

HW3 约束优化

Task I 严格凸的等式约束 QP 的 KKT 推导和求解

见第 3 章第 9 节视频最后

Task II 低维度严格凸 QP 线性时间复杂度算法的补全（投影子问题的构建，Householder 反射）

在 sdqp.hpp 文件中，按照提示补全以下代码。

```
155     for (int i = 0; i != m; i = next[i])
156     {
157         const double *plane_i = halves + (d + 1) * i;
158
159         if (dot<d>(opt, plane_i) + plane_i[d] > (d + 1) * eps)
160         {
161             const double s = sqrt_norm<d>(plane_i);
162
163             if (s < (d + 1) * eps * eps)
164             {
165                 return INFEASIBLE;
166             }
167
168             mul<d>(plane_i, -plane_i[d] / s, new_origin);
169
170             if (i == 0)
171             {
172                 continue;
173             }
174
175             /////////////////////////////////////////////////// HOMEWORK START ///////////////////////////////////
176             //
177             // MISSION TO BE ACCOMPLISHED:
178             //
179             // now we know the best solution "opt" violates the i-th halfspace. Therefore,
180             // please project all previous i halfspaces (from the 0-th to the (i-1)-th one)
181             // onto the boundary of the i-th halfspace, then store all projected halfspaces
182             // in the double-type-c-array "new_halves".
183             // If you successfully complete the mission, the sdqp_example should prints
184             //   optimal sol: 4.11111 9.15556 4.50022
185             //   optimal obj: 201.14
186             //   cons precision: *.*****e-16
187             // This means you obtained the correct exact solution (precision near DBL_EPSILON)
188             //
189             // VARIABLES YOU NEED TO ACCESS:
190             //
191             // opt is a d-dimensional double-type-c-array
192             // opt contains an optimal solution that meets all linear constraints from the 0-th
193             // to the (i-1)-th one, but it is known to violate the i-th halfspace here
194             //
195             // new_origin is also a d-dimensional double-type-c-array
196             // new_origin contains the minimum norm point on the boundary of the i-th plane
197             //
198             // you can read all previous halfspaces via the iteration below
199             //
200             for (int j = 0; j != i; j = next[j])
201             {
202                 const double *halfspace = halves + (d + 1) * j;
203                 // thus the j-th halfspace is the inequality below
204                 // halfspace[0] * x1 + halfspace[1] * x2 + ... + halfspace[d-1] * xd + halfspace[d] <= 0
205             }
206             //
207             // you can write or store all your projected halfspaces via the iteration below
208             //
209             for (int j = 0; j != i; j = next[j])
210             {
211                 double *proj_halfspace = new_halves + d * j;
212                 // thus the j-th projected halfspace is the inequality below
213                 // proj_halfspace[0] * y1 + proj_halfspace[1] * y2 + ... + proj_halfspace[d-2] * y(d-1) + proj_halfspace[d-1] <= 0
214                 // y1 to y(d-1) is the new coordinate constructed on the boundary of the i-th halfspace
215             }
216             //
217         }
```

Task III 用 PHR-ALM 方法求解 NMPC（已给出 penalty 方法求解的范例，修改求解器即可）

Step1: Run the solveNMPC example in mpc-car-tutorial-master.zip;

Step2: Use PHR-ALM to replace the Penalty Method in solveNMPC;

Step3: Compare the constrain violation in Penalty Method and PHR-ALM.