

2021-02-03-T.P.2

$$f_{act} = \text{sigmoide} \quad g_s(x) = \frac{1}{1+e^{-x}} \quad g'(x) = x \cdot (1-x)$$

$p = 1.0$
 $x = (-1, -1) \quad , \quad t = (1, 0)$

$$\Theta_1^1 = [1, -1, -1] \quad \Theta_1^2 = [1, -1] \quad \Theta_2^2 = [1, -1]$$

Notación extendida 1.0 $x = (1, -1, -1)$

salida
capa
oculta

$$\phi_1^1 = \Theta_1^1 \cdot x = 1 \cdot 1 + (-1) \cdot (-1) + (-1) \cdot (-1) = 3 \rightarrow S_1^1 = \frac{1}{1+e^{-3}} = 0.9525$$

salida
capa

$$\phi_1^2 = \Theta_1^2 \cdot S_1^1 = 1 \cdot 1 + (-1) \cdot 0.9525 = 0.0475 \rightarrow S_1^2 = \frac{1}{1+e^{-0.0475}} = 0.5118$$

salida

$$\phi_2^2 = \Theta_2^2 \cdot S_1^1 = 1 \cdot 1 + (-1) \cdot 0.9525 = 0.0475 \rightarrow S_2^2 = \frac{1}{1+e^{-0.0475}} = 0.5118$$

Resultado esperado $\rightarrow t = (1, 0)$

Cálculo error capa salida:

$$\delta_1^2 = (t_1 - S_1^2) \cdot S_1^2 (1 - S_1^2) = (1 - 0.5118) \cdot 0.5118 (1 - 0.5118) = 0.122$$

$$\delta_2^2 = (t_2 - S_2^2) \cdot S_2^2 (1 - S_2^2) = (0 - 0.5118) \cdot 0.5118 (1 - 0.5118) = -0.128$$

Cálculo error capa oculta:

$$\delta_1^1 = (\delta_1^2 \cdot \Theta_{11}^2 + \delta_2^2 \cdot \Theta_{21}^2) \cdot S_1^1 (1 - S_1^1) = (0.122 \cdot (-1) + (-0.128) \cdot (-1)) \cdot 0.9525 (1 - 0.9525) = 0.00027$$

Actualización pesos: Θ_{21}^2 y Θ_{22}^2

$$\Theta_{21}^2 = \Theta_{21}^2 + p \delta_1^1 X_2 = -1 + 1 \cdot 0.00027 \cdot (-1) = -1.00027$$

$$\Theta_{22}^2 = \Theta_{22}^2 + p \delta_1^1 X_2 = -1 + 1 \cdot 0.00027 \cdot (-1) = -1.00027$$