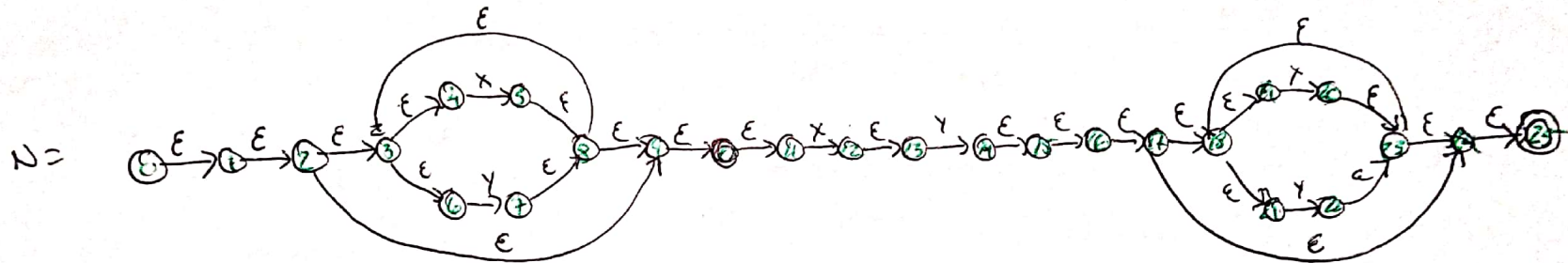


$$3. (x+y)^*xy(x+y)^*$$

a) AFN-ε



b)

$$\begin{aligned} \mathcal{E}(q_0) &= \{q_0, q_1, q_2, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\ \mathcal{E}(q_1) &= \{q_1, q_2, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\ \mathcal{E}(q_2) &= \{q_2, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\ \mathcal{E}(q_3) &= \{q_3, q_4\} \\ \mathcal{E}(q_4) &= \{q_4\} \\ \mathcal{E}(q_5) &= \{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\ \mathcal{E}(q_6) &= \{q_6\} \\ \mathcal{E}(q_7) &= \{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\ \mathcal{E}(q_8) &= \{q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\ \mathcal{E}(q_9) &= \{q_9, q_{10}, q_{11}\} \\ \mathcal{E}(q_{10}) &= \{q_{10}, q_{11}\} \\ \mathcal{E}(q_{11}) &= \{q_{11}\} \\ \mathcal{E}(q_{12}) &= \{q_{12}, q_{13}\} \\ \mathcal{E}(q_{13}) &= \{q_{13}\} \\ \mathcal{E}(q_{14}) &= \{q_{14}, q_{15}, q_{16}, q_{17}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\ \mathcal{E}(q_{15}) &= \{q_{15}, q_{16}, q_{17}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\ \mathcal{E}(q_{16}) &= \{q_{16}, q_{17}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \end{aligned}$$

$$\begin{aligned} \mathcal{E}(q_{17}) &= \{q_{17}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\ \mathcal{E}(q_{18}) &= \{q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\ \mathcal{E}(q_{19}) &= \{q_{19}\} \\ \mathcal{E}(q_{20}) &= \{q_{20}, q_{23}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\ \mathcal{E}(q_{21}) &= \{q_{21}\} \\ \mathcal{E}(q_{22}) &= \{q_{22}, q_{23}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\ \mathcal{E}(q_{23}) &= \{q_{23}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\ \mathcal{E}(q_{24}) &= \{q_{24}, q_{25}\} \\ \mathcal{E}(q_{25}) &= \{q_{25}\} \end{aligned}$$

b)

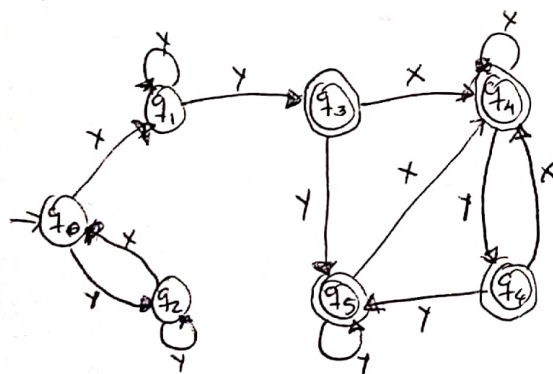
$$\begin{aligned}
\delta_m(q_0, x) &= \{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}\} \\
\delta_m(q_1, x) &= \{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}\} \\
\delta_m(q_2, x) &= \{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}\} \\
\delta_m(q_3, x) &= \delta(q_2, x) \\
\delta_m(q_4, x) &= \delta(q_2, x) \\
\delta_m(q_5, x) &= \delta(q_2, x) \\
\delta_m(q_6, x) &= \emptyset \\
\delta_m(q_7, x) &= \delta(q_2, x) \\
\delta_m(q_8, x) &= \delta(q_2, x) \\
\delta_m(q_9, x) &= \{q_{12}, q_{13}\} \\
\delta_m(q_{10}, x) &= \{q_{12}, q_{13}\} \\
\delta_m(q_{11}, x) &= \{q_{12}, q_{13}\} \\
\delta_m(q_{12}, x) &= \emptyset \\
\delta_m(q_{13}, x) &= \emptyset \\
\delta_m(q_{14}, x) &= \{q_{20}, q_{23}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\
\delta_m(q_{15}, x) &= \delta_m(q_{14}, x) \\
\delta_m(q_{16}, x) &= \delta_m(q_{14}, x) \\
\delta_m(q_{17}, x) &= \delta_m(q_{14}, x) \\
\delta_m(q_{18}, x) &= \delta_m(q_{14}, x) \\
\delta_m(q_{19}, x) &= \delta_m(q_{14}, x) \\
\delta_m(q_{20}, x) &= \delta_m(q_{14}, x) \\
\delta_m(q_{21}, x) &= \emptyset \\
\delta_m(q_{22}, x) &= \delta_m(q_{14}, x) \\
\delta_m(q_{23}, x) &= \delta_m(q_{14}, x) \\
\delta_m(q_{24}, x) &= \emptyset \\
\delta_m(q_{25}, x) &= \emptyset
\end{aligned}$$

