550.400: Mathematical Modeling and Consulting

Lecture Notes

Instructor:

Dr. N. H. Lee

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	Hello World	
Hello World.		
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Adobe Connect

https://connect.johnshopkins.edu/meeting550400/

Announcement

• HW SET 1 due on Monday Oct 8
• Include your drawing in HW SET 1 as a figure
• Marked Work Statement is returned on Monday Oct 8
• Check the blackboard frequently for updates
• Ask non-sensitive questions on Blackboard Discussion Forum FAQ

Vim EAC

Vim FAQ

In Vim, how do you

- start, save, quit Vim?
- show numbers on the side?
- change the color theme?
- move around?
- spell check?
- find particular words?
- save typing while coding these LATEX commands?
- install plugins?

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FAQ

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Vim FAQ

Vim is a highly customizable text editor

- 1. $\triangle T_E X$, R, C/C++, Java, Python, Git and etc.
- 2. Regular expression, syntax coloring, auto-completion
- 3. <ESC>-mode
 - :-mode, aka., the last line mode
 - i-mode, aka., the insert mode

Vim FAQ

How do I disable/enable this?

number column :set number and :set nonumber

colorscheme :colorscheme <TAB>

tetris :source /.vim/tetris.vim and te

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FAQ

Vim FAQ

- Download & Install GVim or MacVim
- Download & Install tetris.vim
- Download & Install minibufexpl.vim
- Download & Install Gundo
- Download & Install Vim-LaTeX

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Vim FAQ motion moves the cursor, or define the range for an operator vi/vim lesson 1 - basic editing Esc h j k l are vi/vim cursor keys – use them as they are much closer than regular cursor keys! u to undo the last action – traditional vi has a single level, while vin pports unlimited undo (CTRL - R to redo) 0 jumps directly to the beginning of the line, 8 to the end, and △ to the first non-blank Use to enter insert mode, cursor turns from a block into a vertical line, and you can type in text. Use Esc to return to normal mode. Use x to delete the current character, or X to delete the one to Use wbe to move along 'words'. A 'word' is a sequence of all alphanumeric or punctuation signs: quux(fool barl baz); Use A to go insert text at the end of the line (wherever you are Use WBE to move along WORDs. A 'WORD' is a sequence of any non-blank characters: quux (foo, bar, baz); (Note: insert mode is actually very similar to a regular editor, you can use Use R to enter insert mode with an overstrike cursor, which cursor/navigation keys, backspace, delete...) types over existing characters. : w and press enter to save, : q and enter to quit. For the rest of the tutorial & a full cheat sheet, go to www.viemu.com - home of ViEmu, vi/vim emulation for Microsoft Visual Studie

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FAQ

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FAQ

How do you add a figure in LATEX ?

\begin{figure}
 \caption{<+caption text+>}
 \begin{center}
 \includegraphics[width=<+number+>\textwidth]{<+filename+>}
 \end{center}
\end{figure}

Here, $<+\ldots+>$ denotes a thing that you need to fill in.

But you will need this in the preamble part of your LATEX:

\usepackage{graphicx}

To save yourself from unnecessary glitches, insert png, jpeg, pdf files only.

Cross Sectional Study Vs. Longitudinal Study

MIDNIGHT

THAT FOR SIGNAL CONDITIONS

BANITATION CONDITIONS

SANITATION CONDITIONS

SANITATION CONDITIONS

SANITATION CONDITIONS

STREET CONDITIONS

SIDDWALA CONDITIONS

ROCENTS

There were 34,522 complaints called in to 311 between September 8 and September 15, 2010. Here are the most common, plotted by time of day.

Can Riots Be Predicted?

A Tunisian protester holds a baguette while taking to riot police in January 2011



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LATEX FAQ

How can I code a beamer?

```
\documentclass[hyperref={colorlinks=false},handout,10pt]{beamer}
\usetheme{Singapore}
\usecolortheme{lily}
\usefonttheme[onlymath]{serif} % What does this do?
```

OR

```
\documentclass[hyperref={colorlinks=false},handout,10pt]{beamer}
\usetheme{Berlin}
\usecolortheme{wolverine}
\usefonttheme[onlymath]{serif} % What does this do?
```

For a more complete array of themes, go to:

http://www.hartwork.org/beamer-theme-matrix/

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FAQ

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LATEX FAQ

How can I code a beamer?: a single side with no block

```
\begin{document}
  \begin{frame} # one frame per one slide
  \frametitle{hello world} # optional but you want one
  \begin{itemize}
  \item apple
  \item orange
  \end{itemize}
  \end{frame}
\end{document}
```

