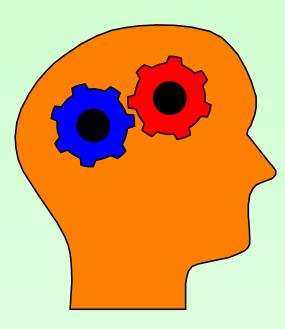


CS2104: Programming Languages Concepts

Lecture 3 : Data Types and Control Constructs



"Types, Constructs and Recursion and Type Classes"

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Topics

- Data Types
- Efficient Recursion
- Type Classes



Program = Data + Algorithm

Primitive and User-Defined Types

Primitive Types

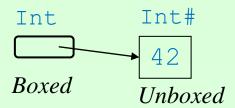
- Built-In Types of Languages
- Directly implemented in hardware (usually).
- Simpler types e.g. boolean, integer, float, char, string, arrays
- Important for performance
- May include Standard Libraries (extensible)
- Language without primitive type
 - Lambda Calculus
 - Use just functions!

Primitive Types (C Language)

- Built-In Types
 - int (bounded integer, e.g. int x = 42)
 - float (single precision floating, e.g. float r = 4.2)
 - double (double precision floating point)
 - char (e.g. char Letter; Letter = 'x';)
 - arrays (e.g. int arr[10];)
- Modifiers
 - short, long (e.g. short int, long double)
 - signed, unsigned
- void can be considered a type with a single value
- void* denotes pointer with unspecified type
- boolean implemented as integer (0 for false, non-0 for true)

Primitive Types (Haskell)

- Types are quite high level in Haskell and are essentially boxed types
 - data Bool = False | True
 -- e.g. b = True
 - type String = [Char]
 - data Int = GHC.Types.I# GHC.Prim.Int#
 - data Float = GHC.Types.F# GHC.Prim.Float#
 - data Double = GHC.Types.D# GHC.Prim.Double#
 - data Char = GHC.Types.C# GHC.Prim.Char#
- Unboxed types are built-in but seldom used, except when implementing the compiler using <code>-fglasgow-exts</code>



 Boxed/unboxed types is identifical to objects/primitive types in Java.

Boxed vs Unboxed Types

- Support Polymorphism
- Support Lazy Evaluation
- Programmer only sees boxed types
- Compiler writers or system programmer can optimize boxed type usages by converting them to the more efficient unboxed types.

User-Defined Types

- User can design their own types
- Support more complex data structures
- Examples:
 - Ordinal type
 - Record type
 - Pointer type
 - Tuple type
 - Union types
 - Algebraic Data type
 - Polymorphic/Generic type
 - Sum vs Product types

Ordinal Types

- An ordinal type is a finite *enumeration* of distinct values that can be associated with positive integers.
- An example in Ada is

```
type DAYS is (Mon, Tue, Wed, Thu, Fri, Sat, Sun)
if today>Fri then
   print "Hippie"
else
   print "Oh.."
```

• If values can occur in more than one ordinal type, it is referred to as *overloaded literals*, but may be difficult to determine which type such values belong to.

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Ordinal Types in Haskell

• Enumeration is a special case of algebraic data type.

```
data DaysObj = Mon | Tue | Wed | Thu | Fri | Sat | Sun
  deriving (Show, Enum, Eq)
```

• Enum class supports a range of useful methods:

```
class Enum a where
  succ :: a -> a
  pred :: a -> a
  toEnum :: Int -> a
  fromEnum :: a -> Int
...
```

• Show class supports printing:

```
class Show a where
  show :: a -> [Char]
```

• Eq class supports == and /=

Ordinal Types in Scala

Scala enumeration can be done through sealed case objects.

```
object DaysObj {
   sealed trait Days
   case object Mon extends Days
   case object Tue extends Days
   case object Wed extends Days
   case object Thu extends Days
   case object Fri extends Days
   case object Sat extends Days
   case object Sun extends Days
   val daysOfWeek = Seq(Mon, Tue, Wed, Thu, Fri, Sat, Sun)
}
```

