

## 2021\_01\_18\_Problema 1

Muestra no linealmente separable

i	1	2	3	4	5	6	7	8
$x_{i1}$	1	3	4	4	3	1	3	2
$x_{i2}$	4	2	1	3	1	2	3	3
Clase	+1	+1	-1	-1	-1	+1	+1	-1
$\alpha_i^*$	0.0	<span style="border: 1px solid black;">10.0</span> \$>0, C\$	0.0	<span style="border: 1px solid black;">6.0</span> \$>0, <C\$	<span style="border: 1px solid black;">6.4</span> \$>0, <C\$	<span style="border: 1px solid black;">2.4</span> \$>0, <C\$	<span style="border: 1px solid black;">10.0</span> \$>0\$	<span style="border: 1px solid black;">10.0</span> \$>0\$

FDL:

$$\Theta^* = C_2 \alpha_2^* X_2 + C_4 \alpha_4^* X_4 + C_5 \alpha_5^* X_5 + C_6 \alpha_6^* X_6 + C_7 \alpha_7^* X_7 + C_8 \alpha_8^* X_8$$

$$\Theta^* = \begin{pmatrix} (1 \cdot 10 \cdot 3 + -1 \cdot 6 \cdot 4 + -1 \cdot 6 \cdot 4 \cdot 3 + 1 \cdot 2 \cdot 4 \cdot 1 + 1 \cdot 10 \cdot 3 + -1 \cdot 10 \cdot 2), \\ (1 \cdot 10 \cdot 2 + -1 \cdot 6 \cdot 3 + -1 \cdot 6 \cdot 4 \cdot 1 + 1 \cdot 2 \cdot 4 \cdot 2 + 1 \cdot 10 \cdot 3 + -1 \cdot 10 \cdot 3) \end{pmatrix}$$

$$\Theta^* = (-0,2, 0,4)$$

$x_4$ , primera muestra que verifica  $\alpha_4^* > 0$  y  $\alpha_4^* < C$

Umbral:

$$\Theta_0^* = C_4 - \Theta^{*T} x_4 = -1 - (-0,2 \cdot 4 + 0,4 \cdot 3) = 1$$

Margen  $\Rightarrow \frac{1}{\|\Theta\|} + \frac{1}{\|\Theta\|} = \frac{2}{\|\Theta\|} = 2,23$

$$= 2 / \sqrt{0,2^2 + 0,4^2} = 2,23606$$

Frontera de separación (hiperplano separador):

$$y \Rightarrow -0,8x_1 + 0,4x_2 + 1 = 0 \begin{cases} \text{clase } +1 \\ + \\ \text{clase } -1 \end{cases}$$

Vectores Soportante:  $\mathcal{V} = \cancel{(2,3)^T}, (3,2)^T, (4,3)^T, (3,1)^T, (1,2)^T, (3,3)^T, (2,3)^T$

Tolerancia:

$$\zeta_1 = 0$$

no cumple  $\alpha \neq 1$   $\zeta_2 = 1 - C_2 (\theta^{*T} x_2 + \theta_0) = 1 - 1 \cdot (-0,8 \cdot 3 + 0,4 \cdot 2 + 1) = 1,6$

$$\zeta_3 = 0$$

$$\zeta_8 = 1 - 1(-0,8 \cdot 2 + 0,4 \cdot 3 + 1) = 1,6$$

$$\zeta_4 = 0$$

$$\zeta_{12} = 1 - 1(-0,8 \cdot 3 + 0,4 \cdot 3 + 1) = 1,2$$

$$\zeta_5 = 0$$

$$\zeta_6 = 0$$

Clasificación de  $(4,4)^T$ :

$$(-0,8 \cdot 4 + 0,4 \cdot 4) + 1 = -0,6 \rightarrow \text{clase } -1$$

