

Lidar and Scan Matching

By Derek Benham
-with ideas carried over from lectures by
Ryan Eustice and Joshua Mangelson

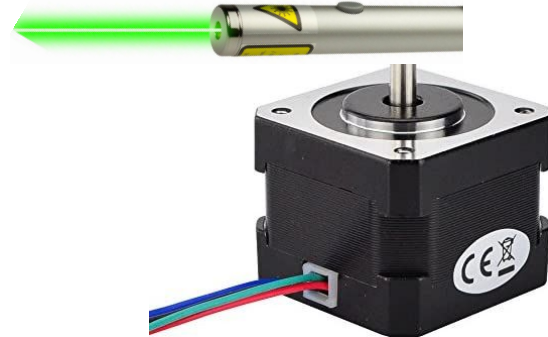
Topics to cover

- Popular scanners and Theory
- ICP Scan Matching
 - Correlation
 - Optimization
 - Error Rejection
- Information Theory in regards to error rejection

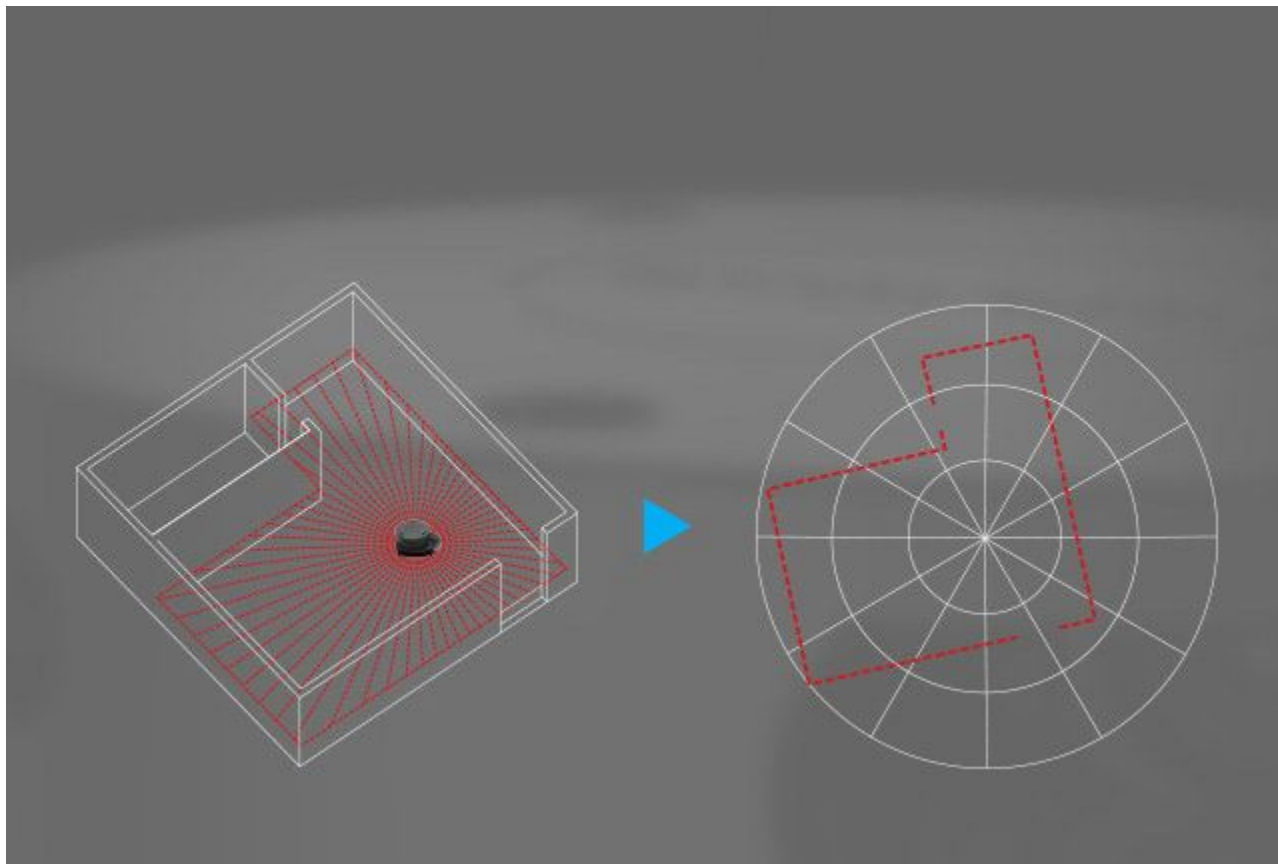
Popular scanners and Theory

Instead of a laser array, let's attach one laser to a motor and spin it!