How can I code a beamer?: a single side with one block

FAC

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LATEX FAQ

How can I code a beamer?: two slides

LATEX FAQ

How can I code a beamer?: a single frame with two columns

```
\begin{document}
        \begin{frame} # one frame per one slide
            \frametitle{hi world} # optional but you want one
            \begin{columns}
                \begin{column}{0.5\textwidth}
                    \begin{itemize}
                        \item Alice!
                    \end{itemize}
                \end{column}
                \begin{column}{0.5\textwidth}
                    \begin{block}{hey world}
                        Bob!
                    \end{block}
                \end{column}
            \end{columns}
        \end{frame}
\end{document}
```

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LATEX FAQ

SO, how to put a code in the slide? and it looks like codes?

```
\begin{lstlisting}
require(tikzDevice)
x = rnorm(100)
plot.ts(x)
dev.off()
\end{lstlisting}
```

require(tikzDevice)
x = rnorm(100)
plot.ts(x)
dev.off()

LATEX FAQ

How can I code a beamer?: with a table of contents

```
\begin{frame}
    \frametitle{Outline}
    \tableofcontents
\end{frame}

\section{Hello World} # optional
    \subsection{hello world} # optional
    \begin{frame} # one frame per one slide
        \frametitle{hi world} # optional but you want one
    \end{frame}

\section{Hello New World}
    \begin{frame} # one frame per one slide
    \frametitle{hi new world} # optional but you want one
    \end{frame}
\end{frame}
\end{document}
```

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FAQ

FAQ

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LATEX FAQ

But, this requires the following in the preamble portion of your tex file:

```
\usepackage{listings}
\lstset{
basicstyle=\footnotesize\ttfamily,
numbers=left,
frame=bottomline,
framextopmargin=50pt,
}
```

You will also need fragile option for your frame:

```
\begin{frame}[fragile]
   \frametitle{hello world}
   \begin{lstlisting}
x = rnorm(100)
   \end{lstlisting}
\end{frame}
```

FAQ

LATEX FAO

Where to get more help:

http://en.wikibooks.org/wiki/LaTeX/Presentations

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R FAQ

system(`ls -ld .*') system(`cat .Rprofile') system(`cat .bashrc') system(`cat .gitignore') system(`cat .vimrc')

- .xxx files are hidden
- Is -Id .* show the hidden files
- .Rprofile set up your R behavior
- .bashrc set up your bash behavior
- .gitignore set up your git behavior
- .vimrc set up you vim behavior
- these files are equivalent to Preference part of your GUI software

R FAQ

```
for(itr in 1:8) {
    stanzaname = paste("stanza",itr,sep="")
    gitaddress = paste("git://github.com/nhlee/550400.",
                             stanzaname,".git",sep="")
    bashcommand = paste("git remote add ",
                             stanzaname, " ", gitaddress, sep="")
    system(bashcommand)
```

- 1:8 creates a vector that ...
- X = 1 assigns 1 to X
- X <- 1 also assigns 1 to X
- lots of things are done through function
- paste and system are functions that ...
- functions has none or more arguments
- arguments are implicitly ordered but the order can be overridden

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FAQ

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R FAQ

How to do software documentation (via R)

```
myfun <- function(x) {x^2}</pre>
package.skeleton(name='MYPAC',
                list='myfun',
                path='~/')
#Do the documentation
system('R CMD check ~/MYPAC')
system('R CMD build ~/MYPAC')
system('R CMD install MYPAC')
```

Assessing Causality (WMA, 527)

• Consistency of association:

The association is observed in several different populations using different types of study design.

Strength of association

A bigger difference in outcomes between cases with and without the purported causal factor indicates a stronger association.

Temporal relationship

The cause preceded the effect. A correlation between two variables measured at the same time gives weaker evidence than one measuring the relationship between changes in the supposed cause and subsequent responses in the outcome.

Mechanism

There is a plausible means by which the alleged cause could affect the outcome.

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Spurious Causality II

How about when there is no context goes with the variables? That is, you just have numbers.

Numerical simulation: presence of confounding variable

```
x \leftarrow y \leftarrow mu \leftarrow rep(0,1000);
for(i in 2:1000)
     mu[i] <- mu[i-1] + rnorm(1);
x <- mu + rnorm(1000);
y <- mu + rnorm(1000);
```

Numerical simulation: presence of "stochastic trend"

```
set.seed(10); x <- rnorm(100); y <- rnorm(100);
for(i in 2:100) {
     x[i] \leftarrow x[i-1] + rnorm(1);
    y[i] \leftarrow y[i-1] + rnorm(1);
}
```

Spurious Causality I

Is there a plausible means by which the alleged cause could affect the outcome?

