## Push Down Automata

 $\#_a(w) = \text{number of } a$ 's in w.

$$L = \{w : \#_a(w) = \#_b(w)\}.$$

PDA:  $(\{q_0, q_1\}, \{a, b\}, \{a, b, Z_0\}, \delta, q_0, Z_0, \{q_1\}).$ 

$$\delta(q_0, a, Z_0) = (q_0, aZ_0)$$

$$\delta(q_0, b, Z_0) = (q_0, bZ_0)$$

$$\delta(q_0, a, b) = (q_0, \epsilon)$$

$$\delta(q_0, a, a) = (q_0, aa)$$

$$\delta(q_0, b, a) = (q_0, \epsilon)$$

$$\delta(q_0, b, b) = (q_0, bb)$$

$$\delta(q_0, \epsilon, Z_0) = (q_1, \epsilon)$$