

CSCE 452 Project 1 Report

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Deriving Forward Kinematics

Link lengths and angles

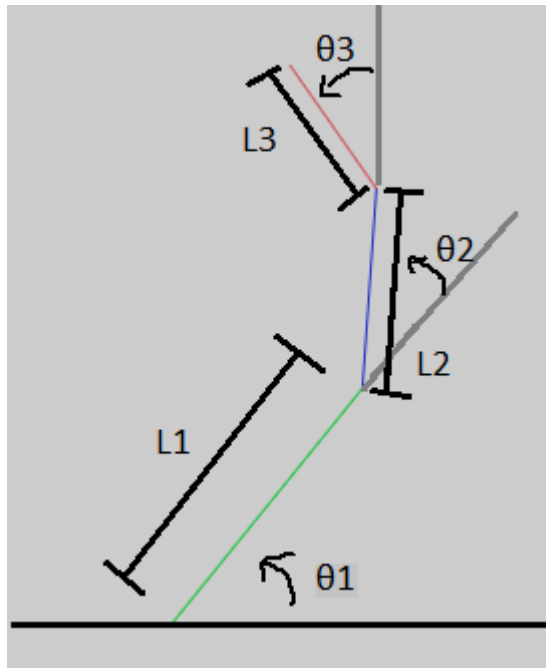


Figure 1: Shows the link lengths and the angles for the paintbot

Frame Attachment

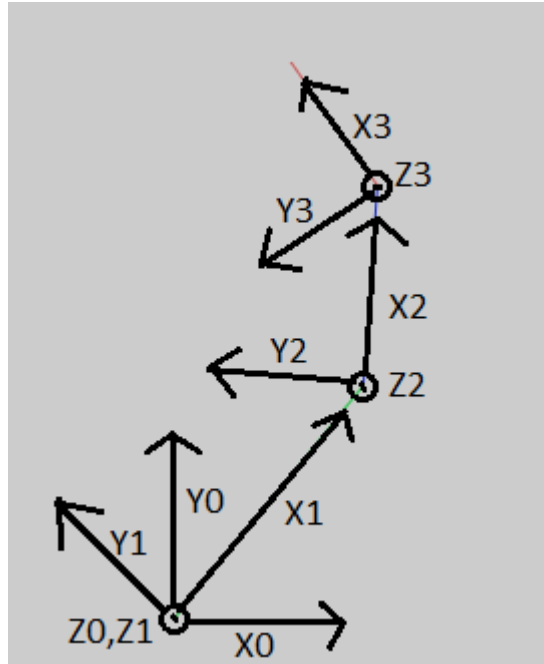


Figure 2: Shows the correct frame attachments for the paintbot. It shows the x,y, and z for each frame. Note that the circle with a dot denotes that the axle is pointing outside of the page

Link Parameters

i	α_{i-1}	a_{i-1}	d_i	θ_i
1	0	0	0	θ_1
2	0			θ_2
3	0	0	0	θ_3

Figure 3: Shows the link parameters for i one through 3 on the paintbot.

T Matrices for Each Link

$${}^0T_1 = \begin{bmatrix} \cos \theta_1 & -\sin \theta_1 & 0 & 0 \\ \sin \theta_1 & \cos \theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^1_2T = \begin{bmatrix} \cos \theta_2 & -\sin \theta_2 & 0 & L_1 \\ \sin \theta_2 & \cos \theta_2 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^2_3T = \begin{bmatrix} \cos \theta_3 & -\sin \theta_3 & 0 & L_2 \\ \sin \theta_3 & \cos \theta_3 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Correct Angles from Handout One

Euler Angles

There is one incorrect angle set given. The rest are correct.

