MEMORY HIERARCHY

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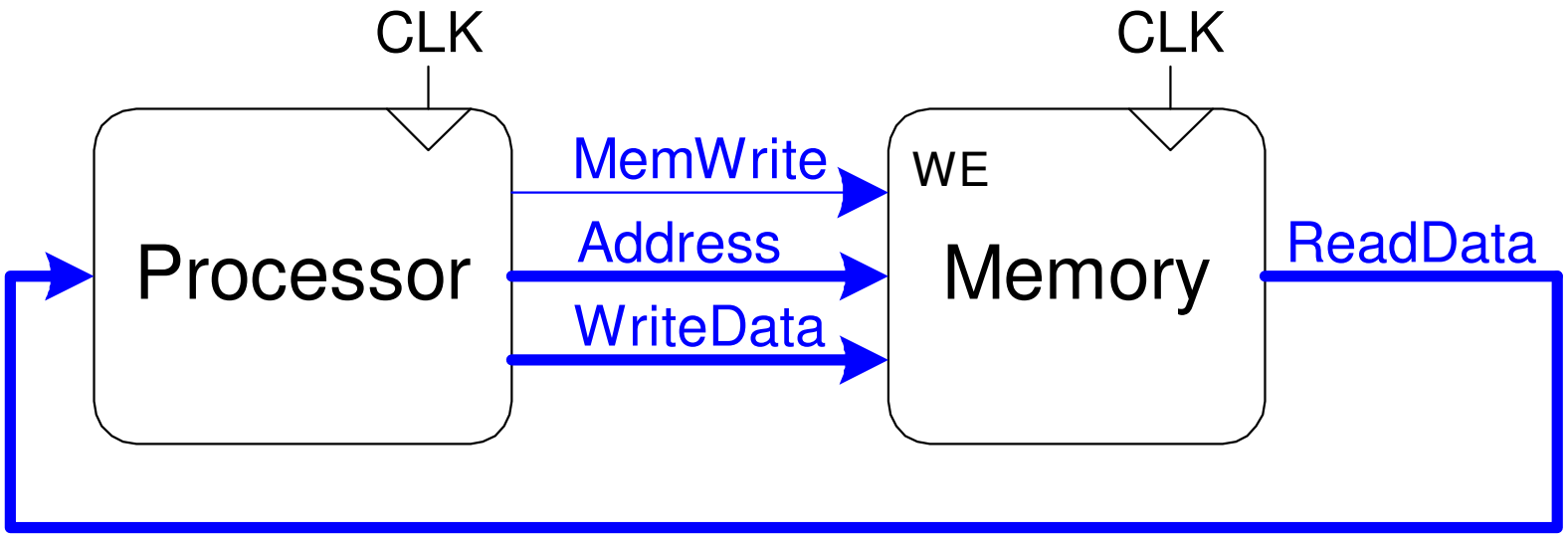
Introduction