- Sealed trait can be extended only in a single file.
- Compiler can thus emit warning if a match is non-exhaustive

Ordinal Types

• Non-exhaustive pattern. (e.g. Tue missing)

```
let weekend x = case x of {
    Mon -> False;
    Sat -> True;
    Sun -> True;
}
```

Avoid by using ghci -Wincomplete-patterns

Same compiler option in code:

```
{-# OPTIONS_GHC -fwarn-incomplete-patterns #-}
```

• Exhaustive Pattern.

```
let weekend x = case x of {
    Sat -> True;
    Sun -> True;
    _ -> False;
}
```

Each pattern contain only one case. No multi-case in Haskell

Pattern Matching: Haskell vs OCaml

Haskell allows guards but not OCaml

OCaml allows multiple cases but not Haskell

```
let weekend x = match x of {
    Mon -> False;
    Sat | Sun -> True;
}
```

No language is perfect!
 We just need to learn to live with them.

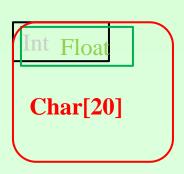
Union Types (in C)

- Union type is a type that may store different type of values within the same memory space but at different times/instances.
- We can define a union of many members but only one member can exists at any one time. Format:

```
union [union_tag] {
  (type id)+
} id+ ;
```

An example where the fields are overlaid.

```
union Data {
   int i;
   float f;
   char str[20]
};
```



Algebraic Data Type (in Haskell)

• A more systematic way to capture union types safely is to use algebraic data types which uses data constructor tags.

• With this, we can build objects of different values.

```
let v1 = I 3;;
let v2 = F 4.5;;
let v3 = S "CS2104";;
```

Algebraic Data Type (in Haskell)

• Generic printer.

```
let print_data v =
    case v of
    I a -> show a
    F v -> show v
    S v -> v
```

- Note pattern-matching is able to obtain type-safe values.
- Q: What is the type of above function?
- Q: What is the difference between **print_data** and **show**?

Tuple Types (Haskell)

- A special case of algebraic data type is the *tuple* type. This is polymorphic (where a, b, c are type variables) with a single data constructor (namely (,,)).
- An example is the triple:

```
data (,,) a b c = (,,) a b c
let stud1 = ("John","A1234567J",2013);;
```

• We can write *type synonym*, as follow:

```
type Student = (String, String, Int)
type Pair a b = (a, b)
type String = [Char]
```

Tuple Types (Haskell)

• Like algebraic data type, the component of tuples can be accessed using pattern-matching:

```
let (name,_,yr) = stud1;;

case stud1 of
  (name,_,yr) -> ... ;;
```

Type Synonym (Haskell)

• Type synonyms cannot be recursive.

```
type Node = (Int, Node);;
Error: Cycle in type synonym declarations
```

• Since type synonyms can be inlined. This restriction prevents infinite expansions.

Record Types

• Record is a collection of values of possibly different types with *field names*. In C, this is implemented as structures,

```
struct [structure_tag] {
    (type id)+
} id+ ;
```

• An example:

```
struct Student {
    char name[20];
    char matric[10];
    int year;
} s1, s2;
```

• Q: What is the difference between *records* and *tuples*?

Record Types (C)

• Can access the fields by the dot notation

```
Examples:s1.year or s2.matric
```

Access is efficiently done via offset calculation.

• Operations on records, e.g. assignment

```
s1 = s2;
```

Entire record is copied or passed as parameters.

Record Types (Haskell)

 Record type can also be supported in Haskell as an extension to algebraic data type

```
data Student = Student {
    name :: String;
    matrix :: String;
    year :: Int
} ;;
```

• Automatically derives name, matrix and year as access methods.

```
name :: Student -> String
matrix :: Student -> String
year :: Student -> Int
```

Record Types (Haskell)

• Pattern-matching with records.

