```
1~\% Generates a file 'calculatePropensities.m' that will contain a function able to calculate arksigma
the necessary propensities for that system.
 2 function GeneratePropensityCalculatorFile(SBMLModel, VHolder)
 4 % determine number of reactions and species present in the model
 5 numReactions = length(SBMLModel.reaction);
 6 numSpecies = length(SBMLModel.species);
 7
 8 [cNames, cValues] = GetParameters(SBMLModel);
 9
10 % matricies to hold propensity values
11 A = zeros(numReactions,1);
12
13 V = VHolder.V;
14 vNumOfReactant = VHolder.vNumOfReactant;
15 vReactant = VHolder.vReactant;
16 vDimerMap = VHolder.vDimerMap;
17
18 fid = fopen('calculatePropensities.m','w');
19 fprintf(fid, 'function A = calculatePropensities(X)\n\n');
20
21 for i = 1:numReactions
22
23
       % set initially to that reaction's parameter
24
       format long;
25
       fprintf(fid, 'A(%d) = (%d)', i, cValues(i));
26
       \% multiply current value by each ractant's value if applicable, and account for m{arepsilon}
27
dimerisation reactions
       for k = 1:(vNumOfReactant(i));
28
29
30
           curSpeciesIndex = vReactant(i,k);
31
32
           fprintf(fid,'*X(%d)', curSpeciesIndex);
33
           % determine is reactant is part of a dimerisation reaction using dimerisation map,\checkmark
34
then alter propensity accordingly
35
           dimer_number = vDimerMap(curSpeciesIndex, i);
36
           if dimer_number > 1
37
               count = 1;
               while (count < dimer_number)</pre>
38
39
                    fprintf(fid,'*(X(%d)-%d)', curSpeciesIndex, count);
40
                    count = count + 1;
41
               end
42
43
               fprintf(fid,'/%d', factorial(dimer_number) );
44
           end
45
       end
46
47
       fprintf(fid, ';\n', i, cValues(i) );
48 end
49
50 fprintf(fid,'\nend',numReactions);
51
52 fclose(fid);
53
54 end
```

```
1 function totalsIndecies = GenerateSpecifiedTotalsCalculatorFile(SBMLModel)
 3 numReactions = length(SBMLModel.reaction);
 4 numSpecies = length(SBMLModel.species);
 6 [speNames, speValues] = GetSpecies(SBMLModel);
 7
 8 totalsIndecies = zeros(numSpecies,1);
10 fid = fopen('calculateSpecifiedTotals.m','w');
11 fprintf(fid, 'function X = calculateSpecifiedTotals(X)\n\n');
12
13 count = 0;
14 for i = 1:length(SBMLModel.rule)
15
       curRule = SBMLModel.rule(i);
16
17
       for j = 1:length( speNames )
           if strcmp( speNames(j), curRule.variable )
18
19
20
               totalsIndecies(count+1) = j;
21
               count = count + 1;
22
               fprintf(fid, 'X(%d) = 0', j);
23
24
               % token string array
25
               ruleToks = strsplit( curRule.formula , '+');
26
27
               for l = 1:length( ruleToks )
                   for m = 1:length(speNames)
28
29
                        if strcmp( speNames(m), ruleToks(l) )
30
                            fprintf(fid, ' + X(%d)', m);
                       end
31
32
                   end
33
               end
34
35
               fprintf(fid, ';\n', m);
36
37
               break;
38
           end
39
       end
40 end
41
42 fprintf(fid, '\nend', numReactions);
43
44 fclose(fid);
45
46 totalsIndecies = totalsIndecies(1:count);
47
48 end
```

```
1 function speConstIndecies = GetConstantSpeciesIndecies(SBMLModel)
3 numSpecies = length(SBMLModel.species);
5 speConstIndecies = zeros(numSpecies,1);
6
7 count = 0;
8 for i = 1:numSpecies
      if SBMLModel.species(i).constant
           speConstIndecies(count + 1) = i;
10
           count = count + 1;
11
12
      end
13 end
14
15 speConstIndecies = speConstIndecies(1:count,1);
16
17 end
```

```
1 function [cNames, cValues] = GetParameters(SBMLModel)
 3 numReactions = length(SBMLModel.reaction);
 5 % get all parameter names, values
 6 [allCNames, allCValues] = GetAllParameters(SBMLModel);
 8 % create matricies to hold parameter names, values
 9 cValues = zeros(numReactions,1);
10 cNames = cell(numReactions,1);
12 % get parameters for each individual reaction as they may not be in order
13 for i = 1:numReactions
14
       % attempt to get parameters from local rection context
15
16
       [cNamesTemp,cValuesTemp] = GetParameterFromReaction(SBMLModel.reaction(i));
17
       % if parameter values are NOT embedded in each local reaction context (return values willarksim
18
be NULL)
19
       if ( length(cNamesTemp) == 0 ) && ( length(cValuesTemp) == 0 )
20
21
           % declare parameter found flag, get string from reaction formula field, tokenize it byoldsymbol{arepsilon}
operator
22
           done = 0;
23
           kinLawString = SBMLModel.reaction(i).kineticLaw.formula;
24
           kinLawStringToks = strsplit( kinLawString ,'*');
25
           % searches for each token in the list of all parameters in the model, assigns those ∠
26
values to the correct reaction if found
           for j = 1:length(kinLawStringToks)
27
               curTok = kinLawStringToks(j);
28
29
               for k = 1:length(allCNames);
30
                    if strcmp( allCNames{k} , curTok )
31
                        cNames{i} = allCNames{k};
32
                        cValues(i) = allCValues(k);
33
                        done = 1;
34
                        break;
35
                   end
36
                   if done == 1
37
38
                        break:
39
                   end
40
               end
41
               if done == 1
42
43
                   break;
44
               end
45
46
       % if parameters were embedded in the local reaction contexts, assign them
47
       else
           cNames(i) = cNamesTemp;
48
49
           cValues(i) = cValuesTemp;
       end
50
51 end
52
53 end
```

```
1 function GraphHist(Y, speciesToGraph, speNames, split_flag, filename, method_name)
 3
 4 num_bins = length(Y)^(1/3);
 6 specific_species_flag = 0;
 7 speIndLength = length(speciesToGraph);
 9 if speIndLength == 0
       end_point = min ( size(Y) );
10
11 else
       end_point = speIndLength;
12
13
       specific_species_flag = 1;
14 end
15
16 if ~split_flag
17
       figure
18
       hold all
19 end
20
21 for i = 1:end_point
22
23
       if specific_species_flag
24
           current_species = speciesToGraph(i);
25
       else
26
           current_species = i;
27
       end
28
29
30
       min_val = min( Y(:,current_species) );
       max_val = max( Y(:,current_species) );
31
32
33
       % determine optimal number of bins (educated guess)
34
       space = max_val - min_val + 1;
       if space > num_bins
35
36
           bins = linspace(min_val, max_val, num_bins);
37
           h = hist( Y(:,current_species) , num_bins );
38
       else
39
           bins = linspace(min_val, max_val, space);
40
           h = hist( Y(:,current_species) , space );
41
       end
42
43
       if split_flag
44
           figure
45
       end
46
47
       plot( bins, h/length(Y) , 'o-' );
48
49
       if split_flag
50
           legend( speNames(current_species) );
           xlabel('Number of Species', 'FontSize', 12, 'FontName', 'Helvetica');
51
           ylabel('Frequency','FontSize',12,'FontName', 'Helvetica');
52
           title('Histogram of number of species at end of simulation', 'FontSize', 16, 'FontName', \nu
53
'Helvetica');
54
       end
55 end
57 if ~split_flag
```

```
58
       hold off
59
60
       if specific_species_flag
61
           legend( speNames(speciesToGraph) );
62
       else
63
           legend( speNames )
64
       end
65
       xlabel('Number of Species','FontSize',12, 'FontName', 'Helvetica');
66
       ylabel('Frequency', 'FontSize', 12, 'FontName', 'Helvetica');
67
68
       title_string = ['Histogram of number of species at end of simulation from model source '''

L
69
filename ''' using ' method_name];
       title(title_string, 'Fontsize', 16,'FontName', 'Helvetica');
71 end
72
73 end
```

```
1 function GraphResults(Y, time, speciesToGraph, speNames, split_flag, filename, method_name)
 3 specific_species_flag = 0;
 4 speIndLength = length(speciesToGraph);
 6 if speIndLength == 0
 7
       dims = size(Y);
 8
       end point = dims(1);
 9 else
10
       end_point = speIndLength;
11
       specific_species_flag = 1;
12 end
13
14 if ~split_flag
15
       figure
16
       hold all
17 end
18
19 for i = 1:end_point
20
21
       if specific_species_flag
22
           current_species = speciesToGraph(i);
23
       else
24
           current_species = i;
25
       end
26
27
       if split_flag
28
           figure
29
       end
30
       plot( time , Y(current_species,:) );
31
32
33
       if split_flag
34
           legend( speNames(current_species) );
           xlabel('Time', 'FontSize', 12, 'FontName', 'Helvetica');
35
           ylabel('Number of Species', 'FontSize', 12, 'FontName', 'Helvetica');
36
           title('Species vs time using SSA', 'FontSize', 16, 'FontName', 'Helvetica');
37
38
       end
39 end
40
41 if ~split_flag
       hold off
42
43
44
       if specific_species_flag
45
           legend( speNames(speciesToGraph) );
46
       else
47
           legend( speNames )
48
       end
49
       xlabel('Time', 'FontSize', 12, 'FontName', 'Helvetica');
50
       ylabel('Number of Species', 'FontSize', 12, 'FontName', 'Helvetica');
51
52
       title_string = ['Species vs time from model source ''' filename ''' using ' method_name];
53
       title(title_string, 'FontSize', 16, 'FontName', 'Helvetica');
54
55 end
56
57 end
```

