

Deepanshu Bansal(150219)

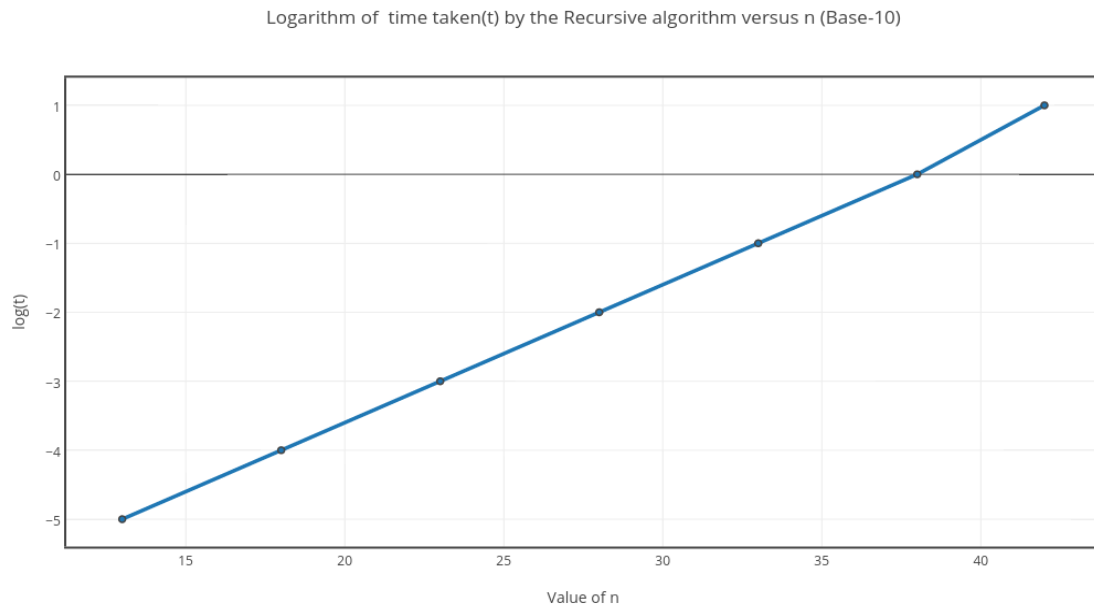
Part-1

For $a=2$, $b=3$, $c=5$, $m = 100$ we get these values for n corresponding to t .

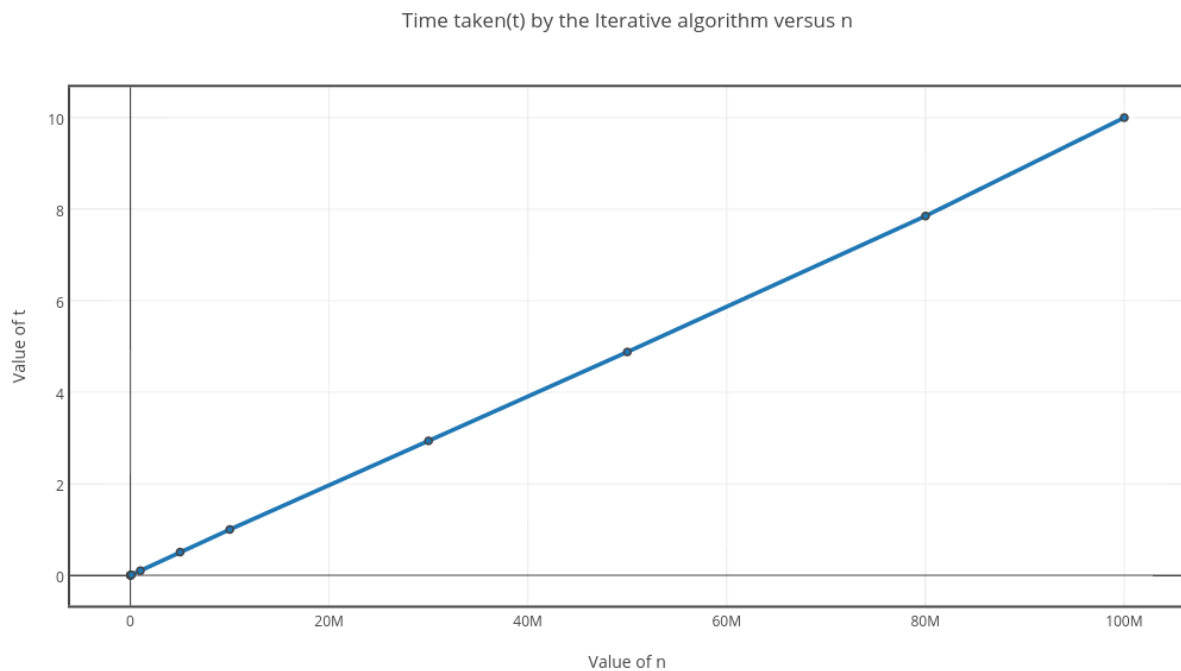
Time taken to compute $G(n) \bmod m$ (in seconds)	10^{-5}	10^{-4}	10^{-3}	10^{-2}	10^{-1}	1	10
Max value of n for recursive algorithm	13	18	23	28	33	38	42
Max value of n for iterative algorithm	92	745	9100	97000 ($\sim 10^5$)	999001 ($\sim 10^6$)	10000000 ($\sim 10^7$)	100000000 ($\sim 10^8$)
Max value of n for matrix method	10	2500000 ($\sim 10^6$)	$>10^{18}$	$>10^{18}$	$>10^{18}$	$>10^{18}$	$>10^{18}$