Measure range via time of flight and pair with motor position



Popular scanners and Theory



Popular scanners and Theory

SICK LiDars

- Industrial safety
- 180 samples, 1 degree spacing, 75Hz
- Resolution $\sim 1\text{cm}$, $\sim 0.25\text{ deg}$.
- Interlacing
- Max range: “80m” 30m fairly reliable
- Intensity
- \$4500



Popular scanners and Theory

SLAMTEC RPLIDARS

A1:

- \$99
- 12m range
- 8,000 samples
- 5.5 HZ

A3:

- \$600
- 25m range
- 16,000 samples
- 15 HZ

RPLIDAR A1



RPLIDAR A3

360 Degree Laser Range Scanner for Indoor and Outdoor Application



Popular scanners and Theory

3D lidar scanners

Much more complicated than a 2D Lidar.

Gives a lot more data

Obviously more expensive

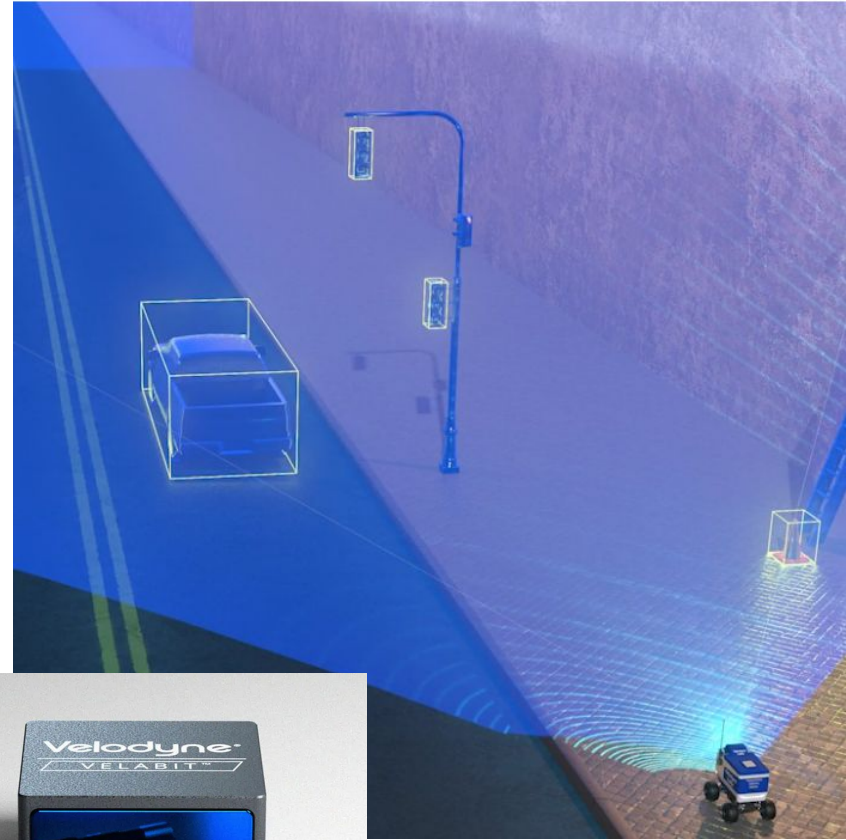
Beware of the dead zones near the sensor