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```
1 function varargout = MARS(filename, varargin)
 3 % Options:
 4 %
 5 % 'Hist'
                - generate a histogram of the results of 10,000 trajecories
 6 % 'Verbose' - enable diagnostic outputs
               - max time to run the simulation for
 7 % 'Time'
 8 % 'Record' - step size between recording simulation state information
                use tau-leaping
 9 % 'Tau'
 10 % 'CLE'
                - use Chemical Langevin Equation
 11 % 'RRE'
                - use raction rate equations
 12 % 'GPU'
                - use the system's CUDA-supported GPU for multiple trajectory generation
13 % 'MLMC'

    generate histogram using Multi-level Monte-Carlo simulation (experimental)

14 % 'Error'
                - error to use for MLMC method
15 % 'Steps'
               - number of data points to generate over the integration interval for all non-GPU
parallel methods
16 % 'Graph'

    plot a graph of the results

17
18 % default values for user-provided arguments
19 hist_flag
                    = 0;
20 verbose_flag
                    = 0;
21 tau flag
                    = 0;
                    = 0;
22 cle_flag
23 rre_flag
                    = 0;
 24 stiff_flag
                    = 0;
25 split_flag
                    = 0;
26 keep_flag
                    = 0;
27 record flag
                    = 0;
28 gpu flag
                    = 0:
29 graph_flag
                    = 0;
30 mlmc_flag
                    = 0;
 31 m_flag
                    = 0;
32 err_flag
                    = 0;
33 steps_flag
                    = 0;
34 tfinal
                    = 50;
35 recordStep
                    = 20;
36 numSteps
                    = 100;
 37 err
 38 speciesToGraph = [];
 39
 40 i = 1;
41 while (1+i) <= nargin
 42
        switch varargin{i}
 43
            case 'Hist'
 44
                hist_flag = 1;
 45
            case 'Verbose'
 46
 47
                verbose_flag = 1;
 48
 49
            case 'Time'
 50
                if (i+2) > nargin
 51
                    disp( sprintf('\nSimulation time argument missing.\n') );
 52
                    return;
 53
                else
 54
                    i = i + 1;
 55
                    time_arg = varargin{i};
 56
                    if ~isnumeric(time arg)
 57
                        disp( sprintf('\nSimulation time argument must be a number.\n') );
```

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```
58
                         return;
 59
                     else
 60
                         tfinal = time_arg;
 61
                     end
 62
                end
 63
 64
            case 'Record' % get record step argument, check for validity (integer)
 65
                if (i+2) > nargin
 66
                     disp( sprintf('\nRecord step size argument missing.\n') );
 67
 68
                else
 69
                     i = i + 1;
 70
                     record_arg = varargin{i};
 71
                     if ~isnumeric(record_arg) || mod(record_arg,1) ~= 0
 72
                         disp( sprintf('\nRecord step size argument must be an integer.\n') );
 73
                         return;
 74
                     else
 75
                         recordStep = record_arg;
 76
                         record_flag = 1;
 77
                     end
 78
                end
 79
 80
            case 'Tau' % use tau-leaping, get value to use for tau
 81
                if (i+2) > nargin
 82
                    tau = 0;
 83
                else
 84
                     next_arg = varargin{i+1};
 85
                     if isnumeric(next arg)
 86
                         tau = next_arg;
 87
                         i = i + 1;
                     else
 88
 89
                         tau = 0;
 90
                     end
 91
                end
 92
                tau_flag = 1;
 93
 94
            case 'CLE' % use Langevin leaping algorithm, get value to use for tau
 95
                if (i+2) > nargin
 96
                     tau = 0;
 97
                else
 98
                     next_arg = varargin{i+1};
 99
                     if isnumeric(next arg)
100
                         tau = next_arg;
101
                         i = i + 1;
102
                     else
103
                         tau = 0;
104
                     end
105
                end
106
                cle_flag = 1;
107
108
            case 'MLMC' % use MLMC method, get value to use for M, defaults to 100 steps
109
                if (i+2) > nargin
110
                    M = 0;
111
                else
112
                     m_arg = varargin{i+1};
113
                     if isnumeric(m_arg) && mod(m_arg,1) ~= 0
114
                         disp( sprintf('\nMLMC M-value argument must be an integer.\n') );
115
                         return;
```

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```
116
                     elseif isnumeric(m_arg) && mod(m_arg,1) == 0
117
                         M = m arg;
118
                         i = i + 1;
119
                         m_flag = 1;
120
                     else
121
                         M = 0;
122
                     end
123
                end
124
                mlmc flag = 1;
125
126
            case 'Steps' % get specific numer of steps to generate for parallel methods not on a∠
GPU
127
                if (i+2) > nargin
                     disp( sprintf('\nNumber of steps size argument missing.\n') );
128
129
                     return;
130
                else
131
                     step_arg = varargin{i+1};
132
                     if isnumeric(step_arg) && mod(step_arg,1) ~= 0
133
                         disp( sprintf('\nNumber of steps argument must be an integer.\n') );
134
135
                     elseif isnumeric(step_arg) && mod(step_arg,1) == 0
136
                         numSteps = step_arg;
137
                         i = i + 1;
138
                     else
139
                         disp( sprintf('\nNumber of steps size argument missing or invalid.\n') );
140
                         return:
141
                     end
142
                end
143
            case 'Error' % get error to use for MLMC method, overrides default
144
145
                if (i+2) > nargin
146
                     disp( sprintf('\nError argument missing.\n') );
147
                     return;
                else
148
149
                     i = i + 1;
150
                     err_arg = varargin{i};
151
                     if ~isnumeric(err_arg)
                         disp( sprintf('\nError argument missing.\n') );
152
                         return;
153
154
                     elseif isnumeric(err_arg) && err_arg < 0</pre>
155
                         disp( sprintf('\nError must be a positive number.\n') );
156
                     else
157
                         err = err_arg;
                     end
158
159
                end
160
161
            case 'Graph' % whether or not to grapht the results, and if so for which species∠
(default is all)
162
                if (i+2) > nargin
163
                     speciesToGraph = [];
164
                else
165
                     next_arg = varargin{i+1};
166
                     if isvector(next_arg) && isnumeric(next_arg)
167
                         speciesToGraph = next_arg;
168
                         i = i + 1;
169
                     else
170
                         speciesToGraph = [];
171
                     end
```

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```
172
                end
173
                graph_flag = 1;
174
            case 'RRE'
175
176
                rre_flag = 1;
177
            case 'Stiff'
178
179
                stiff_flag = 1;
180
            case 'Split'
181
182
                split_flag = 1;
183
            case 'Keep'
184
185
                keep_flag = 1;
186
187
            case 'GPU'
188
                gpu_flag = 1;
189
190
            otherwise
191
                disp( sprintf('\nInvalid option detected at argument %d.\n',i) );
192
193
        end
194
        i = i + 1;
195 end
196 if (tau_flag + cle_flag + rre_flag + mlmc_flag + gpu_flag) > 1
197
        disp( sprintf('\nInvalid options: multiple methods selected. You may only pick one of ∠
CLE, Tau-Leaping, RRE, MLMC, or GPU\n') );
198
        return
199 end
200
201 \text{ if tfinal} == 0
202
        disp( sprintf('\nInvalid final time argument\n') );
203
        return
204 end
205
206 if recordStep == 0
        disp( sprintf('\nInvalid record step size argument\n') );
207
208
209 end
210
211 if numSteps == 0
        disp( sprintf('\nInvalid number of steps argument\n') );
212
213
        return
214 end
215
216 if m_flag && M < 2
217
        disp( sprintf('\nMLMC M-value must be an integer greater than 1\n') );
218
        return
219 end
220
221 addpath(genpath('./toolbox/SBMLToolbox'));
222
223 platform_str = computer;
224
225 % get type of platform so proper libraries can be added to path, currently only PC, Macば
supported
226 switch platform_str
227
        case 'MACI64'
```

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```
228
            addpath(genpath('./toolbox/libSBML/mac'));
229
        case 'PCWIN'
230
            addpath(genpath('./toolbox/libSBML/win32'));
231
        case 'PCWIN64'
            addpath(genpath('./toolbox/libSBML/win64'));
232
        case 'GLNXA64'
233
234
            addpath(genpath('./toolbox/libSBML/linux'));
235
        otherwise
236
            disp('Platform not supported');
237
            return;
238 end
239
240 % create files to be filled, then close all
241 file_list = {'calculatePropensities.m';...
                'calculateSpecifiedTotals.m';...
243
                'RRE_functions.m';...
244
                'fireGpuTrajectories.m'};
245
246 num_files = length(file_list);
247 for i = 1:num_files
248
        cur_file = file_list{i};
249
        fid = fopen(cur_file,'w');
250
        fclose(fid);
251 end
252
253 % get system (model) inforamtion from SBML file
254 SysInf = SSA_setup(filename, verbose_flag);
                      = SysInf.numSpecies;
255 numSpecies
256 numReactions
                      = SysInf.numReactions;
257 speNames
                      = SysInf.speNames;
258 speValues
                      = SysInf.speValues;
259 cNames
                      = SysInf.cNames;
260 cValues
                      = SysInf.cValues;
261 speConstIndecies = SysInf.speConstIndecies;
262 totalsIndecies
                      = SysInf.totalsIndecies;
263 VHolder
                      = SysInf.VHolder;
264
265 % check for bad species—to—graph entries
266 if graph_flag && ~mlmc_flag
        numSpeToGraph = length(speciesToGraph);
267
268
        if numSpeToGraph ~= 0
269
            for i = 1:numSpeToGraph
270
271
                curIndex = speciesToGraph(i);
272
                if curIndex > numSpecies || curIndex < 1</pre>
273
                    disp( sprintf(['Error: invalid species index provided, exceeds number of ✓
species in system or is less than 1.'...
                                    Graph will not be displayed.\n'l) );
274
275
                    graph_flag = 0;
276
                end
277
                for j = 1:(i-1)
278
279
                    checkIndex = speciesToGraph(j);
280
                    if checkIndex == curIndex
                        disp( sprintf('Error: invalid species index provided, duplicate index.

