

$$a) \quad \begin{aligned} S &= 0S0 \\ S &= 1S1 \\ S &= \epsilon \end{aligned}$$

$$S \rightarrow 0S0 \rightarrow 01S10 \rightarrow 010S010 \rightarrow 0100010$$

$$b) \quad a^i b^i c^j$$

$$\begin{aligned} S &= TE \\ T &= aTb \\ T &= \epsilon \\ E &= E_c \\ E &= \epsilon \end{aligned}$$

$$c) \quad a^i b^i c^j$$

$$\begin{aligned} S &= ET \\ E &= aE \\ E &= \epsilon \\ T &= aTb \\ T &= \epsilon \end{aligned}$$

$$d) \quad (ab)^*$$

$$\begin{aligned} S_1 &= abS_1 \\ S_1 &= \epsilon \end{aligned}$$

$$(ab)^k$$

$$\begin{aligned} S_2 &= S_2 ab \\ S_2 &= \epsilon \end{aligned}$$

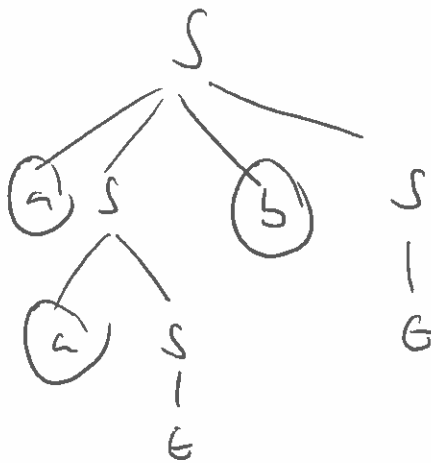
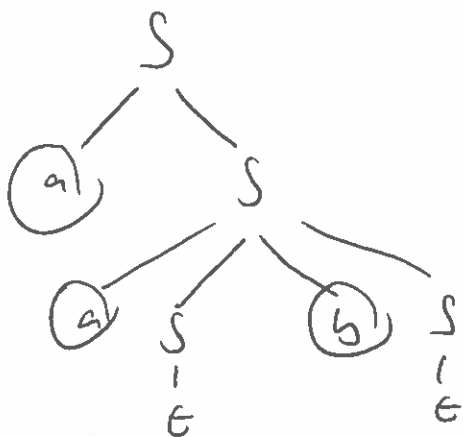
a.

$$S \rightarrow aS$$

$$S \rightarrow aSbS$$

$$S \rightarrow \epsilon$$

aab



b.

$$S \rightarrow aS \rightarrow aaSbS \rightarrow aabS \rightarrow aab$$

$$S \rightarrow aSbS \rightarrow aaaSbS \rightarrow aabS \rightarrow aab$$

c. $S \rightarrow aS \rightarrow aaaSbS \rightarrow aaaSb \rightarrow aab$

$$S \rightarrow aSbS \rightarrow aSb \rightarrow aaaSb \rightarrow aab$$

EC: ~~For condition~~

For the transition $S \rightarrow aS$, it's clear that more A 's are produced than B 's.

For transition $S \rightarrow aSbS$, there is an equal number of A 's and B 's produced.

Since at each transition, ~~there~~ we are either adding more A 's than B 's or keeping them equal, there will be at least as many A 's as B 's.