Part-2

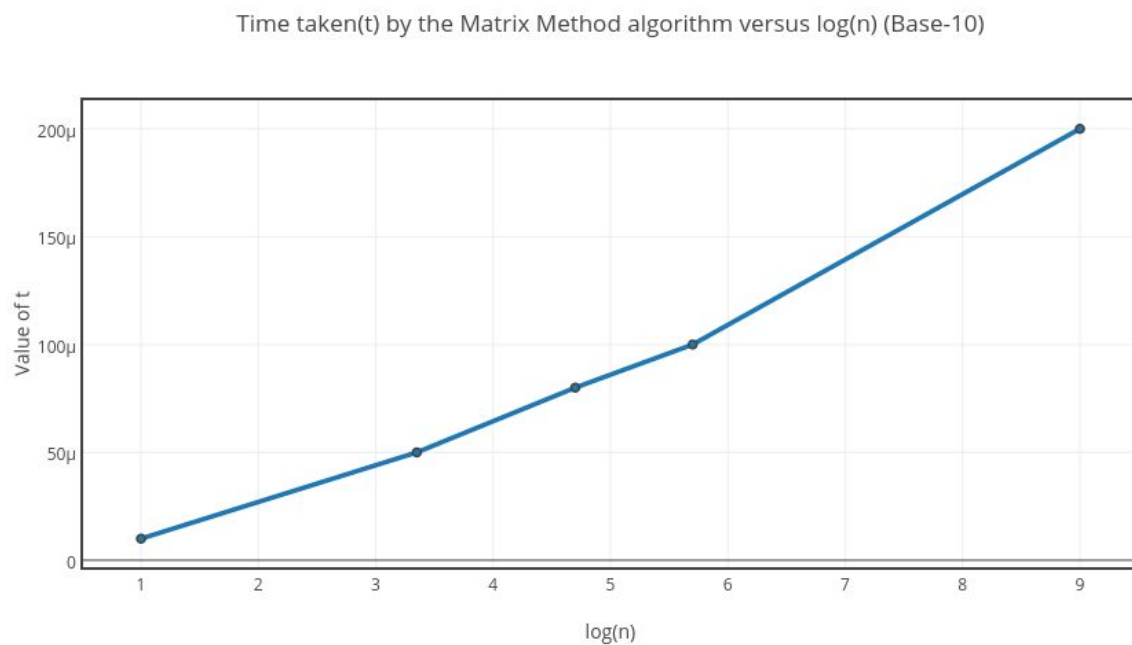
Plot of the logarithm of the time taken by the recursive algorithm versus n



Plot the time taken by the iterative algorithm versus n



Plot the time taken by the matrix method algorithm versus the logarithm of n



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Part-3

Since for the **Recursive** algorithm time complexity is **$O(2^n)$** hence

$$T = k \cdot 2^n$$

$$\log(T) = \log(k) + n \cdot \log(2)$$

Hence $\log(t)$ vs n is a linear equation of type **$y = mx + c$** .

So graph of **$\log(t)$ vs n** is a **straight line**

Time complexity for **Iterative** algorithm is **$O(n)$** hence

$$T = k \cdot n$$

Hence t vs n is a linear equation of type **$y = mx + c$** .

So graph of **t vs n** is a **straight line**

Time complexity for **Matrix method** algorithm is **$O(\log n)$**

$$T = k \cdot \log n$$

Hence t vs $\log(n)$ is a linear equation of type **$y = mx + c$** .

So graph of **t vs $\log(n)$** is a **straight line**

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