Graph will not be displayed.\n') );
282
                        graph_flag = 0;
283
                    end
```

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```
284
                end
285
286
            end
287
        end
288 end
289
290 method_name = '';
291 rehash
292
293 if gpu_flag
294
        Y = SSA_gpu(filename, SysInf, tfinal, verbose_flag);
295
        method_name = 'SSA on GPU';
296
297 elseif mlmc flag
298
        %open parallel pool based on installed toolbox version
299
        version_less_flag = verLessThan('distcomp', '6.3');
300
        if version_less_flag
301
            matlabpool open;
302
        else
303
            parpool;
304
        end
305
306
        [Mean, Step] = MLMCGen(SysInf, tfinal, numSteps, verbose_flag, split_flag, ∠
speciesToGraph, graph_flag, M, err);
307
        Y = Mean;
308
        varargout{3} = Step;
309
        time = linspace(0,tfinal,numSteps);
310
        varargout{2} = time;
        method_name = 'MLMC';
311
312
        % close parallel pool
313
314
        if version_less_flag
315
            matlabpool close;
316
        else
317
            delete(gcp);
318
        end
319
320 elseif hist_flag
        %open parallel pool based on installed toolbox version
321
        version_less_flag = verLessThan('distcomp', '6.3');
322
323
        if version_less_flag
324
            matlabpool open;
325
        else
326
            parpool;
327
        end
328
329
        % use indicated method to generate trajectories accross multiple CPUs or CPU cores
330
        if tau_flag
            [Y,Mean,Std] = SSAGen_parfor_tauleap(SysInf, tfinal, recordStep, verbose_flag, tau, ∠
331
speciesToGraph, numSteps, graph_flag, 0);
            method_name = 'SSA with tau-leaping on parallel CPUs';
332
333
        elseif cle_flag
            [Y,Mean,Std] = SSAGen_parfor_cle(SysInf, tfinal, recordStep, verbose_flag, tau, ∠
334
speciesToGraph, numSteps, graph_flag);
335
            method_name = 'CLE on parallel CPUs';
336
        elseif rre flag
337
            disp( sprintf('\n''Hist'' is not a valid option to use with the Reaction Rate⊭
Equation method\n') );
```

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```
338
        else
339
            [Y,Mean,Std] = SSAGen parfor(SysInf, tfinal, recordStep, verbose flag, ∠
speciesToGraph, numSteps, graph_flag);
            method_name = 'SSA on parallel CPUs';
340
341
        end
342
343
        varargout{2} = Mean;
344
        varargout{3} = Std;
345
346
        % close parallel pool
347
        if version_less_flag
348
            matlabpool close;
349
        else
350
            delete(gcp);
351
        end
352
353 else
        % generate single trajectory based on indicated method
354
355
        if tau_flag
356
            [time, Y] = SSAGen_tauleap(SysInf, tfinal, recordStep, verbose_flag, tau);
357
            method_name = 'SSA with tau-leaping';
358
        elseif cle flag
359
            [time, Y] = SSAGen_cle(SysInf, tfinal, recordStep, verbose_flag, tau);
360
            method_name = 'CLE';
361
        elseif rre_flag
362
            if record_flag
                disp(sprintf('\nWarning: ''Record'' argument will be ignored - not valid with ∠
363
Reaction Rate Equation method\n'));
364
            [time, Y] = RREGen(SysInf, tfinal, verbose_flag, stiff_flag);
365
366
            method name = 'RRE';
367
        else
368
            [time, Y] = SSAGen(SysInf, tfinal, recordStep, verbose_flag);
369
            method_name = 'SSA';
370
        end
371
372
        varargout{2} = time;
373 end
374
375 \text{ varargout}\{1\} = Y;
376
377 arg_type = class(filename);
378 switch arg_type
379
        case 'struct'
380
            filename = filename.name;
381 end
382
383 % graph end of simulation histogram is using a parallel method and graph flag has been set
384 if graph_flag
385
        if gpu_flag || hist_flag
            GraphHist(Y, speciesToGraph, speNames, split_flag, filename, method_name);
386
387
        else
            GraphPlot(Y, time, speciesToGraph, speNames, split_flag, filename, method_name);
388
389
        end
390 end
391
392 % keep temporary files if indicated
393 if ~keep flag
```

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```
1 function [Y, Step] = MLMCGen(SysInf, tfinal, numSteps, verbose_flag, split_flag, ∠
speciesToGraph, graph_flag, M, err)
 3 numSpecies
                      = SysInf.numSpecies;
                      = SysInf.numReactions;
 4 numReactions
                      = SysInf.speNames;
 5 speNames
                      = SysInf.speValues;
 6 speValues
 7 cNames
                      = SysInf.cNames;
 8 cValues
                      = SysInf.cValues;
 9 speConstIndecies = SysInf.speConstIndecies;
 10 totalsIndecies
                      = SysInf.totalsIndecies;
 11 VHolder
                      = SysInf.VHolder;
12
13 % initial values
14 X = speValues;
15 numSteps = numSteps - 1;
16
17 if err == 0
18
        err = 1/100;
19 end
20
21 % extract V from VHolder and display
22 V = VHolder.V;
23
 24 if verbose flag
25
        disp( sprintf('Stoichiometric Matrix:\n') ); disp(V);
26 end
27
 28 % matricies to hold propensity values, number of species present after each step, and the \checkmark
length of each step
29 A = zeros(numReactions,1);
30
31 % parameters
32 N = max(X);
33
34 % default M
35 \text{ if } M == 0
 36
       M = 3;
37 end
38
39 alp = zeros(numSpecies,1);
40 for i = 1:numSpecies
41
        val = X(i);
 42
        if val == 0
 43
            alp(i) = 0;
 44
        else
 45
            alp(i) = log(val)/log(N);
 46
        end
 47 end
48
 49 bet = zeros(numReactions,1);
 50 for i = 1:numReactions
 51
        val = cValues(i);
 52
        if val ~= 0
            bet(i) = log(val)/log(N);
 53
 54
        end
 55 end
 56
```

```
57 V_pos = -V;
 58 V_{pos}(V_{pos} < 0) = 0;
 60 % get gamma value from largest of candidates
 61 \text{ gam} = -Inf;
 62 for i = 1:numSpecies
        for k = 1:numReactions
 63
 64
            if V(i,k) \sim 0
 65
                 gam_can = bet(k) + dot(V_pos(:,k),alp) - alp(i);
 66
                 if gam_can > gam
 67
                     gam = gam_can;
 68
                 end
 69
            end
        end
 70
 71 end
 72
 73 % get rho value from largest of candidates
 74 rho = Inf;
 75 for k = 1:numReactions
 76
        for i = 1:numSpecies
 77
            if V(i,k) ~= 0
 78
                 rho_can = alp(i);
 79
                 if rho_can < rho</pre>
 80
                     rho = rho_can;
 81
                 end
 82
            end
        end
 83
 84 end
 85
 86 L = ceil(abs(log(err)));
 88 % should have three levels
 89 if L <= 2
 90
        l_0 = 0;
 91 else
 92
        l_0 = L - 2;
 93 end
 94
 95 num_levels = L - l_0 + 1;
 97 % get required number of coarsest trajectories
 98 n 0 = 4 * ceil( (N^-rho * N^-gam * err^-2) / 4 );
 99
100 % get level step sizes and required number of trajectories
101 h_l = zeros(num_levels, 1);
102 n_l = zeros(num_levels, 1);
103 for i = 1:num_levels
104
        l = l_0 + i - 1;
        h_l(i) = tfinal/(M^l);
105
        n_l(i) = ceil( N^-rho * N^gam * (L - l_0) * h_l(i) * err^-2 );
106
107 end
108
109 % make each n_l divisible by 4
110 for i = 1:num_levels
        val = n_l(i);
112
        while mod(val, 4) \sim = 0
113
            val = val+1;
114
        end
```

```
115
        n_l(i) = val;
116 end
117
118 % print information if required
119 if verbose_flag
        fprintf('N:\t%d\n', N);
120
        fprintf('Gamma:\t%d\n', gam);
121
        fprintf('Rho:\t%d\n', rho);
122
123
        fprintf('M:\t%d\n', M);
124
        fprintf('Error:\t%d\n', err);
        fprintf('Granularities:\n\n');
125
126
            disp(h_l);
        fprintf('Number of trajectories at each level:\n\n');
127
128
            disp(n 0);
129
            disp(n_l(2:num_levels));
130 end
131
132 num_trajectories = sum(n_l);
133
134 interval = tfinal/(numSteps+1);
135
136 % level 0
137 [~, Mean_coarse, ~] = SSAGen_parfor_tauleap(SysInf, tfinal, 0, 0, h_l(1), speciesToGraph, ∠
numSteps+1, 0, n_0);
138
139 Y = Mean_coarse;
140 time = linspace(0,tfinal,numSteps+1);
                          ----- % start MLMC
142 % ---
143
144 for i = 2:num_levels
145
146
        num_runs = n_l(i);
147
        Y_sub = zeros( num_runs , numSpecies, numSteps+1);
148
149
150
        parfor k = 1:num_runs
151
            % setup that level trajectory
152
153
            hl
                    = h_l(i);
                    = M*hl;
154
            hl_1
            l
                        = 10 + i - 1;
155
                        = X;
156
            zl
            zl_1
157
                        = X;
                        = zeros(numSpecies, numSteps+1);
158
            Ζl
159
            Zl_1
                        = zeros(numSpecies, numSteps+1);
160
            Zl(:,1)
                        = X;
161
            Zl_1(:,1)
                        = X;
162
            t
                        = 0;
                        = 2;
163
            n
164
            while n <= (numSteps+1)</pre>
165
166
167
                lam_bot = calculatePropensities(zl_1)';
168
                A = zeros(numReactions, 3);
169
170
                for j = 1:M
171
```

```
172
                     lam_top = calculatePropensities(zl)';
173
174
                    % (a)
175
                    A(:,1) = min(lam_top, lam_bot);
176
                    A(:,2) = lam_{top} - A(:,1);
177
                    A(:,3) = lam_bot - A(:,1);
178
179
                    % (b)
180
                    Lam = poissrnd(A*hl);
181
                    % (c)
182
                    delta_top = Lam(:,1) + Lam(:,2);
183
184
                    delta_bot = Lam(:,1) + Lam(:,3);
                    zl = zl + V*delta_top;
185
186
                    zl_1 = zl_1 + V*delta_bot;
187
188
                    zl(speConstIndecies) = speValues(speConstIndecies);
                     zl_1(speConstIndecies) = speValues(speConstIndecies);
189
190
                    zl = calculateSpecifiedTotals(zl);
191
                    zl_1 = calculateSpecifiedTotals(zl_1);
192
193
                end
194
195
                t = t + hl_1;
196
197
                % record
198
                if t > ((n-1)*interval)
199
                    Zl(:,n) = zl;
200
                    Zl_1(:,n) = zl_1;
201
                    n = n + 1;
202
                end
203
            end
204
205
            data = Zl - Zl_1;
206
            Y_{sub}(k,:,:) = data;
207
208
        end
209
210
        Mean_level = zeros(numSpecies, numSteps+1);
211
212
        for i = 1:numSpecies
213
            for j = 1:(numSteps+1)
                Mean(i,j) = mean(Y_sub(:,i,j));
214
215
            end
216
        end
217
218
        Y = Y + Mean_level;
219
220 end
221
222 Step = h_l(length(h_l));
223
224 end
```