Popular scanners and Theory

Velodyne Velabit: \$99

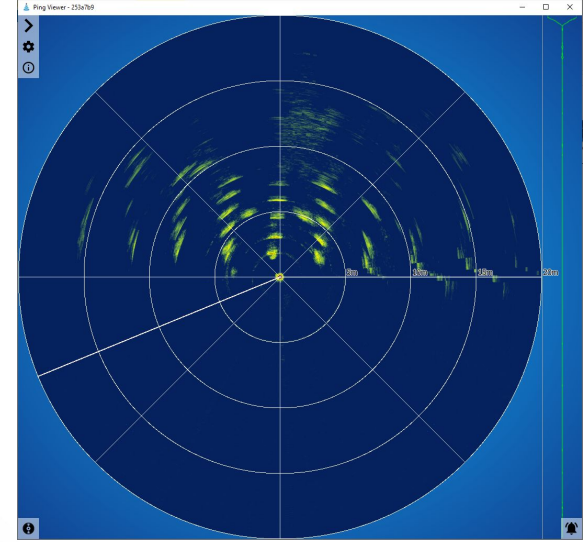
- horizontal (90°) and vertical (70°) field of view
- Small form factor: lightweight (125g) and compact (2.4" x 2.4" x 1.38") with integrated processing
- Range of up to 100 meters
- Low power consumption (3-6W)
- Expected to release Q1 2023



Popular scanners and Theory

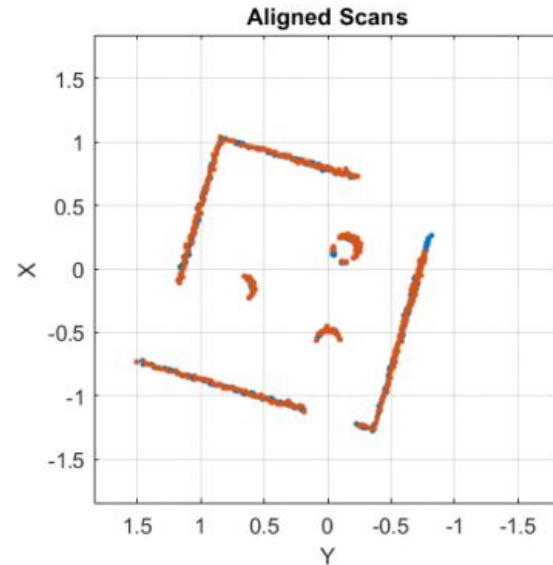
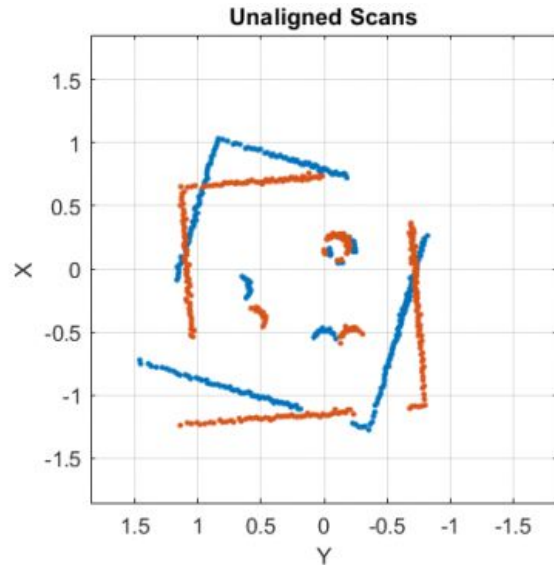
Ping 360 Scanning imaging sonar

- Shameless underwater robotics tie-in
- \$2,500
- 50m range
- Scan frequency dependent on desired scan distance (sound is slow)
- Scan speed
 - @2m: 9 secs/rotation
 - @50m: 35 secs/rotation



ICP Scan Matching: Purpose

- We can compute relative translation between scans
 - Replaces odometry
- Loop closing while running SLAM



ICP Scan Matching: Approach Overview

Two approaches:

- Feature based alignment
- Featureless based, correspondence alignment

ICP Scan Matching: Feature Extraction Approach

- Extract features from two scans
- Match features
- Computer Rigid body transformation

Possible Features

- Lines
- Corners
- Discontinuities

Intuition: Data compression by using features instead of every point makes optimization easier

ICP Scan Matching: Feature Extraction Approach

Issues:

- Difficult to implement
- Can be dependent on order of received points
- Computationally intensive

Tradeoffs between robustness and simplicity (including computationally)



ICP Scan Matching: Aligning scans without features:

Correlation-based scan matching

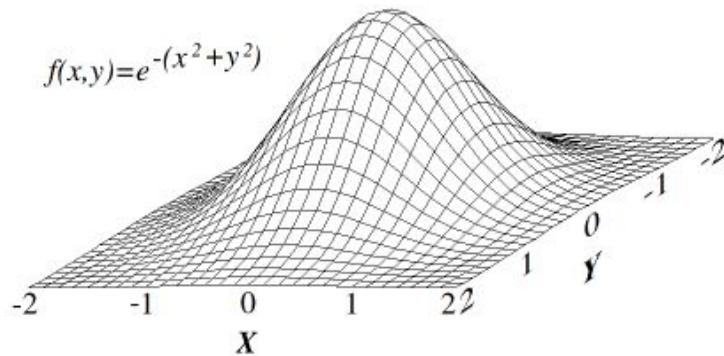
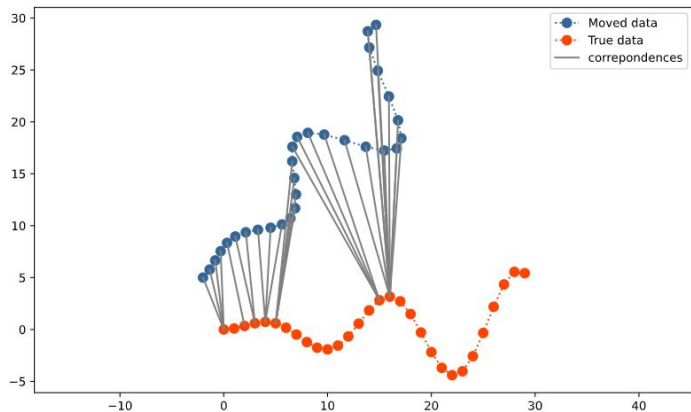
Iterative closest point (ICP)

“How well do the scans match up?”

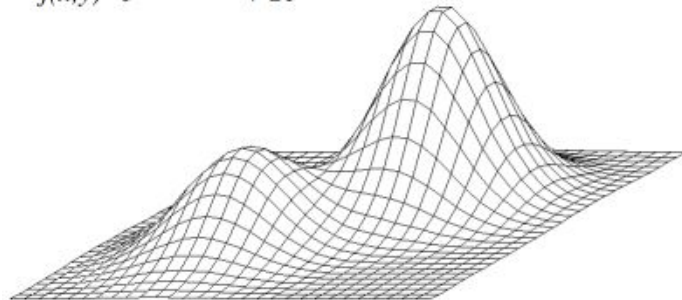
Find the rotation/translation that lines the two scans up the best

ICP Scan Matching: Correspondence Overview

- Compute scan correspondence
- Some form of iterative alignment
 - ICP based on SVD
 - Non linear Least Squares based ICP
 - Point to plane metric with Least Squares ICP
- Outlier rejection and information theory