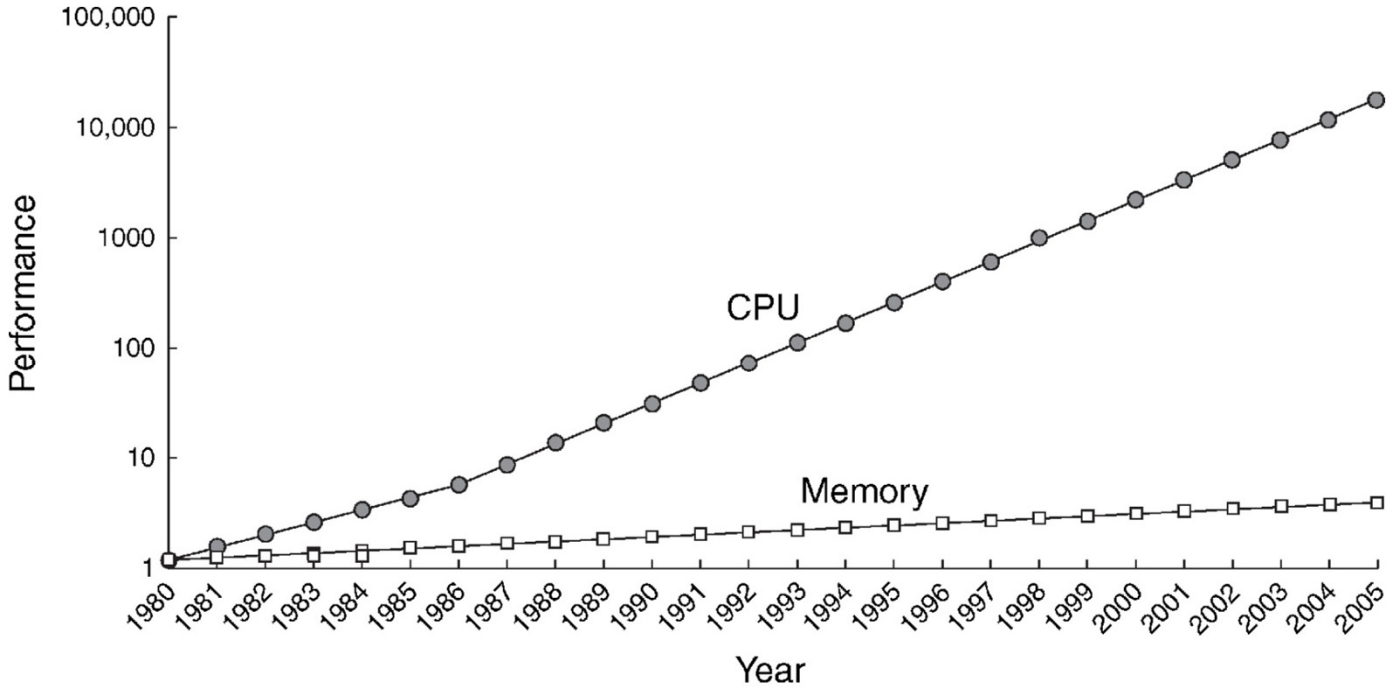
- Computer performance depends on:
  - Processor performance
  - Memory system performance

Memory Interface



Introduction

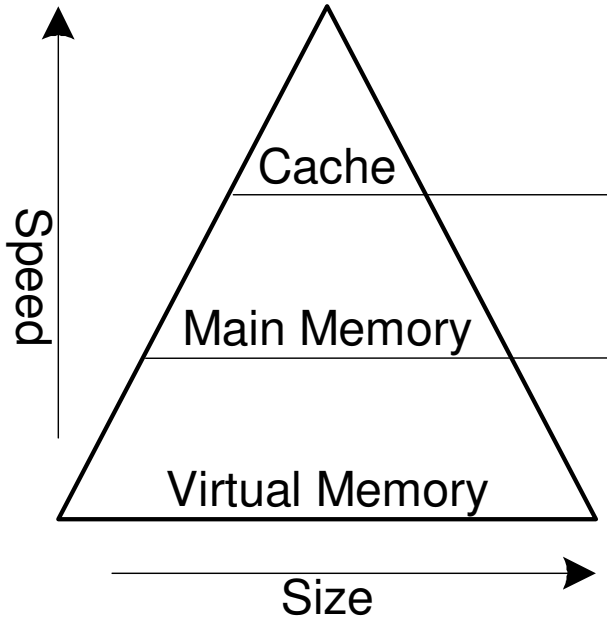
- Up until now, assumed memory could be accessed in 1 clock cycle
- But that hasn't been true since the 1980's



Memory System Challenge

- Make memory system appear as fast as processor
- Use a hierarchy of memories
- Ideal memory:
  - Fast
  - Cheap (inexpensive)
  - Large (capacity)
- But we can only choose two!