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```
1 function [time, Y] = RREGen(SysInf, tfinal, verbose_flag, stiff_flag)
  3 numSpecies
                      = SysInf.numSpecies;
  4 numReactions
                      = SysInf.numReactions;
  5 speNames
                      = SysInf.speNames;
  6 speValues
                      = SysInf.speValues;
  7 cNames
                      = SysInf.cNames;
  8 cValues
                      = SysInf.cValues;
  9 speConstIndecies = SysInf.speConstIndecies;
                      = SysInf.totalsIndecies;
 10 totalsIndecies
 11 VHolder
                      = SysInf.VHolder;
 12
 13 if verbose_flag
        disp( sprintf('\nNumber of species types:\n') ); disp(numSpecies);
 15
        disp( sprintf('\nNumber of reactions:\n') ); disp(numReactions);
 16 end
 17
 18 if verbose_flag
        disp( sprintf('\nParameter names:\n') ); disp(cNames);
 19
        disp( sprintf('\nParameter values:\n') ); disp(cValues);
 20
 21 end
 22
 23 if verbose_flag
        disp( sprintf('\nSpecies'' names:\n') ); disp(speNames);
 24
        disp( sprintf('\nSpecies'' initial amounts:\n') ); disp(speValues);
 25
 26 end
 27
 28 % holder strings for RHS of RREs
 29 for i = 1:numReactions
        A\{i\} = '';
 30
 31 end
 32 A = A';
 33
 34 V = VHolder.V;
 35 vNumOfReactant = VHolder.vNumOfReactant;
 36 vReactant = VHolder.vReactant;
 37 vDimerMap = VHolder.vDimerMap;
 39 if verbose_flag
        disp( sprintf('Stoichiometric Matrix:\n') ); disp(V);
 40
 41 end
 42
 43 for i = 1:numReactions
 44
        % set initially to that reaction's parameter
 45
        format long;
 46
 47
        A{i} = strcat( A{i} , num2str( cValues(i) ) );
 48
        st multiply current value by each reactant's value if applicable, and account foroldsymbol{arepsilon}
 49
dimerisation reactions
        for k = 1:(vNumOfReactant(i));
 50
 51
 52
            curSpeciesIndex = vReactant(i,k);
 53
 54
            A{i} = strcat( A{i} , sprintf('*X(%d)',curSpeciesIndex) );
 55
            % determine if reactant is part of a dimerisation reaction using dimerisation map, \checkmark
then alter propensity accordingly
```

```
57
            dimer_number = vDimerMap(curSpeciesIndex, i);
 58
            if dimer number > 1
 59
                for j = 1:(dimer_number-1)
 60
                    A\{i\} = strcat(A\{i\}, sprintf('*(X(%d)-%d)', curSpeciesIndex, j));
 61
                end
 62
 63
                A{i} = strcat( A{i} , sprintf('/%d', factorial(dimer_number) ) );
 64
            end
 65
        end
 66 end
 67
 68 fid = fopen('RRE functions.m','w');
 69 fprintf(fid, 'function dXdt = RRE_functions(t,X)');
 70
 71 fprintf(fid, '\n\ndXdt = zeros(%d,1);\n\n', numSpecies);
 72
 73 for i = 1:numSpecies
 74
 75
        fprintf(fid, 'dXdt(%d) = 0',i);
 76
 77
        if ~ismember(i,speConstIndecies)
 78
            for j = 1:numReactions
 79
                if V(i,j) ~= 0
 80
                    fprintf(fid, ' + %d*%s', V(i,j), A{j});
 81
                end
 82
            end
 83
        end
 84
 85
        fprintf(fid,';\n');
 86
 87 end
 88
 89 fprintf(fid, '\nend');
 90 fclose(fid);
 92 %tspan = linspace(0,tfinal,tfinal);
 93 tspan = [0 tfinal];
 95 disp( sprintf('======Starting Solver======') )
 96
 97 if stiff_flag
        [time,y] = ode15s(@RRE functions,tspan,speValues);
 98
 99 else
        [time,y] = ode45(@RRE_functions,tspan,speValues);
100
101 end
102
103 Y = y';
104
105 if length(totalsIndecies) ~= 0
        for i = 1:length(time)
106
            Y(:,i) = calculateSpecifiedTotals(Y(:,i));
107
108
        end
109 end
110
111 if verbose_flag
        disp(sprintf('\nSpecies'' final amounts:\n'));
112
113
        Amount = Y(:, length(Y));
        dataTable = table(Amount, 'RowNames', speNames);
114
```

```
115          disp(dataTable);
116 end
117
118 end
```

```
1 function [Y, X, time, run_time] = SingleTrajectory(V, X, speConstIndecies, numSpecies, ∠
speValues, tfinal, recordStep, verbose_flag)
3 % set max muber of data points for each chunk of the recorded values matrix
 4 numMaxDataPoints = 10000;
6 Y = zeros(numSpecies, numMaxDataPoints);
7 time = zeros(1, numMaxDataPoints);
9 % assign initial values recorded values
10 Y(:, 1) = X;
11 time(1) = 0;
12
13 % initial values
14 t = 0;
15 count = 1;
16
17 speConstIndeciesLength = length(speConstIndecies);
18
19 if verbose_flag
20
       disp( sprintf('\n==============\n') );
21 end
22
23 tic
24
25 while t < tfinal
26
27
       % calculate value of each propensity at that step
28
29
       A = calculatePropensities(X);
30
31
32
      asum = sum(A);
33
34
      % break out of simulation if all species are consumed
35
       if asum == 0
36
           if verbose_flag
               disp(sprintf('\n=======REACTION HALTED - ALL SPECIES COMSUMED=======\n'));
37
               disp(sprintf('Final time was %f', t) );
38
39
           end
40
           Y(:, ceil(count/recordStep) + 1) = X;
41
42
           time( ceil(count/recordStep) + 1 ) = t;
43
44
           break
45
       end
46
       j = min( find( rand < cumsum(A/asum) ) );</pre>
47
       tau = log(1/rand)/asum;
48
49
      X = X + V(:,j);
50
51
52
53
       X = calculateSpecifiedTotals(X);
54
55
56
       for i = 1:speConstIndeciesLength
57
           X(speConstIndecies(i)) = speValues(speConstIndecies(i));
```

```
58
      end
59
60
      t = t + tau;
61
       if mod(count, recordStep) == 0
62
63
           Y(:, (count/recordStep) + 1) = X;
64
           time(count/recordStep + 1) = t;
65
      end
66
67
      count = count + 1;
68 end
69
70 run_time = toc;
71
72 Y = Y( : ,1:(floor(count/recordStep)) );
73 time = time( 1:(floor(count/recordStep)) );
74
75 if verbose_flag
      disp( sprintf('\n%d steps taken\n', count ) );
76
77
      disp( sprintf('%d steps recorded\n', floor(count/recordStep) ) );
78 end
79
80 end
```

```
1 function [Y, X, time, run_time] = SingleTrajectory_cle(V, X, speConstIndecies, numSpecies, ✓
speValues, tfinal, recordStep, verbose_flag, tau)
3 % set max muber of data points for each chunk of the recorded values matrix
 4 numMaxDataPoints = 10000;
6 Y = zeros(numSpecies, numMaxDataPoints);
7 time = zeros(1, numMaxDataPoints);
9 % assign initial values recorded values
10 Y(:, 1) = X;
11 time(1) = 0;
12
13 % initial values
14 t = 0;
15 count = 1;
16
17 speConstIndeciesLength = length(speConstIndecies);
18
19 if verbose_flag
20
      disp( sprintf('\n==========\n') );
21 end
22
23 tic
24
25 while t < tfinal
26
27
       % calculate value of each propensity at that step
28
29
      A = calculatePropensities(X);
30
31
32
      % break out of simulation if all species are consumed
33
       if cumsum(A) == 0
34
          if verbose flag
               disp(sprintf('\n=======REACTION HALTED - ALL SPECIES COMSUMED=======\n'));
35
               disp(sprintf('Final time was %f', t) );
36
37
38
          Y(:, floor(count/recordStep) + 1) = X;
39
          time( floor(count/recordStep) + 1) = t;
40
41
42
          break
43
      end
44
45
      % get sampling of random variables and sub into CLE formula
46
      d = tau*A + sqrt(abs(tau*A)) * rand;
47
48
      % update values
49
      X = X + V * d';
50
51
      X = calculateSpecifiedTotals(X);
52
53
54
55
       for i = 1:speConstIndeciesLength
56
          X(speConstIndecies(i)) = speValues(speConstIndecies(i));
57
       end
```

```
58
59
      t = t + tau;
60
61
       if mod(count, recordStep) == 0
           Y(:, (count/recordStep) + 1) = X;
62
           time(count/recordStep + 1) = t;
63
64
       end
65
66
      count = count + 1;
67 end
68
69 run_time = toc;
70
71 Y = Y(: ,1:(floor(count/recordStep)));
72 time = time( 1:(floor(count/recordStep)) );
73
74 if verbose_flag
      disp( sprintf('\n%d steps taken\n', count-1 ) );
75
       disp( sprintf('%d steps recorded\n', floor(count/recordStep)-1 ) );
76
77 end
78
79 end
```

