Constructing a PCA Index | Replicating S&P 500

```
[18]: import os
      import time
      import datetime
      import numpy as np
      import pandas as pd
      import scipy.stats as scs
      from pylab import plt, mpl
      from sklearn.decomposition import KernelPCA, PCA
      from sklearn.preprocessing import StandardScaler
      plt.style.use('seaborn-v0_8')
      mpl.rcParams['savefig.dpi'] = 300
      mpl.rcParams['font.family'] = 'serif'
      pd.set option('mode.chained assignment', None)
      pd.set option('display.float format', '{:.4f}'.format)
      np.set printoptions(suppress=True, precision=4)
      os.environ['PYTHONHASHSEED'] = '0'
```

In this section, we present an illustrative example showcasing the application of Principal Component Analysis (PCA) in a specific context. We gather data from S&P 500 Index, all the individual stocks comprising the index. Subsequently, we employ PCA to extract the principal components, which we utilize to construct a composite index.

Data

Pull S&P 500 data for 2020

```
[19]:

A AAL AAPL ABBV ABT ACGL ACN ADBE

Date

2020-01-02 83.9481 28.9829 73.2490 75.6563 81.7302 43.4000 199.2254 334.4300

2020-01-03 82.6002 27.5482 72.5369 74.9382 80.7338 43.3500 198.8936 331.8100

2020-01-06 82.8444 27.2194 73.1149 75.5296 81.1568 43.5200 197.5948 333.7100
```

```
2020-01-07 83.0983 27.1198 72.7710 75.0987 80.7056 43.1600 193.3287 333.3900 2020-01-08 83.9188 27.7375 73.9416 75.6310 81.0346 42.7300 193.7080 337.8700
```

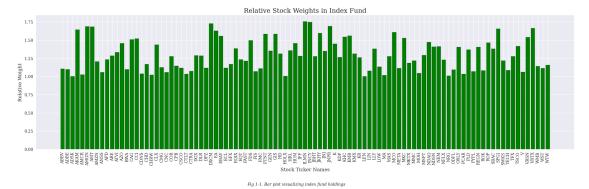
Implementing Principal Component Analysis (PCA)

Typically, Principal Component Analysis (PCA) is applied to standardized normalized datasets.

```
Explained Variance of Each Component:
[0.5454 0.2713 0.0544 0.0325 0.0192 0.0125 0.0089 0.0083 0.0053 0.0042]
```

Create Index Fund of S&P500 using principle component weights

Bar plot visualizing index fund holdings



Compare S&P 500 to PCA Index Fund

Figure 1-2 illustrates the replication of the SP500 index by the PCA index.

```
plt.figtext(0.5, 0.01, 'Fig 1-2. Replicating the S&P 500 Index using the PCA

→Index', style='italic', ha='center')

plt.show()
```



Compare the returns of the two investment strategies over a one-year period

Actual percentage return of the S&P500

Percentage return of S&P500 0.193800234486313

Actual percentage return of the PCA Index

Percentage return of PCA Index 0.23832183783101527

The outcome achieved through the implementation of the PCA index investment strategy is remarkably impressive, considering the straightforward nature of the approach.