Memory Hierarchy



Technology	cost / GB	Access time
SRAM	~ $10,000	~ 1 ns
DRAM	~ $100	~ 100 ns
Hard Disk	~ $1	~ 10,000,000 ns

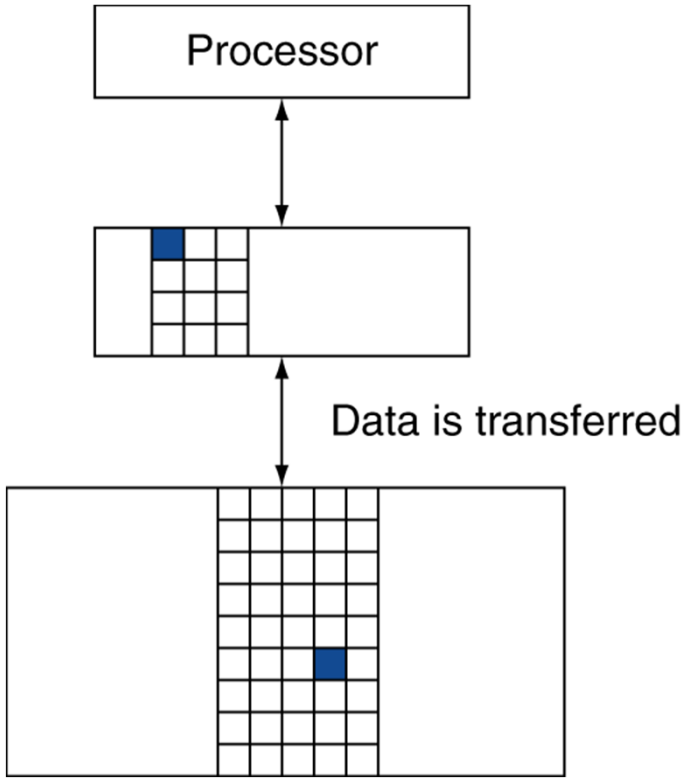
Principle of Locality

- Programs access a small proportion of their address space at any time
- Temporal locality
  - Items accessed recently are likely to be accessed again soon
  - e.g., instructions in a loop, induction variables
- Spatial locality
  - Items near those accessed recently are likely to be accessed soon
  - E.g., sequential instruction access, array data

Taking Advantage of Locality

- Memory hierarchy
- Store everything on disk
- Copy recently accessed (and nearby) items from disk to smaller DRAM memory
  - Main memory
- Copy more recently accessed (and nearby) items from DRAM to smaller SRAM memory
  - Cache memory attached to CPU

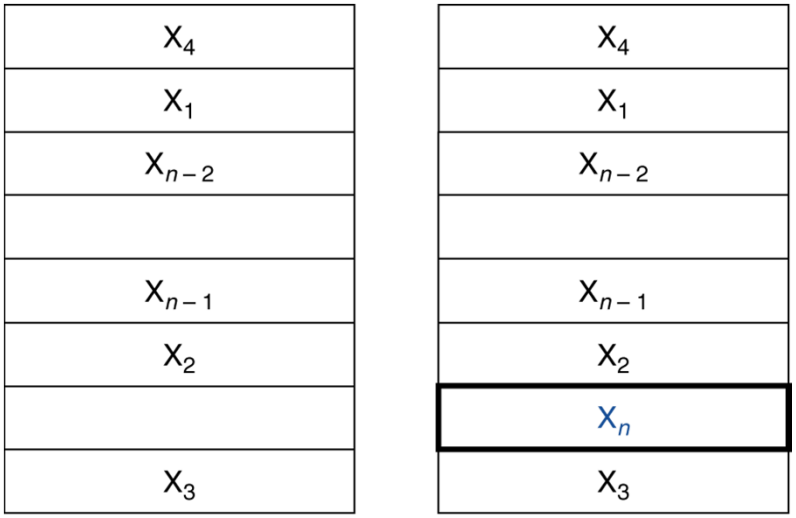
Memory Hierarchy Levels



- Block (aka line): unit of copying
  - May be multiple words
- If accessed data is present in upper level
  - Hit: access satisfied by upper level
    - Hit ratio: hits/accesses
- If accessed data is absent
  - Miss: block copied from lower level
    - Time taken: miss penalty
    - Miss ratio: misses/accesses
      = 1 – hit ratio
  - Then accessed data supplied from upper level

Cache Memory

- Cache memory
  - The level of the memory hierarchy closest to the CPU
- Given accesses X_1, …, $X_{n–1}$, X_n



a. Before the reference to X_n b. After the reference to X_n

- How do we know if the data is present?
- Where do we look?