```
1 function [Y, X, time, run_time] = SingleTrajectory_tauleap(V, X, speConstIndecies, numSpecies, ∠
speValues, tfinal, recordStep, verbose_flag, tau)
3 % set max muber of data points for each chunk of the recorded values matrix
 4 numMaxDataPoints = 10000;
6 Y = zeros(numSpecies, numMaxDataPoints);
7 time = zeros(1, numMaxDataPoints);
9 % assign initial values recorded values
10 Y(:, 1) = X;
11 time(1) = 0;
12
13 % initial values
14 t = 0;
15 count = 1;
16
17 speConstIndeciesLength = length(speConstIndecies);
18
19 if verbose_flag
20
      disp( sprintf('\n==========\n') );
21 end
22
23 tic
24
25 while t < tfinal
26
27
       % calculate value of each propensity at that step
28
29
      A = calculatePropensities(X);
30
31
32
      % break out of simulation if all species are consumed
33
       if cumsum(A) == 0
34
          if verbose flag
               disp(sprintf('\n=======REACTION HALTED - ALL SPECIES COMSUMED=======\n'));
35
               disp(sprintf('Final time was %f', t) );
36
37
          end
38
39
          Y(:, floor(count/recordStep) + 1) = X;
          time( floor(count/recordStep) + 1) = t;
40
41
42
          break
43
      end
44
45
      % get sampling of poisson random variables
46
      pois_rand_vars = poissrnd(A*tau);
47
48
      % update values
49
      X = X + V * pois_rand_vars';
50
51
      X = calculateSpecifiedTotals(X);
52
53
54
55
       for i = 1:speConstIndeciesLength
56
          X(speConstIndecies(i)) = speValues(speConstIndecies(i));
57
       end
```

```
58
59
      t = t + tau;
60
61
       if mod(count, recordStep) == 0
           Y(:, (count/recordStep) + 1) = X;
62
           time(count/recordStep + 1) = t;
63
64
       end
65
66
      count = count + 1;
67 end
68
69 run_time = toc;
70
71 Y = Y( : ,1:(floor(count/recordStep)) );
72 time = time( 1:(floor(count/recordStep)) );
73
74 if verbose_flag
      disp( sprintf('\n%d steps taken\n', count-1 ) );
75
       disp( sprintf('%d steps recorded\n', floor(count/recordStep)-1 ) );
76
77 end
78
79 end
```

```
1 function Y = SSA_gpu(filename, SysInf, tfinal, verbose_flag)
 3 numSpecies
                     = SysInf.numSpecies;
 4 numReactions
                     = SysInf.numReactions;
 5 speNames
                     = SysInf.speNames;
 6 speValues
                     = SysInf.speValues;
 7 cNames
                     = SysInf.cNames;
 8 cValues
                     = SysInf.cValues;
 9 speConstIndecies = SysInf.speConstIndecies;
                     = SysInf.totalsIndecies;
10 totalsIndecies
11 VHolder
                     = SysInf.VHolder;
12 gpu = gpuDevice();
13
14 if verbose_flag
15
       disp( sprintf('GPU Device detected:\n') );
16
       disp(gpu);
17 end
18
19 V = VHolder.V;
20 vNumOfReactant = VHolder.vNumOfReactant;
21 vReactant = VHolder.vReactant;
22 vDimerMap = VHolder.vDimerMap;
23
24 fid = fopen('fireGpuTrajectories.m','w');
25 fprintf(fid, 'function Y = fireGpuTrajectories(VHolder, verbose_flag)\n\n');
26
27 fprintf(fid, 'V = VHolder.V;\n\n');
29 for i = 1:numSpecies
       fprintf(fid, 'x%d = %d;\n', i, speValues(i));
30
31 end
32
33 fprintf(fid, '\ntfinal = %d;\n\n', tfinal);
35 fprintf(fid, '\tfunction [input');
36 for i = 1:numSpecies
37
       fprintf(fid, ', x%d', i);
38 end
39 fprintf(fid, ']');
40
41 fprintf(fid, ' = fire_single_gpu_trajectory(input');
42 for i = 1:numSpecies
43
       fprintf(fid, ', x%d', i);
44 end
45 fprintf(fid, ')\n\n');
46
47 format long
48
49 for i = 1:numReactions
50
       fprintf(fid, '\t\tc%d = %e;\n', i, cValues(i));
51 end
52
53 fprintf(fid, '\n\t = 0;\n');
54
55 fprintf(fid, '\n\t\twhile t < tfinal\n\n');</pre>
57 for i = 1:numReactions
58
```

```
59
        % set initially to that reaction's parameter
 60
        format long;
 61
        fprintf(fid, '\t\ta%d = (%e)', i, cValues(i) );
 62
        st multiply current value by each ractant's value if applicable, and account foroldsymbol{arepsilon}
 63
dimerisation reactions
        for k = 1:(vNumOfReactant(i));
 64
 65
 66
            curSpeciesIndex = vReactant(i,k);
 67
            fprintf(fid,'*x%d', curSpeciesIndex);
 68
 69
            % determine is reactant is part of a dimerisation reaction using dimerisation map, \nu
 70
then alter propensity accordingly
 71
            dimer number = vDimerMap(curSpeciesIndex, i);
 72
            if dimer_number > 1
 73
                count = 1;
 74
                while (count < dimer_number)</pre>
 75
                    fprintf(fid,'*(x%d-%d)', curSpeciesIndex, count);
 76
                    count = count + 1;
 77
                end
 78
                fprintf(fid,'/%d', factorial(dimer_number) );
 79
 80
            end
 81
        end
 82
 83
        fprintf(fid, ';\n', i, cValues(i) );
 84 end
 85
 86 fprintf(fid, '\n\t\t\tasum =');
 87 for i = 1:numReactions
 88
        fprintf(fid, ' + a%d', i);
 89 end
 90 fprintf(fid, ';\n\n');
 92 fprintf(fid, '\t\tif asum == 0\n\t\t\treturn\n\t\tend\n\n');
 93
 94 for i = 1:numReactions
 95
        fprintf(fid, '\t\ta_tot_%d = (', i);
 96
        for j = 1:i
 97
            fprintf(fid,'+a%d', j);
 98
 99
        fprintf(fid, ')/asum;\n');
100 end
101
102 fprintf(fid, '\n\t\tj = 1;\n\n');
103 fprintf(fid, '\t\trand_num = rand;\n\n');
105 fprintf(fid, '\t\tif a_tot_1 > rand_num\n');
106 fprintf(fid, '\t\t\tj = 1;\n');
107
108 for i = 2:numReactions
        fprintf(fid, '\t\telseif a_tot_%d > rand_num\n', i);
109
        fprintf(fid, '\t\t\tj = %d;\n', i);
110
111 end
112
113 fprintf(fid, '\t\tend\n\n');
114
```

```
115 fprintf(fid, '\t\ttau = log(1/rand)/asum;\n\n');
117 for i = 1:numSpecies
        if ~ismember(i,speConstIndecies)
118
119
            fprintf(fid, '\t\t\x%d = x%d + V(%d,j);\n', i, i, i);
        end
120
121 end
122
123 fprintf(fid, '\n');
124 SBMLModel = TranslateSBML(filename);
125 count = 0;
126 for i = 1:length(SBMLModel.rule)
        curRule = SBMLModel.rule(i);
127
128
129
        for j = 1:length( speNames )
130
            if strcmp( speNames(j), curRule.variable )
131
132
                totalsIndecies(count+1) = j;
133
                count = count + 1;
                fprintf(fid, '\t\tx%d =', j);
134
135
136
                % token string array
137
                ruleToks = strsplit( curRule.formula , '+');
138
139
                for l = 1:length( ruleToks )
140
                    for m = 1:length(speNames)
141
                        if strcmp( speNames(m), ruleToks(l) )
142
                             fprintf(fid, ' + x%d', m);
143
                        end
                    end
144
145
                end
146
147
                fprintf(fid, ';\n', m);
148
149
                break;
150
            end
        end
151
152 end
153
154 fprintf(fid, '\n\t\t\tt = t + tau;\n\n');
156 fprintf(fid, '\t\tend\n\n');
157 fprintf(fid, '\tend');
158
159 fprintf(fid, '\n\nnum_trajectories = 10000;\n');
160
161 fprintf(fid, 'trial_nums = linspace(1,num_trajectories, num_trajectories)'';\n' );
162 fprintf(fid, 'inputs = gpuArray(trial_nums);\n' );
164 fprintf(fid, '\n[g_trial');
165 for i = 1:numSpecies
        fprintf(fid, ', g_x%d', i);
166
167 end
168 fprintf(fid, '] = arrayfun(@fire_single_gpu_trajectory, inputs');
169 for i = 1:numSpecies
170
        fprintf(fid, ', x%d', i);
171 end
172 fprintf(fid, ');\n\n');
```

```
173
174 fprintf(fid, 'trials = gather(g_trial);\n');
175
176 fprintf(fid, 'Y = [');
177 for i = 1:numSpecies
178
        fprintf(fid, ' gather(g_x%d)', i);
179 end
180 fprintf(fid, '];\n\n');
182 fprintf(fid,'\nend');
183
184 fclose(fid);
185
186 Y = fireGpuTrajectories(VHolder, verbose_flag);
187 wait(gpu);
188
189 Mean = zeros(numSpecies, 1);
190 Std_dev = zeros(numSpecies, 1);
191 for i = 1:numSpecies
192
        data = Y(:, i);
193
        Mean(i) = mean( data );
        Std_dev(i) = std( data );
194
195 end
196
197 if verbose_flag
        dataTableMean = table(Mean, 'RowNames', speNames);
198
199
        disp(dataTableMean);
200
        dataTableStddev = table(Std_dev,'RowNames',speNames);
201
        disp(dataTableStddev);
202 end
203
204 end
```