- Automatically derives name, x and y as access methods
- Can use pattern-matching for records, e.g.

```
myfn :: X -> Int
myfn A = 50
myfn B{} = 200
myfn C{x=v} = v
```

Record Types (OCaml)

• Record type is a separate type in OCaml.

```
type student = {
   name : string;
   matrix : string;
   year : int;
   mutable status : ...;
} ;;
```

- Fields are *immutable*, by default. *Mutable* fields are also permitted.
- Use pattern-matching to access *selected* components

```
match s with
| {name = n; year = y} -> ...
```

• What are types of \mathbf{n} and \mathbf{y} ?

Pointer Type (in C)

- A pointer type is meant to capture the address of an object value. There is also a special value nil that is not a valid address.
- An example in C with pointer types are:

```
int count, init;
int *ptr;
int *ptr;
init 6

...
ptr = &init;
count = *ptr;
```

• The * operation will dereference a pointer type.

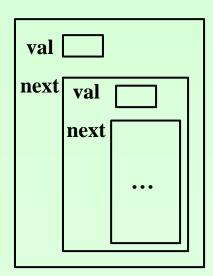
Pointer Type (in C)

- Pointer types are crucial for recursive data type.
- An example in C is:

inf list

• We cannot use below. Why?

```
struct node {
  int val;
  struct node next;
} inf_list;
```



Pointer Types (in Haskell?)

- No need for pointer types in Haskell.
- By default, each algebraic data type is already implemented as a pointer to a boxed value.
- Thus, recursive type is possible but can be infinite.

```
data Rnode = Rnode(Int,Rnode)

let list = Rnode(3,list)

list
3
```

Pointer Types (Haskell)

We may use a general Maybe type

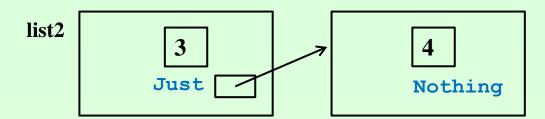
```
data Maybe a = Nothing | Just a
```

• Possibly finite data structure:

```
data RNode2 = RNode2 Int (Maybe RNode2)
    deriving Show
```

An Example

```
let list2 = RNode2 3 (Just (RNode2 4 Nothing))
```



Product vs Sum Types

- Fundamentally, there are two kinds of types.
- *Product* types that include tuples and records.
- *Sum* types that include ordinals and general algebraic data types.
- Product type is similar to conjunction a ^ b

```
type Pair a b = (a, b)
```

Sum type is similar to disjunction a v b.

```
type Either a b = Left a | Right b
```

Untyped Languages

• Untyped language essentially sums different types together, without using tags, e.g:

```
data Univ = Int | Float | .. | Array ..
```

• However, cannot distinguish between the sum type and its constituent types!

```
data Sum a b = a | b
let v1 = [3, "cs2104"];;
```

• Without constructor tags, there is *no type safety* that can be ensured at both compile and run-time.

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Type Classes

Type Classes and Overloading

- Parametric polymorphism works for all types. However, *ad-hoc polymorphism* works for a *class of types* and can systematically support overloading.
- For example, what is the type for (+) operator?

```
(+) :: a -> a -> a
(+) :: Int -> Int -> Int
(+) :: Float -> Float -> Float
```

• What about methods built from (+)?

```
double x = x + x
```

Solution is to use a type class for numerics!

```
(+) :: Num a => a -> a -> a double :: Num a => a -> a
```

Equality Class

Similar issue with equality. Though it looks like:

```
(==) :: a -> a -> Bool
```

- Equality can be tested for any data structure but not functions!
- Solution: define a type class that supports the equality method, as follows:

• Then: (==) :: Eq a => a -> a -> Bool

Members of Eq Type Class

The class is open and can be extended, as follows:

```
instance Eq Integer where
   x == y = x 'integerEq' y

instance Eq Float where
   x == y = x 'FloatEq' y
```

• Recursive type can also be handled but elements (or parameters) may need to be given *type qualifiers*.