Cache Terminology

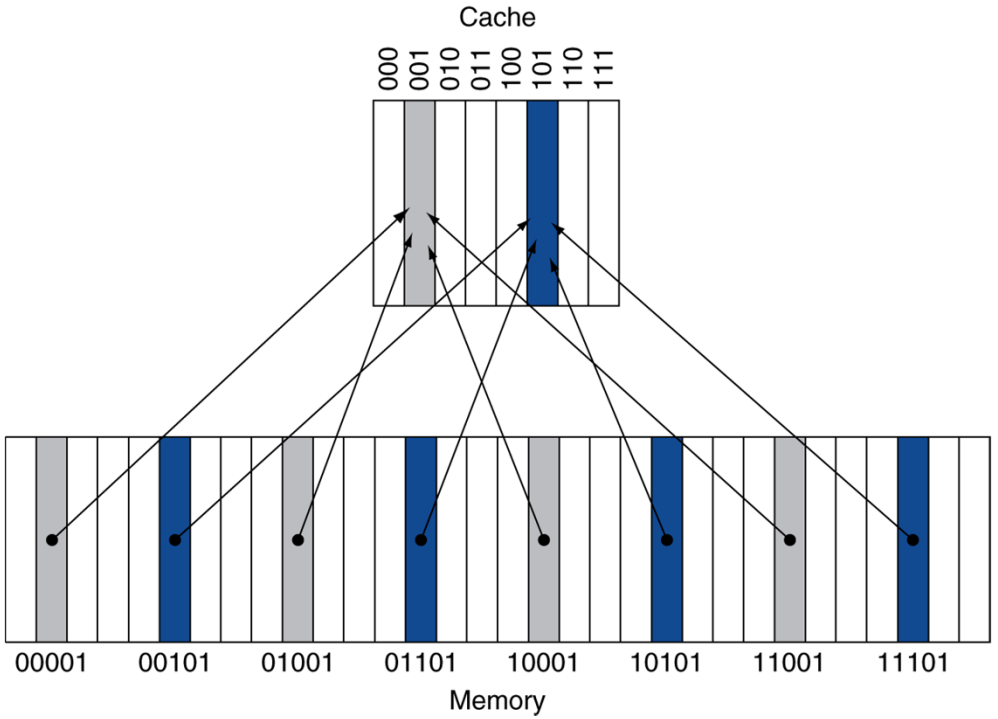
- Capacity (*C*):
  - the number of data bytes a cache stores
- Block size (*b*):
  - bytes of data brought into cache at once
- Number of blocks (*B = C/b*):
  - number of blocks in cache: *B = C/b*
- Degree of associativity (*N*):
  - number of blocks in a set
- Number of sets (*S = B/N*):
  - each memory address maps to exactly one cache set

How is data found?

- Cache organized into *S* sets
- Each memory address maps to exactly one set
- Caches categorized by number of blocks in a set:
  - **Direct mapped:** 1 block per set
  - **N-way set associative:** N blocks per set
  - **Fully associative:** all cache blocks are in a single set
- Examine each organization for a cache with:
  - Capacity (C = 8 words)
  - Block size (b = 1 word)
  - So, number of blocks (B = 8)

Direct Mapped Cache

- Location determined by address
- Direct mapped: only one choice
  - (Block address) modulo (#Blocks in cache)



- #Blocks is a power of 2
- Use low-order address bits

Tags and Valid Bits

- How do we know which particular block is stored in a cache location?
  - Store block address as well as the data
  - Actually, only need the high-order bits
  - Called the tag
- What if there is no data in a location?
  - Valid bit: 1 = present, 0 = not present
  - Initially 0

Cache Example

- 8-blocks, 1 word/block, direct mapped
- Initial state

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	N		
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Miss	110