```
1 function SysInf = SSA_setup(filename, verbose_flag)
 3 if verbose_flag
       disp(' ');
 4
 5 end
 6
 7 arg_type = class(filename);
 8
 9 switch arg_type
       case 'char'
10
11
           SBMLModel = TranslateSBML(filename);
12
       case 'struct'
13
           SBMLModel = filename;
14 end
15
16
17 % determine number of reactions and species present in the model
18 numReactions = length(SBMLModel.reaction);
19 numSpecies = length(SBMLModel.species);
20
21 if verbose_flag
22
       disp( sprintf('\nNumber of species types:\n') ); disp(numSpecies);
       disp( sprintf('\nNumber of reactions:\n') ); disp(numReactions);
23
24 end
25
26 [cNames, cValues] = GetParameters(SBMLModel);
27
28 if verbose flag
       [cNames_us, cValues_us] = GetAllParameters(SBMLModel);
29
30
       cNames_us = cNames_us';
31
       cValues_us = cValues_us';
32
33
       disp(sprintf('\nParameter Values:\n'))
34
       Value = cValues_us;
35
       dataTable = table(Value, 'RowNames', cNames_us);
36
       disp(dataTable);
37 end
38
39 % get species names and values, set X to initial values
40 [speNames, speValues] = GetSpecies(SBMLModel);
41 speNames = speNames';
42 speValues = speValues';
43
44 if verbose_flag
       disp(sprintf('\nSpecies'' initial amounts:\n'))
45
46
       Amount = speValues;
47
       dataTable = table(Amount, 'RowNames', speNames);
48
       disp(dataTable);
49 end
50
51 % matricies to hold propensity values, number of species present after each step, and thearkappa
length of each step
52 A = zeros(numReactions,1);
53
54 VHolder = StoichiometricMatricesHolder(SBMLModel);
55
56 % will generate 'calculatePropensities.m' file
57 GeneratePropensityCalculatorFile(SBMLModel, VHolder);
```

```
58
59 % will generate 'calculateSpecifiedTotals.m' file
60 totalsIndecies = GenerateSpecifiedTotalsCalculatorFile(SBMLModel);
61
62 % determine if any species have a boundary condition and get their indecies
63 speConstIndecies = GetConstantSpeciesIndecies(SBMLModel);
64
65 SysInf = SystemInformationHolder;
66
67 SysInf.numSpecies
                            = numSpecies;
68 SysInf.numReactions
                            = numReactions;
69 SysInf.speNames
                            = speNames;
70 SysInf.speValues
                            = speValues;
71 SysInf.cNames
                            = cNames;
72 SysInf.cValues
                            = cValues;
73 SysInf.speConstIndecies = speConstIndecies;
74 SysInf.totalsIndecies
                           = totalsIndecies;
75 SysInf.VHolder
                            = VHolder;
76
77 end
```

D:\mars\SSAGen.m

```
1 function [time, Y] = SSAGen(SysInf, tfinal, recordStep, verbose_flag, split_flag)
3 numSpecies
                    = SysInf.numSpecies;
4 numReactions
                    = SysInf.numReactions;
5 speNames
                    = SysInf.speNames;
6 speValues
                    = SysInf.speValues;
7 cNames
                    = SysInf.cNames;
8 cValues
                    = SysInf.cValues;
9 speConstIndecies = SysInf.speConstIndecies;
                    = SysInf.totalsIndecies;
10 totalsIndecies
11 VHolder
                    = SysInf.VHolder;
12
13 % initial values
14 X = speValues;
16 % extract V from VHolder and display
17 V = VHolder.V;
18
19 if verbose_flag
       disp( sprintf('Stoichiometric Matrix:\n') ); disp(V);
20
21 end
23 % matricies to hold propensity values, number of species present after each step, and the⊭
length of each step
24 A = zeros(numReactions,1);
25
26 % Actually do SSA ---- %
27 [Y, X, time, run_time] = SingleTrajectory(V, X, speConstIndecies, numSpecies, speValues, ⊬
tfinal, recordStep, verbose_flag);
28 % ---
29
30 if verbose_flag
31
       disp(sprintf('\nSpecies'' final amounts:\n'));
32
       Amount = X;
33
       dataTable = table(Amount, 'RowNames', speNames);
34
       disp(dataTable);
35 end
36
37 if verbose_flag
       disp(' ');
38
39 end
40
41 end
```

```
1 function [time, Y] = SSAGen(SysInf, tfinal, recordStep, verbose_flag, tau)
 3 numSpecies
                     = SysInf.numSpecies;
 4 numReactions
                     = SysInf.numReactions;
 5 speNames
                     = SysInf.speNames;
 6 speValues
                     = SysInf.speValues;
 7 cNames
                     = SysInf.cNames;
 8 cValues
                     = SysInf.cValues;
9 speConstIndecies = SysInf.speConstIndecies;
10 totalsIndecies
                     = SysInf.totalsIndecies;
11 VHolder
                     = SysInf.VHolder;
12
13 % initial values
14 X = speValues;
16 % extract V from VHolder and display
17 V = VHolder.V;
18 if verbose_flag
       disp( sprintf('Stoichiometric Matrix:\n') ); disp(V);
19
20 end
21
22 % attempt to pick tau if not specified - *extremely* crude estimate
23 if tau == 0
24
       % Single SSA trajectory to help determine good tau
25
       [Y, X, time, run_time] = SingleTrajectory(V, X, speConstIndecies, numSpecies, speValues, ∠
tfinal, recordStep, verbose_flag);
       tau = ( time(length(time)) / ( length(time)*recordStep ) ) * 3;
26
27 end
28
29 if verbose_flag
       disp( sprintf('Chosen value for tau:\n') ); disp(tau);
30
31 end
32
33 X = speValues;
34
35 tic
36 [Y, X, time, run_time] = SingleTrajectory_cle(V, X, speConstIndecies, numSpecies, speValues, ∠
tfinal, recordStep, verbose_flag, tau);
37 time_with_leap = toc;
38
39 if verbose_flag
       disp(sprintf('\nSpecies'' final amounts:\n'));
40
41
       Amount = X;
42
       dataTable = table(Amount, 'RowNames', speNames);
43
       disp(dataTable);
44 end
45
46 if verbose_flag
       disp(' ');
47
48 end
49
50 end
```

```
1 function varargout = SSAGen_parfor(SysInf, tfinal, recordStep, verbose_flag, speciesToGraph, ∠
numSteps, graph_flag)
 2
                      = SysInf.numSpecies;
 3 numSpecies
 4 numReactions
                      = SysInf.numReactions;
                     = SysInf.speNames;
 5 speNames
                     = SysInf.speValues;
 6 speValues
 7 cNames
                     = SysInf.cNames;
 8 cValues
                     = SysInf.cValues;
 9 speConstIndecies = SysInf.speConstIndecies;
                     = SysInf.totalsIndecies;
10 totalsIndecies
11 VHolder
                      = SysInf.VHolder;
12
13 if verbose_flag
14
        disp(' ');
15 end
16
17 % set max muber of data points for each chunk of the recorded values matrix
18 numMaxDataPoints = 10008;
19
20 % set X to initial values
21 X = speValues;
22
23 % matrix to hold propensity values, number of constant species
24 speConstIndeciesLength = length(speConstIndecies);
25 A = zeros(numReactions,1);
26
27 % extract V from VHolder and display
28 V = VHolder.V;
29 if verbose_flag
       disp( sprintf('\nStoichiometric Matrix:\n') ); disp(V);
30
31 end
32
33 num_cores = feature('numCores');
34
35 if verbose_flag
       disp( sprintf('\nDetected %d CPU cores\n', num_cores) );
36
37 end
38
39 %Y = zeros(numMaxDataPoints, numSpecies);
40 Y = zeros(numSpecies, numSteps, numMaxDataPoints);
41 %time = zeros(1, numMaxDataPoints);
42
43 % begin SSA algorithm
44
45 if verbose_flag
        disp( sprintf('\n========= STARTING SSA FOR HISTOGRAM ========== ' ) );
46
        disp( sprintf( 'Remember - this part takes a while. Please be patient.\n') );
47
48 end
49
50 \text{ halt_flag} = 0;
51 time = linspace(0,tfinal,numSteps);
52 interval = tfinal/numSteps;
53
54 parfor l = 1:numMaxDataPoints
55
56
        % initial values
57
       t = 0;
```

```
58
        n = 2;
 59
        X = speValues;
 60
        A = zeros(numReactions,1);
 61
        Y_sub = zeros(numSpecies, numSteps);
 62
        Y_{sub}(:,1) = X;
 63
 64
        while n <= numSteps</pre>
 65
 66
            next step = (n-1)*interval;
 67
 68
            % calculate value of each propensity at that step
 69
 70
            A = calculatePropensities(X);
 71
 72
 73
            asum = sum(A);
 74
 75
            % break out of simulation if all species are consumed
 76
            if asum == 0
 77
                 halt_flag = 1;
 78
                 break
 79
            end
 80
 81
            j = find( rand < cumsum(A/asum) , 1 );</pre>
 82
            tau = log(1/rand)/asum;
 83
 84
            X = X + V(:,j);
 85
 86
 87
            X = calculateSpecifiedTotals(X);
 88
 89
 90
            for i = 1:speConstIndeciesLength
 91
                 X(speConstIndecies(i)) = speValues(speConstIndecies(i));
 92
            end
 93
 94
            t = t + tau;
 95
            if t > next_step
 96
 97
                Y_sub(:,n) = X';
 98
                 n = n + 1;
 99
            end
100
        end
101
102
103
        Y(:,:,l) = Y_sub;
104
105 end
106
107 if halt_flag && verbose_flag
        disp(sprintf('\n=======REACTION HALTED - ALL SPECIES COMSUMED=======\n'));
108
109 end
110
111 if verbose_flag
112
        disp(' ');
113 end
114
115 Y_last = zeros(numMaxDataPoints, numSpecies);
```