$$\begin{aligned}
\delta_m(q_0, y) &= \{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\
\delta_m(q_1, y) &= \{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\
\delta_m(q_2, y) &= \{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\
\delta_m(q_3, y) &= \delta_m(q_2, y) \\
\delta_m(q_4, y) &= \emptyset \\
\delta_m(q_5, y) &= \{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\} \\
\delta_m(q_6, y) &= \delta(q_5, y) \\
\delta_m(q_7, y) &= \delta(q_5, y) \\
\delta_m(q_8, y) &= \delta(q_5, y) \\
\delta_m(q_9, y) &= \emptyset \\
\delta_m(q_{10}, y) &= \emptyset \\
\delta_m(q_{11}, y) &= \emptyset \\
\delta_m(q_{12}, y) &= \{q_{14}, q_{15}, q_{16}, q_{17}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\
\delta_m(q_{13}, y) &= \delta_m(q_{12}, y) \\
\delta_m(q_{14}, y) &= \{q_{22}, q_{23}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\} \\
\delta_m(q_{15}, y) &= \delta_m(q_{14}, y) \\
\delta_m(q_{16}, y) &= \delta_m(q_{14}, y) \\
\delta_m(q_{17}, y) &= \delta_m(q_{14}, y) \\
\delta_m(q_{18}, y) &= \delta_m(q_{14}, y) \\
\delta_m(q_{19}, y) &= \emptyset \\
\delta_m(q_{20}, y) &= \delta_m(q_{14}, y) \\
\delta_m(q_{21}, y) &= \delta_m(q_{14}, y) \\
\delta_m(q_{22}, y) &= \delta_m(q_{14}, y) \\
\delta_m(q_{23}, y) &= \delta_m(q_{14}, y) \\
\delta_m(q_{24}, y) &= \emptyset \\
\delta_m(q_{25}, y) &= \emptyset
\end{aligned}$$

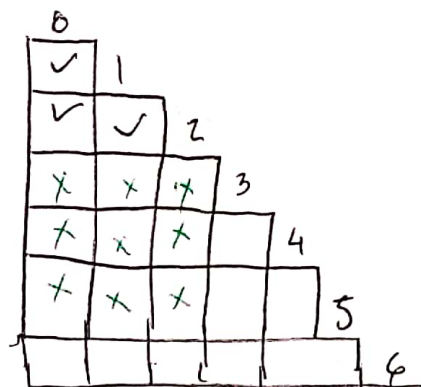
c)

	x	y
$\rightarrow q_0$	$\{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}\}^1$	$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\}^2$
$\{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}\}^1$	$\{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}\}^1$	$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{14}, q_{15}, q_{17}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\}^3$
$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\}^2$	$\{q_5, q_8, q_{13}, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}\}^1$	$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}\}^2$
$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{14}, q_{15}, q_{17}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\}^3$ F	$\{q_5, q_8, q_{13}, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}, q_{20}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\}^4$	$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{22}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\}^5$
$\{q_5, q_8, q_{13}, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}, q_{20}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\}^4$ F	$\{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}, q_{20}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\}^4$	$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{14}, q_{15}, q_{16}, q_{17}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}, q_{22}\}^6$
$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{22}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}, q_{25}\}^5$ F	$\{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}, q_{20}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}\}^4$	$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{22}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}\}^5$
$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{14}, q_{15}, q_{16}, q_{17}, q_{18}, q_{19}, q_{21}, q_{25}, q_{22}\}^6$ F	$\{q_5, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{12}, q_{13}, q_{20}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}\}^4$	$\{q_7, q_8, q_3, q_4, q_6, q_9, q_{10}, q_{11}, q_{22}, q_{25}, q_{18}, q_{19}, q_{21}, q_{24}\}^5$

AFD



d)



$\Rightarrow 3 \approx 4 \approx 5 \approx 6$