$$\begin{aligned} \text{Euler XYZ} & \begin{bmatrix} \cos \beta \cos y & -\cos \beta \sin y & \sin \beta \\ \sin \alpha \sin \beta \cos y + \cos \alpha \sin y & -\sin \alpha \sin \beta \sin y + \cos \alpha \cos y & -\sin \alpha \cos \beta \\ -\cos \alpha \sin \beta \cos y + \sin \alpha \sin y & \cos \alpha \sin \beta \sin y + \sin \alpha \cos y & \cos \alpha \cos \beta \end{bmatrix} \\ \text{Euler XZY} & \begin{bmatrix} \cos \beta \cos y & -\sin \beta & \cos \beta \sin y \\ \cos \alpha \sin \beta \sin y + \sin \alpha \sin y & \cos \alpha \cos \beta & \cos \alpha \sin \beta \sin y - \sin \alpha \cos y \\ \sin \alpha \sin \beta \cos y - \cos \alpha \sin y & \sin \alpha \cos \beta & \sin \alpha \sin \beta \sin y + \cos \alpha \cos y \end{bmatrix} \\ \text{Euler YXZ} & \begin{bmatrix} \sin \alpha \sin \beta \sin y + \cos \alpha \cos y & \sin \alpha \sin \beta \cos y - \cos \alpha \sin y & \sin \alpha \cos \beta \\ \cos \beta \sin y & \cos \beta \cos y & -\sin \beta \\ \cos \alpha \sin \beta \sin y - \sin \alpha \cos y & \cos \alpha \sin \beta \cos y + \sin \alpha \sin y & \cos \alpha \cos \beta \end{bmatrix} \\ \text{Euler YZX} & \begin{bmatrix} \cos \alpha \cos \beta & -\cos \alpha \sin \beta \cos y + \sin \alpha \sin y & \cos \alpha \sin \beta \sin y + \sin \alpha \cos y \\ \sin \beta & \cos \beta \cos y & -\cos \beta \sin y \\ -\sin \alpha \cos \beta & \sin \alpha \sin \beta \cos y + \cos \alpha \sin y & -\sin \alpha \sin \beta \sin y + \cos \alpha \cos y \end{bmatrix} \\ \text{Euler ZXY} & \begin{bmatrix} -\sin \alpha \sin \beta \sin y + \cos \alpha \cos y & -\sin \alpha \cos \beta & \sin \alpha \sin \beta \cos y + \cos \alpha \sin y \\ \cos \alpha \sin \beta \sin y + \sin \alpha \cos y & \cos \alpha \cos \beta & -\cos \alpha \sin \beta \cos y + \sin \alpha \sin y \\ -\cos \beta \sin y & \sin \beta & \cos \beta \cos y \end{bmatrix} \\ \text{Euler ZYX} & \begin{bmatrix} \cos \alpha \cos \beta & \cos \alpha \sin \beta \sin y - \sin \alpha \cos y & \cos \alpha \sin \beta \cos y + \sin \alpha \sin y \\ \sin \alpha \cos \beta & -\sin \alpha \sin \beta \sin y + \cos \alpha \cos y & \sin \alpha \sin \beta \cos y - \cos \alpha \sin y \\ -\sin \beta & \cos \beta \sin y & \cos \beta \cos y \end{bmatrix} \end{aligned}$$

Note: This (ZYX) is incorrect on handout

$$\begin{aligned} \text{Euler YXY} & \begin{bmatrix} \cos \beta & \sin \beta \sin y & \sin \beta \cos y \\ \sin \alpha \sin \beta & -\sin \alpha \cos \beta \sin y + \cos \alpha \cos y & -\sin \alpha \cos \beta \cos y - \cos \alpha \sin y \\ -\cos \alpha \sin \beta & \cos \alpha \cos \beta \sin y + \sin \alpha \cos y & \cos \alpha \cos \beta \cos y - \sin \alpha \sin y \end{bmatrix} \\ \text{Euler XZX} & \begin{bmatrix} \cos \beta & -\sin \beta \cos y & \sin \beta \sin y \\ \cos \alpha \sin \beta & \cos \alpha \cos \beta \cos y - \sin \alpha \sin y & -\sin \alpha \cos y - \cos \alpha \cos \beta \sin y \\ \sin \alpha \sin \beta & \sin \alpha \cos \beta \cos y + \cos \alpha \sin y & -\sin \alpha \cos \beta \sin y + \cos \alpha \cos y \end{bmatrix} \\ \text{Euler YXY} & \begin{bmatrix} -\sin \alpha \cos \beta \sin y + \cos \alpha \cos y & \sin \alpha \sin \beta & \sin \alpha \cos \beta \cos y + \cos \alpha \sin y \\ \sin \beta \sin y & \cos \beta & -\sin \beta \cos y \\ -\cos \alpha \cos \beta \sin y - \sin \alpha \cos y & \cos \alpha \sin \beta & +\cos \alpha \cos \beta \cos y - \sin \alpha \sin y \end{bmatrix} \end{aligned}$$

$$\begin{aligned}
\mathbf{Euler\ YZY} & \begin{bmatrix} \cos \alpha \cos \beta \cos y - \sin \alpha \sin y & -\cos \alpha \sin \beta & \cos \alpha \cos \beta \sin y + \sin \alpha \cos y \\ \sin \beta \cos y & \cos \beta & \sin \beta \sin y \\ -\sin \alpha \cos \beta \cos y - \cos \alpha \sin y & \sin \alpha \sin \beta & -\sin \alpha \cos \beta \sin y + \cos \alpha \cos y \end{bmatrix} \\
\mathbf{Euler\ ZXZ} & \begin{bmatrix} -\sin \alpha \cos \beta \sin y + \cos \alpha \cos y & -\sin \alpha \cos \beta \cos y - \cos \alpha \sin y & \sin \alpha \sin \beta \\ \cos \alpha \cos \beta \sin y + \sin \alpha \cos y & \cos \alpha \cos \beta \cos y - \sin \alpha \sin y & -\cos \beta \\ \sin \beta \sin y & \sin \beta \cos y & \cos \beta \end{bmatrix}
\end{aligned}$$

Fixed Angles

All provided Fixed Angles are correct