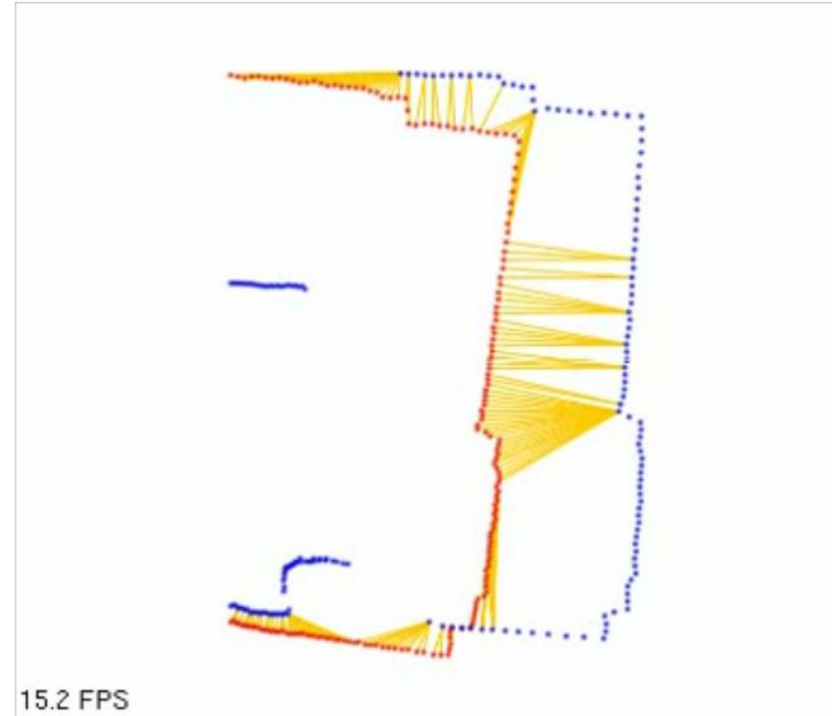
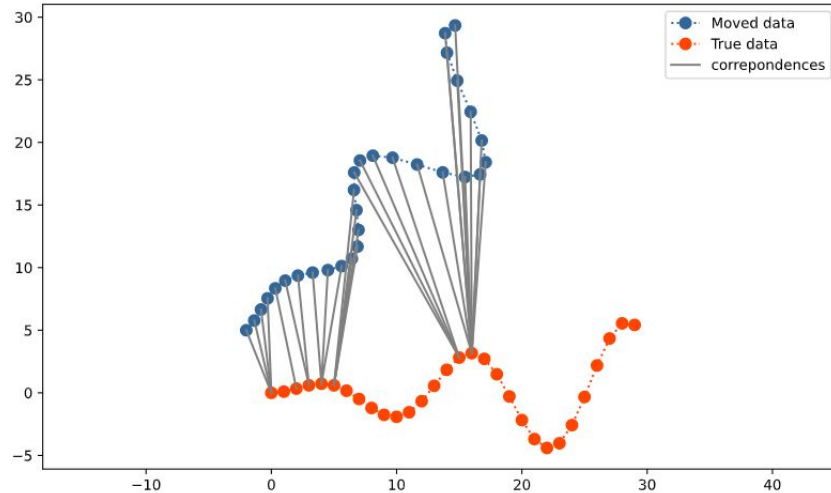


$$f(x,y) = e^{-(x^2+y^2)} + 2e^{-((x-1.7)^2+(y-1.7)^2)}$$



ICP Scan Matching: Example Jupyter notebook

<https://nbviewer.org/github/niosus/notebooks/blob/master/icp.ipynb>



ICP Scan Matching: Issues?

- Local minima
 - Use closer, incremental scans to avoid this issue
- Lidar scans points arbitrary
 - Solution: Iterative closest line, or plane, instead of point
- Sensitive to outliers
- $O(m*n)$
 - M, N are number of points in scans A and B

ICP Scan Matching: (ICL) Iterative Closest Line

Lidars sample points at arbitrary space

- Exact points sampled in A may not be sampled in B
- Solution: interpolate lines between points in Scan B, find closest *line* instead of closest *point*
- Same can be done with planes in 3D

ICP Scan Matching: Dealing with Outliers

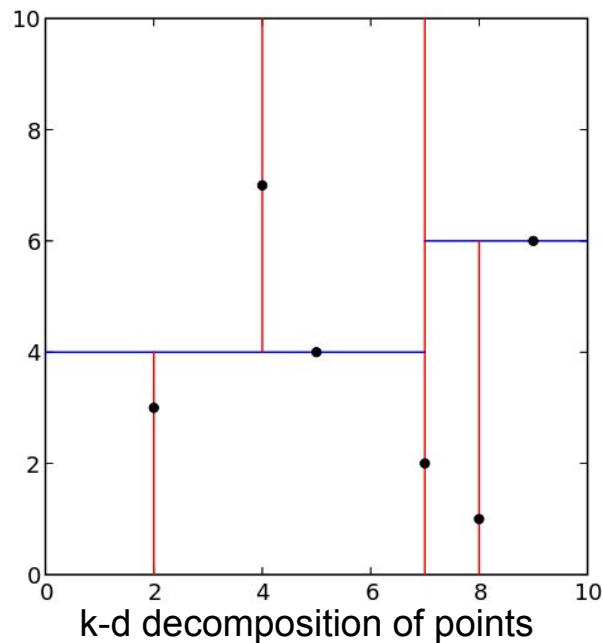
- Review literature for current methods
- Simplistic methods
 - Outlier removal based on threshold
 - Weighting points
- Modified K-D Tree

