

Statistical Methods for CS

Weekly Questions Week 1

Q1 (a) $10! = 10 \times 9 \times 8 \times \dots \times 2 \times 1 = \boxed{3,628,800}$ ways.

(b) Let's consider E and F as a single letter.

~~Handwritten scribbles and crossed-out text.~~

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There are 9 letters in total.

$$9! = 362,880$$

E and F can be arranged in $2!$ ways

$$2! = 2$$

∴ Total no. of way to rearrange

$$= 9! \times 2! = \boxed{725,760} \text{ ways}$$

(c) There are 6 letters in BANANA.
There is 1 B, 3 A's, 2 N's.

Number of possible arrangements is $6!$, however we must remove duplicate words.

$$\Rightarrow \frac{6!}{(2! * 3!)} = \boxed{60} \text{ different letter arrangements.}$$

(d) Choose 3 letters from ABCDE

$$\text{(ie) } \cancel{5C3} \binom{5}{3} = \boxed{10}$$

Q2(a) The die has 6 possible outcomes each time it is rolled.

Therefore when it is rolled 4 times, the possible number of outcomes is:

$$6 \times 6 \times 6 \times 6 = 6^4 = \boxed{1296} \text{ outcomes}$$

(b) ~~Imagine~~ Imagine the rolls ordered from 1 to 4.
We can choose which rolls the ~~the~~ 3's will be rolled on as a combination.

Since there are ~~four~~ possible slots ~~one~~ and two 3's to place:

$$\binom{4}{2} = 6$$

After choosing the 3's, we have ~~two~~ slots remaining and five possible dice outcomes for each slot.

(As there cannot be anymore 3's)
Final answer:

$$6 * 5^2 = \boxed{150} \text{ possible outcomes}$$

(C) At least two 3's?

I will find the number of outcomes containing no 3's and outcomes ~~containing~~ containing one 3 and then minus these from the total no. of outcomes $\rightarrow 1296$.

How many contain exactly one 3?

Four possible slots and one 3 to place
 $\Rightarrow \binom{4}{1} = 4$

Three slots remaining and five ^{possible} dice outcomes for each slot:

$$4 * 5^3 = 500$$

How many contain no 3's?

Only 5 outcomes on ~~the~~ the dice roll will suffice (1, 2, 4, 5, 6) and there are 4 rolls:

$$\cancel{5^4} \quad 5^4 = 625 \text{ outcome with no 3's.}$$

At least two 3's?

$$1296 - 500 - 625 = \boxed{171} \text{ possible outcomes.}$$

Q3 (a) There are 8 cards, they are all aces with each ace sharing a suit with one other ace. Therefore, there are 2 hearts, 2 spades, 2 clubs and 2 diamonds.

No. of possible arrangements is $8!$, however we must remove duplicates.

$$\Rightarrow \frac{8!}{(2! \cdot 2! \cdot 2! \cdot 2!)} = \frac{40,320}{16} = \boxed{2,520} \text{ ways}$$

(b) Heart = H, Diamond = D, Club = C, Spade = S

outcome table

	H	D	C	S
H	HH	HD	HC	HS
D	DH	DD	DC	DS
C	CH	CD	CC	CS
S	SH	SD	SC	SS

Since order does not matter, there are only 6 distinct outcomes that are not 2 of the same suit nor reverse of another outcome.

Answer = $\boxed{6}$ distinct pairs

(c) From the outcome table above, there are 4 "good" pairs: HH, HD, DH, DD. Since order does not matter, $HD = DH$. Therefore, there are 3 ways to get two "good" cards.