```
116
117 % get means, standard deviations, last slice data
            = zeros(numSpecies, numSteps);
119 Std
            = zeros(numSpecies, numSteps);
120 for i = 1:numSpecies
121
        for j = 1:numSteps
122
            data = Y(i,j,:);
123
            if j == numSteps
124
                Y_{last(:,i)} = data;
125
            end
126
            Mean(i,j) = mean(data);
            Std(i,j) = std(data);
127
128
        end
129 end
131 specific_species_flag = 0;
132
133 if ~isempty(speciesToGraph)
134
        stop_point = length(speciesToGraph);
135
        specific_species_flag = 1;
136 else
137
        stop_point = numSpecies;
138 end
139
140 warning('off', 'MATLAB:legend:IgnoringExtraEntries');
141
142 if graph_flag
143
        for i = 1:stop point
144
            if specific_species_flag
                index = speciesToGraph(i);
145
146
            else
147
                index = i;
148
            end
149
150
            data = zeros(numSteps, numMaxDataPoints);
151
            data(1:numSteps,1:numMaxDataPoints) = Y(index,:,:);
152
            data = data';
153
154
            figure;
155
            % graph boxplot for each slice
156
            subplot(2,1,1);
157
            boxplot( data , time, 'plotstyle', 'compact');
158
            legend( findobj(gca,'Tag','Box'),speNames(index) );
159
            xlabel('Time','FontSize',12, 'FontName', 'Helvetica');
160
            ylabel('Number of Species','FontSize',12,'FontName', 'Helvetica');
161
162
            title('Box and whisker plot of species vs time at given intervals','FontSize','
16, 'FontName', 'Helvetica');
163
            % graph means +- standard deviations for each slice
164
165
            subplot(2,1,2);
166
            hold all
            plot( time, Mean(index,:), 'b-o');
167
168
            plot( time, Mean(index,:) - Std(index,:), 'c');
169
            plot( time, Mean(index,:) + Std(index,:), 'c');
            legend( findobj(gca, 'Tag', 'Box'), speNames(index) );
170
            xlabel('Time', 'FontSize', 12, 'FontName', 'Helvetica');
171
            ylabel('Number of Species', 'FontSize', 12, 'FontName', 'Helvetica');
172
```

```
title('Box and whisker plot of species vs time at given intervals', 'FontSize', ∠
173
16, 'FontName', 'Helvetica');
174
        end
175 end
176
177 Mean_last = Mean(:,numSteps);
178 Std_dev_last = Std(:,numSteps);
179
180 varargout{1} = Y_last;
181 varargout{2} = Mean;
182 varargout{3} = Std;
183
184 if verbose_flag
        dataTableMean = table(Mean_last, 'RowNames', speNames);
185
        disp(dataTableMean);
        dataTableStddev = table(Std_dev_last, 'RowNames', speNames);
187
188
        disp(dataTableStddev);
189 end
190
191 end
```

```
1 function varargout = SSAGen_parfor_cle(SysInf, tfinal, recordStep, verbose_flag, tau, ∠
speciesToGraph, numSteps, graph flag)
                      = SysInf.numSpecies;
 3 numSpecies
 4 numReactions
                      = SysInf.numReactions;
                      = SysInf.speNames;
 5 speNames
                      = SysInf.speValues;
 6 speValues
 7 cNames
                      = SysInf.cNames;
 8 cValues
                      = SysInf.cValues;
 9 speConstIndecies = SysInf.speConstIndecies;
                      = SysInf.totalsIndecies;
10 totalsIndecies
11 VHolder
                      = SysInf.VHolder;
12
13 if verbose_flag
14
        disp(' ');
15 end
16
17 % set max muber of data points for each chunk of the recorded values matrix
18 numMaxDataPoints = 10008;
19
20 % set X to initial values
21 X = speValues;
22
23 % matrix to hold propensity values, number of constant species
24 speConstIndeciesLength = length(speConstIndecies);
25 A = zeros(numReactions,1);
26
27 % extract V from VHolder and display
28 V = VHolder.V;
29 if verbose_flag
       disp( sprintf('\nStoichiometric Matrix:\n') ); disp(V);
30
31 end
32
33 if tau == 0
       % Single SSA trajectory to help determine good tau
        [Y, X, time, run_time] = SingleTrajectory(V, X, speConstIndecies, numSpecies, speValues, ∠
tfinal, recordStep, verbose_flag);
        tau = ( time(length(time)) / ( length(time)*recordStep ) ) * 3;
37 end
38
39 num_cores = feature('numCores');
41 if verbose flag
        disp( sprintf('\nDetected %d CPU cores\n', num_cores) );
42
43 end
44
45 %Y = zeros(numMaxDataPoints, numSpecies);
46 Y = zeros(numSpecies, numSteps, numMaxDataPoints);
47 %time = zeros(1, numMaxDataPoints);
48
49 % begin SSA with tau-leaping algorithm
50
51 if verbose_flag
       disp( sprintf('\n========== STARTING parallel SSA with tau-leaping ============
52
);
53
        disp( sprintf( 'Remember - this part takes a while. Please be patient.\n') );
54 end
55
```

```
56 halt_flag = 0;
 57 time = linspace(0,tfinal,numSteps);
 58 interval = tfinal/numSteps;
 59
 60 parfor l = 1:numMaxDataPoints
 61
 62
        % initial values
        t = 0;
 63
 64
        n = 2;
 65
        X = speValues;
        A = zeros(numReactions,1);
 66
 67
        Y_sub = zeros(numSpecies, numSteps);
 68
        Y_{sub}(:,1) = X;
 69
 70
        while n <= numSteps</pre>
 71
 72
            next_step = (n-1)*interval;
 73
 74
 75
            % calculate value of each propensity at that step
 76
            A = calculatePropensities(X);
 77
 78
 79
            asum = sum(A);
 80
 81
            % break out of simulation if all species are consumed
 82
            if asum == 0
 83
                halt_flag = 1;
 84
                break
 85
            end
 86
 87
            % get sampling of random variables and sub into CLE formula
 88
            d = tau*A + sqrt( abs(tau*A) ) * randn;
 89
 90
            % update values
 91
            X = X + V * d';
 92
 93
 94
            X = calculateSpecifiedTotals(X);
 95
 96
 97
            for i = 1:speConstIndeciesLength
 98
                X(speConstIndecies(i)) = speValues(speConstIndecies(i));
 99
            end
100
101
            t = t + tau;
102
103
            if t > next_step
                Y_sub(:,n) = X';
104
105
                n = n + 1;
106
            end
107
108
        end
109
        Y(:,:,l) = Y_sub;
110
111
112 end
113
```

```
114 if halt_flag && verbose_flag
        disp(sprintf('\n=======REACTION HALTED - ALL SPECIES COMSUMED=======\n'));
116 end
117
118 if verbose_flag
        disp(' ');
119
120 end
121
122 Y last = zeros(numMaxDataPoints, numSpecies);
124 % get means, standard deviations, last slice data
            = zeros(numSpecies, numSteps);
126 Std
            = zeros(numSpecies, numSteps);
127 for i = 1:numSpecies
        for j = 1:numSteps
129
            data = Y(i,j,:);
130
            if j == numSteps
131
                Y_{last(:,i)} = data;
132
            end
133
            Mean(i,j) = mean(data);
134
            Std(i,j) = std(data);
135
        end
136 end
137
138 specific_species_flag = 0;
139
140 if ~isempty(speciesToGraph)
141
        stop point = length(speciesToGraph);
142
        specific_species_flag = 1;
143 else
        stop_point = numSpecies;
144
145 end
146
147 warning('off', 'MATLAB:legend:IgnoringExtraEntries');
148
149 if graph_flag
150
        for i = 1:stop_point
151
            if specific_species_flag
                index = speciesToGraph(i);
152
153
            else
                index = i;
154
155
            end
156
            data = zeros(numSteps, numMaxDataPoints);
157
158
            data(1:numSteps,1:numMaxDataPoints) = Y(index,:,:);
159
            data = data';
160
161
            figure;
162
            % graph boxplot for each slice
163
164
            subplot(2,1,1);
            boxplot( data , time, 'plotstyle', 'compact');
165
            legend( findobj(gca,'Tag','Box'),speNames(index) );
166
            xlabel('Time', 'FontSize', 12, 'FontName', 'Helvetica');
167
            ylabel('Number of Species', 'FontSize', 12, 'FontName', 'Helvetica');
169
            title('Box and whisker plot of species vs time at given intervals','FontSize', ∠
16, 'FontName', 'Helvetica');
170
```

```
171
            % graph means +- standard deviations for each slice
172
            subplot(2,1,2);
            hold all
173
            plot( time, Mean(index,:), 'b-o');
174
            plot( time, Mean(index,:) - Std(index,:), 'c');
175
176
            plot( time, Mean(index,:) + Std(index,:), 'c');
            legend( findobj(gca,'Tag','Box'),speNames(index) );
177
            xlabel('Time', 'FontSize', 12, 'FontName', 'Helvetica');
178
            ylabel('Number of Species', 'FontSize', 12, 'FontName', 'Helvetica');
179
            title('Box and whisker plot of species vs time at given intervals','FontSize', ∠
180
16, 'FontName', 'Helvetica');
181
        end
182 end
183
184 Mean last = Mean(:,numSteps);
185 Std_dev_last = Std(:,numSteps);
186
187 varargout{1} = Y_last;
188 varargout{2} = Mean;
189 varargout{3} = Std;
190
191 if verbose_flag
        dataTableMean = table(Mean_last, 'RowNames', speNames);
192
193
        disp(dataTableMean);
194
        dataTableStddev = table(Std_dev_last, 'RowNames', speNames);
195
        disp(dataTableStddev);
196 end
197
198 end
```

```
1 function varargout = SSAGen_parfor_tauleap(SysInf, tfinal, recordStep, verbose_flag, tau, ✓
speciesToGraph, numSteps, graph flag, num traj)
                     = SysInf.numSpecies;
 3 numSpecies
 4 numReactions
                     = SysInf.numReactions;
                    = SysInf.speNames;
 5 speNames
                    = SysInf.speValues;
 6 speValues
 7 cNames
                     = SysInf.cNames;
 8 cValues
                     = SysInf.cValues;
 9 speConstIndecies = SysInf.speConstIndecies;
                    = SysInf.totalsIndecies;
10 totalsIndecies
11 VHolder
                     = SysInf.VHolder;
12
13 if verbose_flag
14
       disp(' ');
15 end
16
17 % set max muber of data points for each chunk of the recorded values matrix
18 if num_traj == 0
19
       numMaxDataPoints = 10008;
20 else
21
       numMaxDataPoints = num_traj;
22
23 % set X to initial values
24 X = speValues;
25
26 % matrix to hold propensity values, number of constant species
27 speConstIndeciesLength = length(speConstIndecies);
28 A = zeros(numReactions,1);
29
30 % extract V from VHolder and display
31 V = VHolder.V;
32 if verbose_flag
33
       disp( sprintf('\nStoichiometric Matrix:\n') ); disp(V);
34 end
35
36 if tau == 0
       % Single SSA trajectory to help determine good tau
       [Y, X, time, run_time] = SingleTrajectory(V, X, speConstIndecies, numSpecies, speValues, ∠
tfinal, recordStep, verbose_flag);
       tau = ( time(length(time)) / ( length(time)*recordStep ) ) * 3;
39
40 end
41
42 num_cores = feature('numCores');
43
44 if verbose_flag
45
       disp( sprintf('\nDetected %d CPU cores\n', num_cores) );
46 end
47
48 %Y = zeros(numMaxDataPoints, numSpecies);
49 Y = zeros(numSpecies, numSteps, numMaxDataPoints);
50 %time = zeros(1, numMaxDataPoints);
51
52 % begin SSA with tau-leaping algorithm
53
54 if verbose flag
55
       );
```