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	**Y**	**10**	**Mem[10110]**
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
26	11 010	Miss	010

Index	V	Tag	Data
000	N		
001	N		
010	**Y**	**11**	**Mem[11010]**
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Hit	110
26	11 010	Hit	010

Index	V	Tag	Data
000	N		
001	N		
010	Y	11	Mem[11010]
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
16	10 000	Miss	000
3	00 011	Miss	011
16	10 000	Hit	000

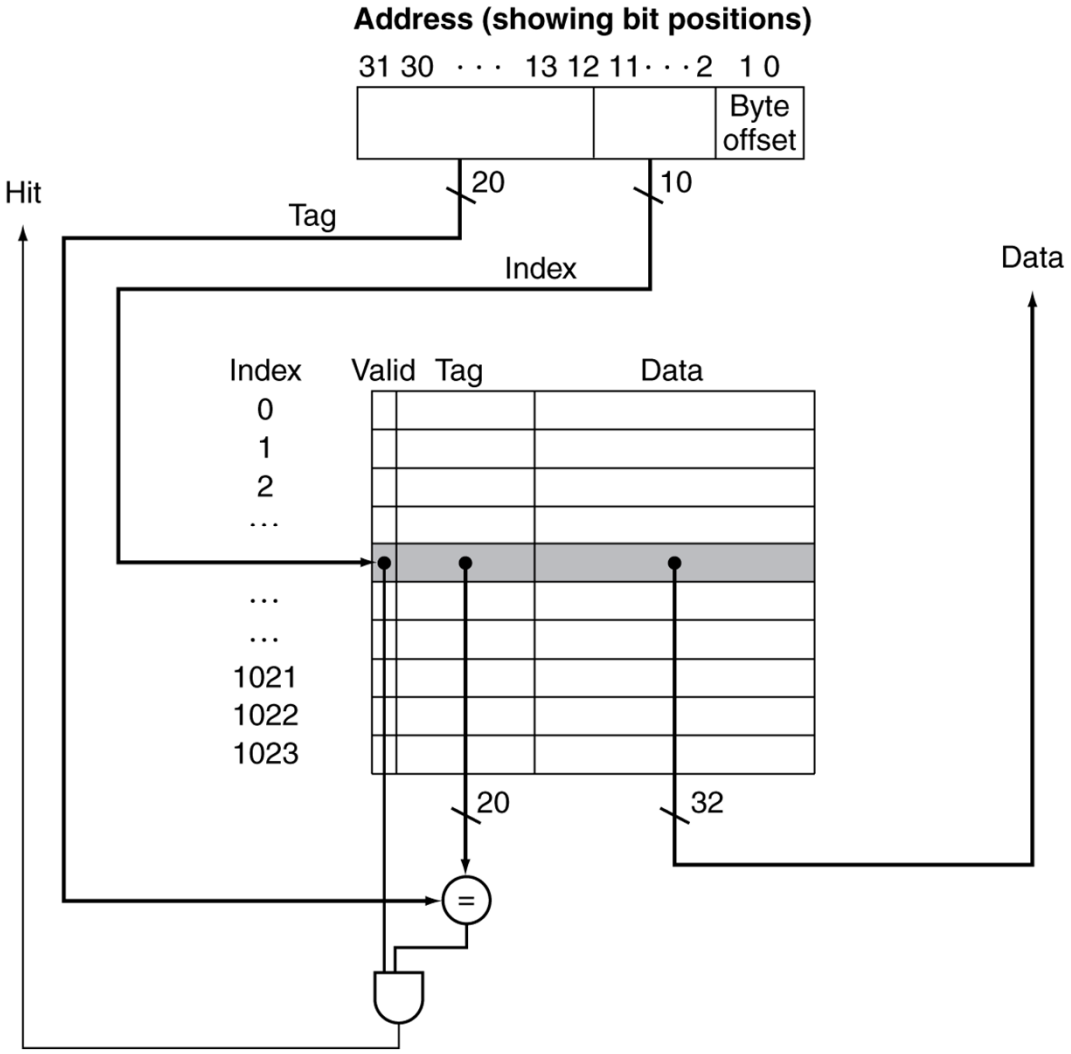
Index	V	Tag	Data
000	**Y**	**10**	**Mem[10000]**
001	N		
010	Y	11	Mem[11010]
011	**Y**	**00**	**Mem[00011]**
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
18	10 010	Miss	010