Chocholate Consumption Vs. Electricity Production

```
cbe.loc<-'http://www.massey.ac.nz/~pscowper/ts/cbe.dat';</pre>
cbe <- read.table(cbe.loc,header=T);</pre>
plot(cbe[,1],cbe[,3]);
```

Euro & UK Pound Exchange Rate against US Dollar

```
xrate.loc <-'http://www.massey.ac.nz/~pscowper/ts/us_rates.dat';</pre>
xrates <- read.table(xrate.loc,header=T);</pre>
plot(xrates$UK,xrates$EU,pch=4);
```

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Spurious Causality III

Working with a model under "stochastic trend" is a tricky husiness.

A procedure of testing for confounding stochastic trend

```
require(tseries);
adf.test(x)$p.value; #this tests for stochastic trend in x
adf.test(y)$p.value; #so does this but in y
po.test(cbind(x,y)); #this tests for confounding factors in x and y
```

Are two exchange-rates confounded? "co-integrated"?

```
pp.test(xrates$UK)
pp.test(xrates$EU)
po.test(cbind(xrates$UK,xrates$EU))
ukeu.lm <- lm(xrates$UK ~ xrates$EU)
ukeu.res <- resid(ukeu.lm)
```

Apropos

Two non-stationary time series X_t and Y_t are *cointegrated* if some linear combination $aX_t + bY_t$, with a and b constant, is a stationary series.

- Have you heard of p-value?
- How about null and alternative hypotheses?
- Again, what do you mean by "stochastic trend"?
- What do you mean by "stationary processes"?

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Time Series Model

Is there a plausible means by which the alleged cause could affect the outcome?

A time series model is a descriptive model

- its primary goal is to describe quantitative relationship between variables,
- it need not provide the underlying mechanism/context,
- it need not be a generative model.

Hypothesis Test

adf.test & pp.test

- the null is that the time series has the stochastic trend
- the alt is that the time series is stationary

po.test

- the null is that two non-stationary series are not co-integrated
- the alt is that two non-stationary series are co-integrated

p-value

- a number between 0 and 1
- near zero means . . .
- near one mean . . .

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FAG

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Time Series Model

A sequence $\{X_i: i=0,\pm 1,\pm 2,\ldots\}$ of random variables taking values in $\mathbb R$ is said to be a "white noise" sequence if

- X_i and X_j are statistically independent,
- X_i and X_i are statistically identical,
- its mean is zero and its variance is posistive.

A white noise sequence is normal/Gaussian if its common likelihood function (aka. density) is normal/Gaussian, i.e.,

$$P(x \le X_i \le x + dx) \approx f(x)dx$$

where

$$f(x) = \frac{1}{\sqrt{2\sigma}} \exp\left(-\frac{x^2}{2\sigma^2}\right).$$

Time Series Model

AR(p) model:

- AR stands for autoregressive
- in words, the current value is a function of past values plus some random noise
- for p = 1, 2, ...,

$$X(t) = \beta_0 + \beta_1 X_{t-1} + \dots + \beta_p X_{t-p} + \varepsilon_t$$

• for example, X_t and Y_t defined below are AR(1) models,

$$X_t = X_{t-1} + \varepsilon_t,$$

$$Y_t = 0.5Y_{t-1} + w_t$$

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Time Series Model

VAR(p) model:

- VAR(p) stands for *vector* autoregressive
- for example,

$$X_t = 0.5X_{t-1} + Y_{t-1} + \varepsilon_t,$$

$$Y_t = X_{t-1} + 0.5Y_{t-1} + w_t.$$

• more generally, for $p \times p$ matrix A,

$$X_t = AX_{t-1} + W_t.$$

Mechanism of Causation?

The cause preceded the effect. A correlation between two variables measured at the same time gives weaker evidence than one measuring the relationship between changes in the supposed cause and subsequent responses in the outcome.

Granger Causality: If $\{Y_t\}$ does not improve the forecasting performance of $\{Z_t\}$, then $\{Y_t\}$ does not Granger cause $\{Z_t\}$.

Exogeneity: $\{Z_t\}$ is exogenous (to $\{Y_t\}$ if it is not affected by the contemporaneous value of $\{Y_t\}$

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Time Series Model

Example on Page 222

```
require(tseries);
data(USeconomic);
myts = cbind(GNP,M1);
plot(myts);
fittedmodel = ar(myts, order.max=1, method ='ols', dmean = F, intercept = T);
print(fittedmodel);
```

- USeconomic contains a quarterly US economic series from 1954 till 1987
- GNP denotes the gross national product
- M1 denotes "real money", which means income adjusted by inflation

Time Series Model

Example on Page 224

```
require(vars);
fittedmodel <- VAR(myts,p=1,type='trend');
print(fittedmodel);</pre>
```

- Yet another way to fit a VAR(1) model in R
- VAR function from vars package is somewhat general than ar function in that you can have linear term, i.e., for type='both', the RHS of the VAR(1) formula contains

$$\alpha_0 + \alpha_1 t$$