## Problem Set 8

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## 1 Question 9: lm() Regression Table

Table 1:

| -                       | Table 1.                               |  |
|-------------------------|--|--|
|                         | Dependent variable:                    |  |
|                         | Y                                      |  |
| X1                      | 1.501***                               |  |
|                         | (0.002)                                |  |
| X2                      | -0.996***                              |  |
|                         | (0.002)                                |  |
| X3                      | -0.249***                              |  |
|                         | (0.002)                                |  |
| X4                      | 0.747***                               |  |
|                         | (0.002)                                |  |
| X5                      | 3.502***                               |  |
|                         | (0.002)                                |  |
| X6                      | -1.999***                              |  |
|                         | (0.002)                                |  |
| X7                      | 0.501***                               |  |
|                         | (0.002)                                |  |
| X8                      | 0.999***                               |  |
|                         | (0.002)                                |  |
| X9                      | 1.253***                               |  |
|                         | (0.002)                                |  |
| X10                     | 1.999***                               |  |
|                         | (0.002)                                |  |
| Observations            | 100,000                                |  |
| $\mathbb{R}^2$          | 0.991                                  |  |
| Adjusted $\mathbb{R}^2$ | 0.991                                  |  |
| Residual Std. Error     | 0.500 (df = 99990)                     |  |
| F Statistic             | $1,080,712.000^{***}$ (df = 10; 99990) |  |
| Note:                   | *p<0.1; **p<0.05; ***p<0.01            |  |

#### 1.1

The True Betas and Estimated Betas are very similar, as you can see looking at the two tables there is a slight difference.

Table 2: True Values of Beta

| Index | Value |  |
|-------|-------|--|
| 1     | 1.5   |  |
| 2     | -1.0  |  |
| 3     | -0.25 |  |
| 4     | 0.75  |  |
| 5     | 3.5   |  |
| 6     | -2.0  |  |
| 7     | 0.5   |  |
| 8     | 1.0   |  |
| 9     | 1.25  |  |
| 10    | 2.0   |  |

### 2 Question 5: OLS estimate - Closed Form Solution

#### 2.1

Again, looking at the True Values of Beta in Table 2 and the estimated Beta Values in Table 3, there is only a slight difference.

Table 3: OLS Estimate (beta\_ols)

| $\operatorname{Index}$ | Value      |
|------------------------|------------|
| 1                      | 1.5005793  |
| 2                      | -0.9956182 |
| 3                      | -0.2486498 |
| 4                      | 0.7471903  |
| 5                      | 3.5017669  |
| 6                      | -1.9994365 |
| 7                      | 0.5011339  |
| 8                      | 0.9987400  |
| 9                      | 1.2528300  |
| 10                     | 1.9993846  |

# 3 Question 7: Compare Beta Estimates using the L-BFGS algorithm and Nelder-Mead algorithm.

#### 3.1

The Beta Estimates generated using the L-BFGS Algorithm (Table 4) are also very similar to the true Beta Values (Table 2).

#### 3.2

The estimates from the Nelder-Mead algorithm are somewhat different from the true values of beta and the estimates obtained using other methods

Table 4: L-BFGS Algorithm Estimates

| Index | Value      |
|-------|------------|
| 1     | 1.5005793  |
| 2     | -0.9956182 |
| 3     | -0.2486498 |
| 4     | 0.7471903  |
| 5     | 3.5017669  |
| 6     | -1.9994365 |
| 7     | 0.5011339  |
| 8     | 0.9987400  |
| 9     | 1.2528300  |
| 10    | 1.9993846  |

Table 5: Nelder-Mead Algorithm Estimates

| Index | Value      |
|-------|------------|
| 1     | 0.9767063  |
| 2     | -0.9680386 |
| 3     | -0.1361704 |
| 4     | 1.1277353  |
| 5     | 3.2668671  |
| 6     | -2.1447235 |
| 7     | 0.5663044  |
| 8     | 1.0422382  |
| 9     | 1.4966523  |
| 10    | 2.3011765  |