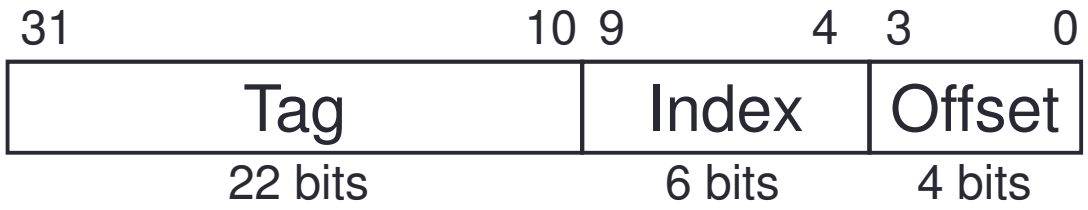
Index	V	Tag	Data
000	Y	10	Mem[10000]
001	N		
010	**Y**	**10**	**Mem[10010]**
011	Y	00	Mem[00011]
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Address Subdivision



Example: Larger Block Size

- 64 blocks, 16 bytes/block
  - To what block number does address 1200 map?
- Block address = $\lfloor 1200/16 \rfloor = 75$
- Block number = 75 modulo 64 = 11



Block Size Considerations

- Larger blocks should reduce miss rate
  - Due to spatial locality
- But in a fixed-sized cache
  - Larger blocks $\Rightarrow$ fewer of them
    - More competition $\Rightarrow$ increased miss rate
  - Larger blocks $\Rightarrow$ pollution
- Larger miss penalty
  - Can override benefit of reduced miss rate
  - Early restart and critical-word-first can help

Cache Misses

- On cache hit, CPU proceeds normally
- On cache miss
  - Stall the CPU pipeline
  - Fetch block from next level of hierarchy
  - Instruction cache miss
    - Restart instruction fetch
  - Data cache miss
    - Complete data access

Write-Through

- On data-write hit, could just update the block in cache
  - But then cache and memory would be inconsistent
- Write through: also update memory
- But makes writes take longer
  - e.g., if base CPI = 1, 10% of instructions are stores, write to memory takes 100 cycles
    - Effective CPI = 1 + 0.1×100 = 11
- Solution: write buffer
  - Holds data waiting to be written to memory
  - CPU continues immediately
    - Only stalls on write if write buffer is already full

Write-Back

- Alternative: On data-write hit, just update the block in cache
  - Keep track of whether each block is dirty
- When a dirty block is replaced
  - Write it back to memory
  - Can use a write buffer to allow replacing block to be read first