More Members of Eq Type Class

• Similarly, we may use structural equality for List:

• One use of Eq class is:

• Q: define set as an instance of the Eq class.

Class Extension

 Haskell supports the notion of extending from some base type class.

```
class (Eq a) => Ord a where
  (<),(<=),(>=),(>) :: a -> a -> Bool
  max, min :: a -> a -> a
```

• This help reuse previous definitions from base class. Default definitions are also supported:

Class Extension

An example that use Ord class:.

```
quicksort :: (Ord a) => [a] -> [a]
```

Actual Ord class in the prelude is based on:

```
data Ordering = EQ | LT | GT
compare :: Ord a => a -> a -> Ordering
```

• Multiple inheritances supported which would allow more operations to be inherited from base classes.

```
class (Eq a, Show a) => C a where ...
```

Enumeration Class

• Class **Enum** supports *syntactic sugar* for arithmetic sequences:

```
class (Enum a)
  enumFromThen :: a -> a -> [a]
  fromEnum :: a -> Int
  toEnum :: Int -> a
```

• An example of arithmetic sequence :

```
[Red..Violet] → [Red,Green,Blue,Indigo,Violet]
```

• Q: Why is this [a..b] notation a syntactic sugar?

Show Class

• The Show class are for types that can be converted to character string.

```
class Show where
   show :: a -> String
   shows :: a -> String -> String
   show x = shows x ""
```

An example of its use:

• Possible problem: quadratic complexity.

Show Class

More efficient to use the accumulating method :

• Can avoid explicitly using *accumulating* parameter in the syntax via higher-order functions.

Read Class

• The converse problem of parsing data structure is handled by the Read class.

```
class Read a
  reads :: String -> [(a,String)]
```

• Empty answer denotes *failure* of parsing, while multiple answers denote *non-determinism*

Read Class

- Problems (i) no white space (ii) punctuation symbols?
- · Lexical analyser is provided in Prelude.

```
lex :: ReadS String
```

• Using lexer, we can build more robust parser:

Derived Instances

• Writing instances for standard type classes can be tedious, so Haskell allows automatic derivation.

```
data Tree a = Leaf a | Branch (Tree a) (Tree a)
    deriving (Eq, Ord)
```

• This automatically derives the following lexicographic ordering for ord class.

Direct Handling of Errors (in Haskell)

Use Maybe type.

```
myDiv2 :: Float -> Float -> Maybe Float
myDiv2 x 0 = Nothing
myDiv2 x y = Just (x / y)
```

Use Either type (opposite of Pair a b)

```
myDiv3 :: Float \rightarrow Float \rightarrow Either String Float myDiv3 x 0 = Left "Divison by zero" myDiv3 x y = Right (x / y)
```

Language Constructs and Recursion

Language Constructs

- Language constructs are features used to build programs
- Statements vs Expressions
 - Statement executed for their *effects*
 - Expression computes a result and may have effects too.
 - Statement a special case of expression
- Examples of Constructs
 - Blocks, Conditional, Sequences,
 - Exceptions, Loops, Calls

Language Construct (for C)

Statement

```
option
                             terminals
        <stmt> ::= if (<exp>) <stmt> [else <stmt>]
                       | {<stmt>}
                 | <type> <id>
                  \langle id \rangle = \langle exp \rangle
non-terminal
                  <stmt> ; <stmt>
                   loop-stmt | break | continue
                   switch (<exp>)
  alternatives
                   { case <exp> : <stmt>; ..;
                           default : <stmt>; }
                   return <exp>
                   <id>(<exp>*)
                                    repetition
```

Language Construct (for C)

Loop Statement

Expression

Language Construct (for Haskell)

• Expression-Oriented Constructs

• let declaration and case pattern contains binders that are immutable (bound values cannot be changed).

