

## Exercise Sheet 8

Ex 1

(A) = Quicksort  $n$  numbers

(B) = put  $n$  numbers in a empty hashtable

Operations of A and B worst case

(A): The worst case is, when the pivot doesn't split the list (e.g. it is the smallest or highest element in the list) for all iterations.

On each recursion the length of the recursion  $n$  is reduced by one.

There are  $n-1$  recursions with an average length of  $n/2$

$$\Rightarrow A = O(n^2)$$

(B): The worst case is, when all elements are mapped in the same bucket

The bucket selection has costs  $O(1)$

The costs of appending on a linked list is  $O(1)$

$$\Rightarrow B = O(1)$$

Block operations

(A): The memory access is random. Two following write operations are not necessary in a close memory address. The cache has to fetch his content more often

(B): The memory access is in a more predictable way. If an address is read, it's very likely that the addresses close by are read as well. This should be cache efficient.

The mapping should be far more efficient, because the difference of complexity is dominating over the cache efficiency.



We can argue, that for small  $n$ , the impact of cache efficiency could have an impact.

Ex. 4 Quicksort is somewhat quadratic and mapping close to linear (but increasing at the end)  
The increase at the End is caused by the cache efficiency, which begins to have an impact with increasing data size  $\rightarrow$  more cache operations required