  $z_L = 0.5 + j0.3$
3.  $z_L = 0.2 - j0.9$
4.  $z_L = 2.0 - j0.3$

Compute actual component values (L, C) if the line impedance is  $75\Omega$  and the operation frequency is 7GHz.

### 2

Repeat exercise 1 using transmission lines of minimum length. Verify your designs using an RF simulation tool.

### 3

Compare the graphical solution obtained in exercise 1 with the one obtained from these formulas, which allow matching a load with impedance  $Z_L = R_L + jX_L$  to a line with impedance  $Z_0$ :

- For loads outside the unit conductance circle (i.e.  $g < 1$ ) we use a shunt-series arrangement with these values:

$$B = \frac{X_L \pm \sqrt{R_L/Z_0} \sqrt{R_L^2 + X_L^2 - Z_0 R_L}}{R_L^2 + X_L^2}$$

$$X = \frac{1}{B} + \frac{X_L Z_0}{R_L} - \frac{Z_0}{B R_L}$$

- For loads outside the unit resistance circle (i.e.  $r < 1$ ) we use a series-shunt arrangement with these values:

$$X = \pm \sqrt{R_L(Z_0 - R_L)} - X_L$$

$$B = \pm \frac{\sqrt{(Z_0 - R_L)/R_L}}{Z_0} \quad (1)$$

Note that each of these conditions leads to two different solutions. Furthermore, some loads satisfy both conditions ( $g < 1$  and  $r < 1$ ); these admit four different matching networks.

### 4

Power handling of transmission lines is partly limited by breakdown of the filling dielectric; for this reason, the maximum voltage along the line must be kept below a given value  $V_{max}$  related to the dielectric strength of the filling material and the actual geometry of the line. Compare the maximum power a transmission line with rating  $V_{max}$  can deliver to a matched load and to an unmatched load (assume a  $\Gamma \neq 0$  value). Based on this, discuss the implications of unmatched loads in terms of system complexity and cost.