Functions

- Types for Functions
- Tupled vs Curried Functions
- Recursion and Tail-Recursion
- Naïve vs Efficient Functions

Types for Functions

- Every value has a type, including functions
- Some examples:

```
(\ x -> x * x) has type Num a => a -> a
sum has type Num a => [a] -> a
length has type [a] -> Int
fst has type (a,b) -> a
```

• Why didn't length method use Integer? Why did sum method use the Num class?

Tupled vs Curried Functions

• Curried function takes one argument at a time, by returning a function that takes the next argument.

```
{- addA::Int->Int->Int -}
let addA x y = x + y
```

• Tupled function takes all its arguments as a tuple/product.

```
{- \text{ addB::}(Int,int)->Int -}
let addB (x,y) = x + y
```

• Curried and tupled function are isomorphic.

```
addB \equiv \langle (x,y) -\rangle addA x y addA \equiv \langle x -\rangle \langle y -\rangle addB(x,y)
```

Partially Applied Functions

- Partially applied functions are those taking only some of their parameters.
- They result in functions that would take remaining arguments.

```
-- inc1 : Integer -> Integer
let inc1 = addA 1
```

• To implement partial application for tupled method, you would need lambda abstraction to mimic it.

```
-- inc2 : Integer -> Integer let inc2 = \ y -> addB (2,y)
```

Topics

- Data Types
- Binders
- Efficient Recursion
- Type Classes

List Append

- (++) joins two lists together.
- Its has type [a] -> [a] -> [a]

```
xs ++ ys =
  case xs of
  [] -> ys
  x:xs -> x:(xs ++ ys)
```

• Q : Guess its time-complexity?

List Reverse

- reverse would reverse the content of its given list, so that the last element become first and vice-versa
- An easy implementation is:

```
reverse xs =
  case xs of
  [] -> []
  x:xs -> (reverse xs) ++ [x]
```

• Q: Is this efficient? Guess its time-complexity?

List Reverse (efficient and tail-recursive)

• A linear-time version that is also tail-recursive is shown below:

```
revit xs =
  let aux xs acc =
    case xs of
    [] -> acc
    x:xs -> aux xs (x:acc)
  in aux xs []
```

- It uses an inner recursive function which kept a list of reversed elements so far in the acc parameter.
- Q : How is its time-complexity? linear-time?

Tail-Recursion

• A function is tail-recursive if the recursive call is always the last operation in the recursive invocations.

```
let aux xs acc =
  case xs of
  [] -> acc
  x::xs -> aux xs (x::acc) in ...
  last call in the recursive branch
```

- Tail-recursion is equivalent to Loop.
- Last recursive call can be compiled into a jump to the beginning of recursive method.

Inefficiency of Naïve Fibonacci

 An often-cited example of inefficiency of recursion is the fibonacci function.

```
let fib n =
if n \le 1 then 1
else (fib(n-1))+(fib(n-2))
```

• However, this is an algorithmic problem (with many repeated calls) rather than the problem of recursion per se.

Tupled Fibonacci

• We can easily write an efficient version of fibonacci by using a recursive helper that returns two fibonacci values:

```
(fib n, fib (n-1))
```

• The efficient fibonacci is now implemented as:

```
let fib2 n =
  let aux n =
      if n<=0 then (1,0)
      else let (a,b)=aux(n-1)
            in (a+b,a)
  in fst(aux n)</pre>
```

• This method eliminates the redundant calls and can compute in linear-time. However, it is not *tail-recursive*.

Tail-Recursive Fibonacci

• We can easily implement a tail-recursive fibonacci function by adding two extra parameters to the recursive method, as follows:

```
let fib3 n =
   let aux n a b =
        if n<=0 then a
        else aux (n-1) (a+b) a
   in aux n 1 0</pre>
```

- This is equivalent to most loop-based implementation of fibonacci.
- Q : You now have an efficient *linear-time recursive* functions. How about logarithmic-time fibonacci?