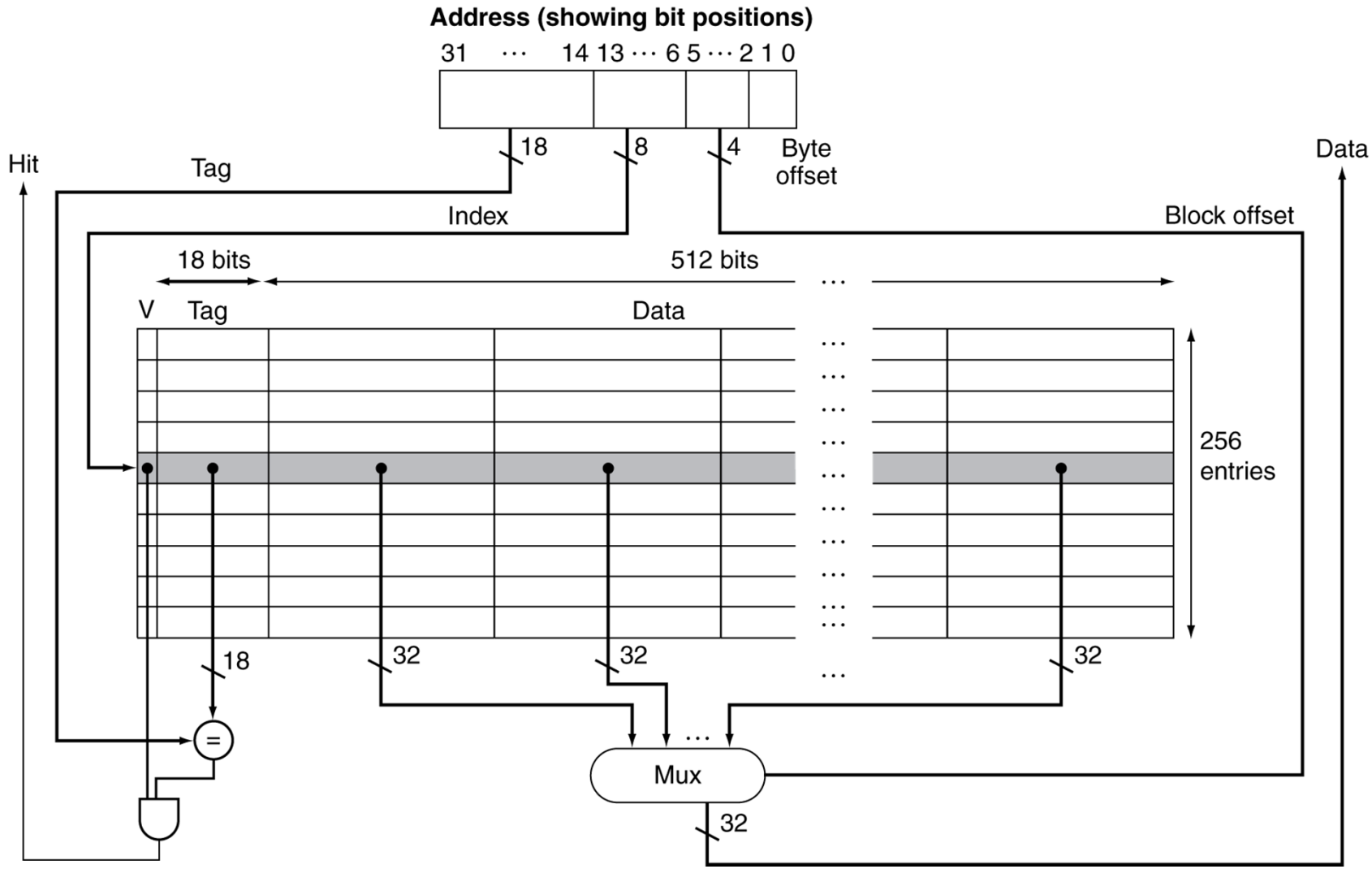
Write Allocation

- What should happen on a write miss?
- Alternatives for write-through
  - Allocate on miss: fetch the block
  - Write around: don’t fetch the block
    - Since programs often write a whole block before reading it (e.g., initialization)
- For write-back
  - Usually fetch the block

Example: Intrinsity FastMATH

- Embedded MIPS processor
  - 12-stage pipeline
  - Instruction and data access on each cycle
- Split cache: separate I-cache and D-cache
  - Each 16KB: 256 blocks × 16 words/block
  - D-cache: write-through or write-back
- SPEC2000 miss rates
  - I-cache: 0.4%
  - D-cache: 11.4%
  - Weighted average: 3.2%