```
56
        disp( sprintf( 'Remember - this part takes a while. Please be patient.\n') );
 57 end
 58
 59 halt_flag = 0;
 60 time = linspace(0,tfinal,numSteps);
 61 interval = tfinal/numSteps;
 63 parfor l = 1:numMaxDataPoints
 64
 65
        % initial values
        t = 0;
 66
 67
        n = 2;
        X = speValues;
 68
        A = zeros(numReactions,1);
 69
 70
        Y_sub = zeros(numSpecies, numSteps);
 71
        Y_{sub}(:,1) = X;
 72
 73
        while n <= numSteps</pre>
 74
 75
            next_step = (n-1)*interval;
 76
 77
            % calculate value of each propensity at that step
 78
 79
            A = calculatePropensities(X);
 80
 81
 82
            asum = sum(A);
 83
 84
            % break out of simulation if all species are consumed
 85
            if asum == 0
                halt_flag = 1;
 86
 87
                break
 88
            end
 89
            % get sampling of poisson random variables
 90
            pois_rand_vars = poissrnd(A*tau);
 91
 92
 93
            % update values
 94
            X = X + V * pois_rand_vars';
 95
 96
 97
            X = calculateSpecifiedTotals(X);
 98
            %_--
 99
            for i = 1:speConstIndeciesLength
100
                X(speConstIndecies(i)) = speValues(speConstIndecies(i));
101
102
            end
103
            t = t + tau;
104
105
            if t > next_step
106
107
                Y_sub(:,n) = X';
108
                n = n + 1;
109
            end
110
111
        end
112
113
        Y(:,:,l) = Y_sub;
```

```
114
115 end
116
117 if halt_flag && verbose_flag
118
        disp(sprintf('\n=======REACTION HALTED - ALL SPECIES COMSUMED=======\n'));
119 end
120
121 if verbose flag
        disp(' ');
122
123 end
124
125 Y_last = zeros(numMaxDataPoints, numSpecies);
126
127 % get means, standard deviations, last slice data
128 Mean
            = zeros(numSpecies, numSteps);
129 Std
            = zeros(numSpecies, numSteps);
130 for i = 1:numSpecies
131
        for j = 1:numSteps
132
            data = Y(i,j,:);
133
            if j == numSteps
134
                Y_{last(:,i)} = data;
135
136
            Mean(i,j) = mean(data);
137
            Std(i,j) = std(data);
138
        end
139 end
140
141 specific_species_flag = 0;
143 if ~isempty(speciesToGraph)
144
        stop_point = length(speciesToGraph);
145
        specific_species_flag = 1;
146 else
147
        stop_point = numSpecies;
148 end
149
150 warning('off', 'MATLAB:legend:IgnoringExtraEntries');
151
152 if graph_flag
        for i = 1:stop_point
153
154
            if specific_species_flag
                index = speciesToGraph(i);
155
156
            else
157
                index = i;
158
            end
159
160
            data = zeros(numSteps, numMaxDataPoints);
161
            data(1:numSteps,1:numMaxDataPoints) = Y(index,:,:);
162
            data = data';
163
164
            figure;
165
166
            % graph boxplot for each slice
167
            subplot(2,1,1);
168
            boxplot( data , time, 'plotstyle', 'compact');
            legend( findobj(gca, 'Tag', 'Box'), speNames(index) );
169
            xlabel('Time', 'FontSize', 12, 'FontName', 'Helvetica');
170
            ylabel('Number of Species','FontSize',12,'FontName', 'Helvetica');
171
```

```
title('Box and whisker plot of species vs time at given intervals','FontSize', ∠
172
16, 'FontName', 'Helvetica');
173
            % graph means +- standard deviations for each slice
174
175
            subplot(2,1,2);
176
            hold all
            plot( time, Mean(index,:), 'b-o');
177
            plot( time, Mean(index,:) - Std(index,:), 'c');
178
            plot( time, Mean(index,:) + Std(index,:), 'c');
179
            legend( findobj(gca, 'Tag', 'Box'), speNames(index) );
180
            xlabel('Time', 'FontSize', 12, 'FontName', 'Helvetica');
181
            ylabel('Number of Species','FontSize',12,'FontName', 'Helvetica');
182
            title('Box and whisker plot of species vs time at given intervals','FontSize', ∠
183
16, 'FontName', 'Helvetica');
184
        end
185 end
186
187 Mean_last = Mean(:,numSteps);
188 Std_dev_last = Std(:,numSteps);
189
190 varargout{1} = Y_last;
191 varargout{2} = Mean;
192 varargout{3} = Std;
193
194 if verbose flag
        dataTableMean = table(Mean_last, 'RowNames', speNames);
195
196
        disp(dataTableMean);
        dataTableStddev = table(Std dev last, 'RowNames', speNames);
197
        disp(dataTableStddev);
198
199 end
200
201 end
```

```
1 function [time, Y] = SSAGen(SysInf, tfinal, recordStep, verbose_flag, tau)
                     = SysInf.numSpecies;
 3 numSpecies
 4 numReactions
                     = SysInf.numReactions;
 5 speNames
                     = SysInf.speNames;
 6 speValues
                     = SysInf.speValues;
 7 cNames
                     = SysInf.cNames;
 8 cValues
                     = SysInf.cValues;
9 speConstIndecies = SysInf.speConstIndecies;
10 totalsIndecies
                     = SysInf.totalsIndecies;
11 VHolder
                     = SysInf.VHolder;
12
13 % initial values
14 X = speValues;
16 % extract V from VHolder and display
17 V = VHolder.V;
18 if verbose_flag
       disp( sprintf('Stoichiometric Matrix:\n') ); disp(V);
19
20 end
21
22 % attempt to pick tau if not specified - *extremely* crude estimate
23 if tau == 0
24
       % Single SSA trajectory to help determine good tau
25
       [Y, X, time, run_time] = SingleTrajectory(V, X, speConstIndecies, numSpecies, speValues, ∠
tfinal, recordStep, verbose_flag);
       tau = ( time(length(time)) / ( length(time)*recordStep ) ) * 3;
26
27 end
28
29 disp( sprintf('Chosen value for tau:\n') ); disp(tau);
30
31 X = speValues;
32
33 tic
34 [Y, X, time, run_time] = SingleTrajectory_tauleap(V, X, speConstIndecies, numSpecies, ⊬
speValues, tfinal, recordStep, verbose_flag, tau);
35 time_with_leap = toc;
36
37 if verbose_flag
       disp(sprintf('\nSpecies'' final amounts:\n'));
38
39
       Amount = X;
40
       dataTable = table(Amount, 'RowNames', speNames);
41
       disp(dataTable);
42 end
43
44 if verbose_flag
45
       disp(' ');
46 end
47
48 end
```

```
1 classdef StoichiometricMatricesHolder
 2
 3
       properties
 4
           ۷;
 5
           vNumOfReactant;
 6
           vReactant;
 7
           vDimerMap;
 8
       end
 9
10
       methods
11
12
           function object = StoichiometricMatricesHolder(SBMLModel)
13
14
                numReactions = length(SBMLModel.reaction);
15
                numSpecies = length(SBMLModel.species);
16
17
                % get the stoichiometric matrix representing the species changes for each reactionoldsymbol{arepsilon}
from the model
18
                V = zeros(numSpecies, numReactions);
19
20
                % matricies to hold the number of reactants in each reaction, the reactants'arksim
indecies, and the dimer map
21
                vNumOfReactant = zeros(numReactions,1);
22
                vReactant = zeros(numReactions, numSpecies);
23
                vDimerMap = zeros(numSpecies, numReactions);
24
25
                maxCount = 0;
26
27
                for j = 1:numReactions
28
29
                    count = 0;
30
                    for i = 1:numSpecies
31
32
                        role = DetermineSpeciesRoleInReaction(SBMLModel.species(i), SBMLModel.

∠
reaction(j));
                        if length(role) > 1
33
34
                             V(i,j) = role(1) - role(2);
35
36
                             if role(2) > 0
37
                                 vReactant( j , (count+1) ) = i;
38
39
                                 count = count + 1;
40
                             end
41
                             if role(2) >= 2
42
43
                                 vDimerMap(i,j) = role(2);
44
                             end
45
                        else
46
                             V(i,j) = 0;
47
                        end
                    end
48
49
50
                    vNumOfReactant(j) = count;
51
52
                    if count > maxCount
53
                        maxCount = count;
54
                    end
55
```

```
56
               end
57
58
               object.V = V;
59
               object.vNumOfReactant = vNumOfReactant;
60
               % truncate reactant index matrix to discard unnecessary elements
61
               object.vReactant = vReactant( : , 1:(maxCount) );
62
63
               % make dimer reactant matrix sparse to discard unnecessary elements
64
65
               object.vDimerMap = vDimerMap;
66
67
           end
68
69
       end
70
71 end
```

```
1 classdef SystemInformationHolder
 3
       properties
 4
           numSpecies;
5
6
7
           numReactions;
           speNames;
           speValues;
8
           cNames;
9
           cValues;
           speConstIndecies;
10
           totalsIndecies;
11
12
           VHolder;
13
       end
14
15 end
```