## **B** INTERPRETABILITY OF COMPONENTS

If each component has a specific pattern rather than a mixture of multiple patterns, the component is easy to distinguishable from the others, making the model more interpretable. In our experiment, we use a DBLP dataset to evaluate latent patterns based on labels, consisting of (author, paper, conference) tuples. Each entity of modes is labeled according to the area of study (DM, AI, DB, IR), which is also used in Section 4.3.1. To evaluate this interpretability, we leverages two metrics:

- Entropy of the top-K label distribution per component. This metric evaluates whether each component per mode represents a distinct latent pattern. A lower entropy indicates less uncertainty about the labels in each column, signifying a higher occurrence of certain labels and making each component easily distinguishable.
- **Distance between the top-***K* **label distributions of the** *r***th components.** This metric evaluates whether how well the *r*th components cluster together based on specific labels. The lower the distance is, the better components clusters.

To find the top-K entities for each column of each factor matrix, we sort the factor values in descending order. Then, we create a top-K label distribution using the labels of the top-K entities. We will explain in detail how to measure the entropy and distance in the following paragraph.

 $L = \{L_1, \dots, L_m, \dots L_M\}$  is a set of labels. If this label is binary, then M = 2 and |L| = 2.  $L^{(n)} = \{(i_n, l_{i_n}) | 1 \le i_n \le I_n, l_{i_n} \in L\}$  is a set of indices  $i_n$  paired with their corresponding labels  $l_{i_n}$ , for  $n = 1, \dots, N$ . The average entropy of top-K label distribution is defined as follows.

$$AE = \frac{1}{N \times R} \sum_{n=1}^{N} \sum_{r=1}^{R} H(\mathbf{p}_{r}^{(n)}) \text{ where } H(\mathbf{p}_{r}^{(n)}) = -\sum_{m=1}^{M} \mathbf{p}_{r}^{(n)}(m) \log \mathbf{p}_{r}^{(n)}(m). \tag{11}$$

Here,  $\mathbf{p}_r^{(n)} \in \mathbb{R}^{M \times 1}$  denotes the top-K label distribution for rth column in the nth factor matrix, which is defined as follows.

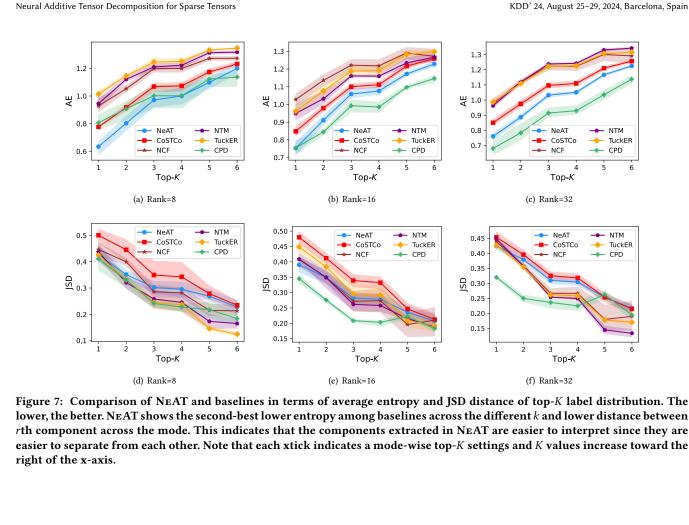
$$\mathbf{p}_r^{(n)} = \frac{1}{K} [\mathbf{p}_r^{(n)}(1) \cdots \mathbf{p}_r^{(n)}(M)], \tag{12}$$

where  $\mathbf{p}_r^{(n)}(m) = |\{i_n \in I_n'| l_{i_n} = L_m\}|$  indicates the number of indices having the label  $L_m$  and  $I_n'$  indicates a set of indices of top-k values in  $\mathbf{a}_r^{(n)}$ . To measure the distance between two top-K label distributions across the different modes, we use Jenson-Shannon divergence, which is defined as follows. For n and n' ( $n \neq n'$ ),

$$JSD(\mathbf{p}_r^{(n)}||\mathbf{p}_r^{(n')}) = \frac{1}{2}D(\mathbf{p}_r^{(n)}||Q) + \frac{1}{2}D(\mathbf{p}_r^{(n')}||Q), \tag{13}$$

where  $Q = \frac{1}{2}(\mathbf{p}_r^{(n)} + \mathbf{p}_r^{(n')}).$ 

We varies K according to the size of each mode and use six settings of top-K such as [5, 10, 3], [15, 30, 3], [30, 50, 5], [30, 100, 5], [50, 100, 10], and [100, 1000, 10]. Figure 7 demonstrates the comparison of NeAT with the baselines in terms of average entropy and distance of top-K label distribution over ranks 8 to 32. NeAT shows the second-best average entropy, and shows a lower distance compared to CoSTCo, which shows the best average entropy among neural tensor models. This indicates that in NeAT, like CPD, each component is well separable, not mixed into multiple patterns, and components across the different modes are well clustered with respect to a specific pattern. Baselines such as NTM, NCF and TuckER showing higher entropy and lower distance indicates that those distributions in each component are not separable but the differences between labels in the distributions are low.



lower, the better. NEAT shows the second-best lower entropy among baselines across the different k and lower distance between rth component across the mode. This indicates that the components extracted in NEAT are easier to interpret since they are easier to separate from each other. Note that each xtick indicates a mode-wise top-K settings and K values increase toward the