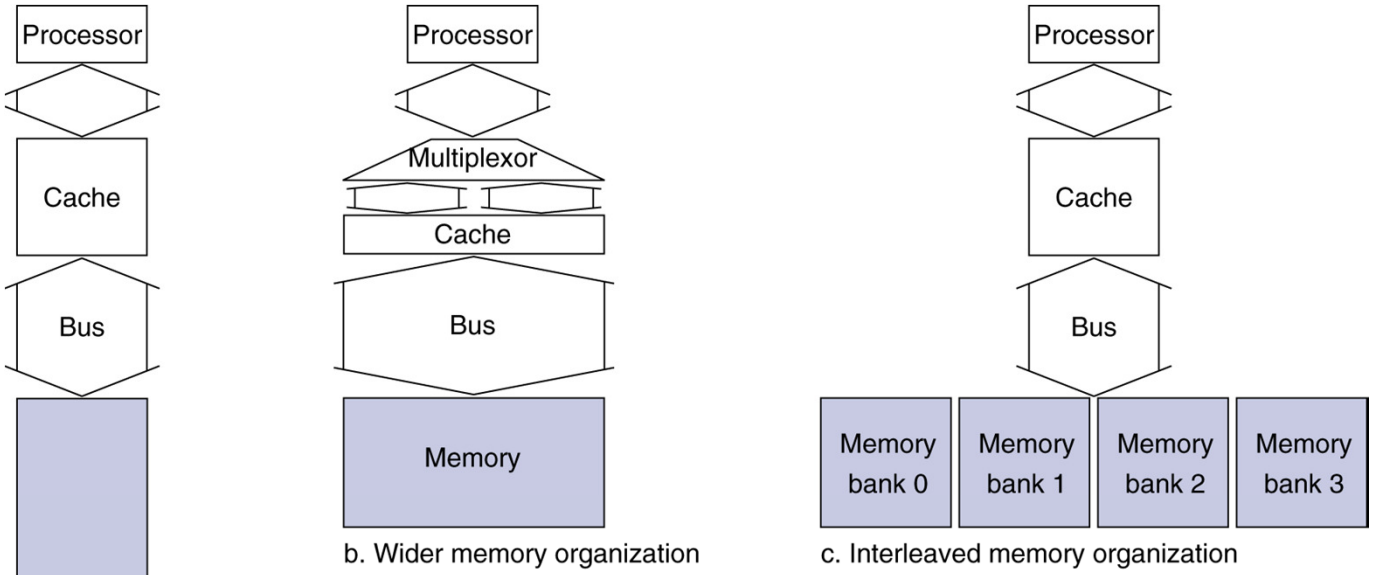
Example: Intrinsity FastMATH



Main Memory Supporting Caches

- Use DRAMs for main memory
  - Fixed width (e.g., 1 word)
  - Connected by fixed-width clocked bus
    - Bus clock is typically slower than CPU clock
- Example cache block read
  - 1 bus cycle for address transfer
  - 15 bus cycles per DRAM access
  - 1 bus cycle per data transfer
- For 4-word block, 1-word-wide DRAM
  - Miss penalty = 1 + 4×15 + 4×1 = 65 bus cycles
  - Bandwidth = 16 bytes / 65 cycles = 0.25 B/cycle

Increasing Memory Bandwidth



a. One-word-wide memory organization

b. Wider memory organization

c. Interleaved memory organization

- 4-word wide memory
  - Miss penalty = 1 + 15 + 1 = 17 bus cycles
  - Bandwidth = 16 bytes / 17 cycles = 0.94 B/cycle
- 4-bank interleaved memory
  - Miss penalty = 1 + 15 + 4×1 = 20 bus cycles
  - Bandwidth = 16 bytes / 20 cycles = 0.8 B/cycle

Advanced DRAM Organization

- Bits in a DRAM are organized as a rectangular array
  - DRAM accesses an entire row
  - Burst mode: supply successive words from a row with reduced latency
- Double data rate (DDR) DRAM
  - Transfer on rising and falling clock edges
- Quad data rate (QDR) DRAM
  - Separate DDR inputs and outputs

DRAM Generations

Year	Capacity	$/GB
1980	64Kbit	$1500000
1983	256Kbit	$500000
1985	1Mbit	$200000
1989	4Mbit	$50000
1992	16Mbit	$15000
1996	64Mbit	$10000
1998	128Mbit	$4000
2000	256Mbit	$1000
2004	512Mbit	$250
2007	1Gbit	$50