ICP Scan Matching: Simplifying Correspondences

- To compute correspondences, currently each point of scan 2 has to check distance with every point of scan 1 $\sim O(N^2)$
 - Not impossible with small lidars only calculating 300 points a scan
 - Velodyne Lidar provides $\sim 300k-700k+$ points a second
- Solution: Preprocess data before each scan
 - K-D Trees

ICP Scan Matching: K-D Trees

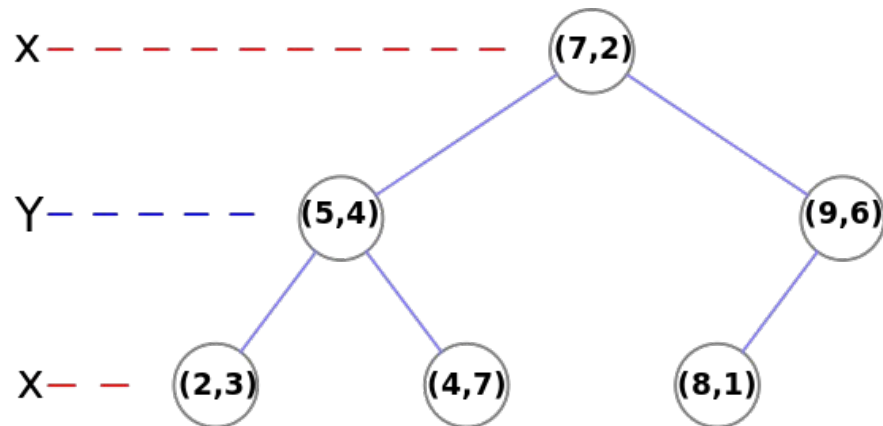
- Process of partitioning data into a tree structure with 2 leaves per node.
- Starts with centered point (methods to estimated center point) to ensure balanced tree



Points

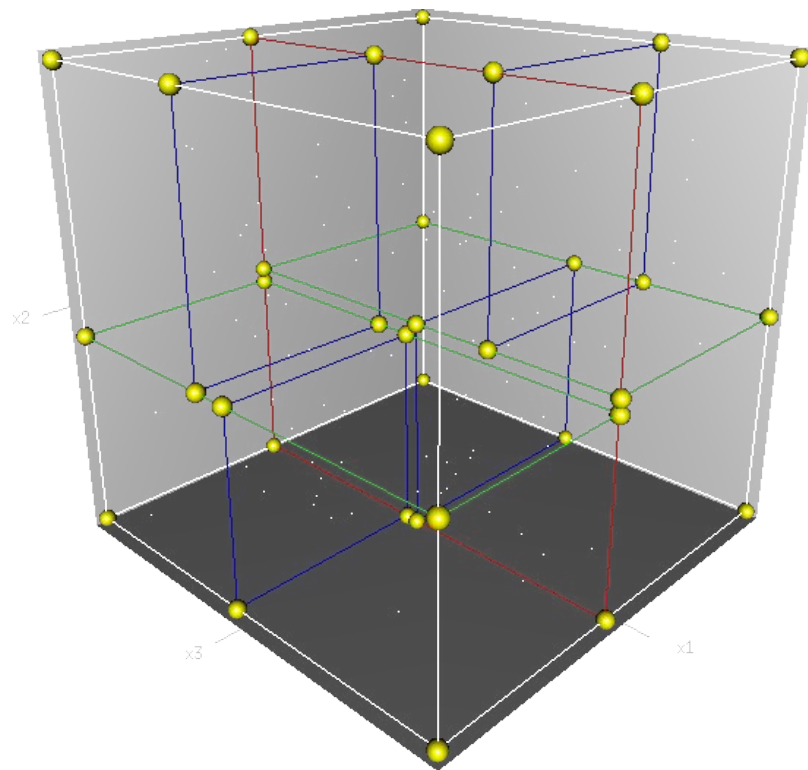
:

(2,3),
(5,4),
(9,6),
(4,7),
(8,1),
(7,2)

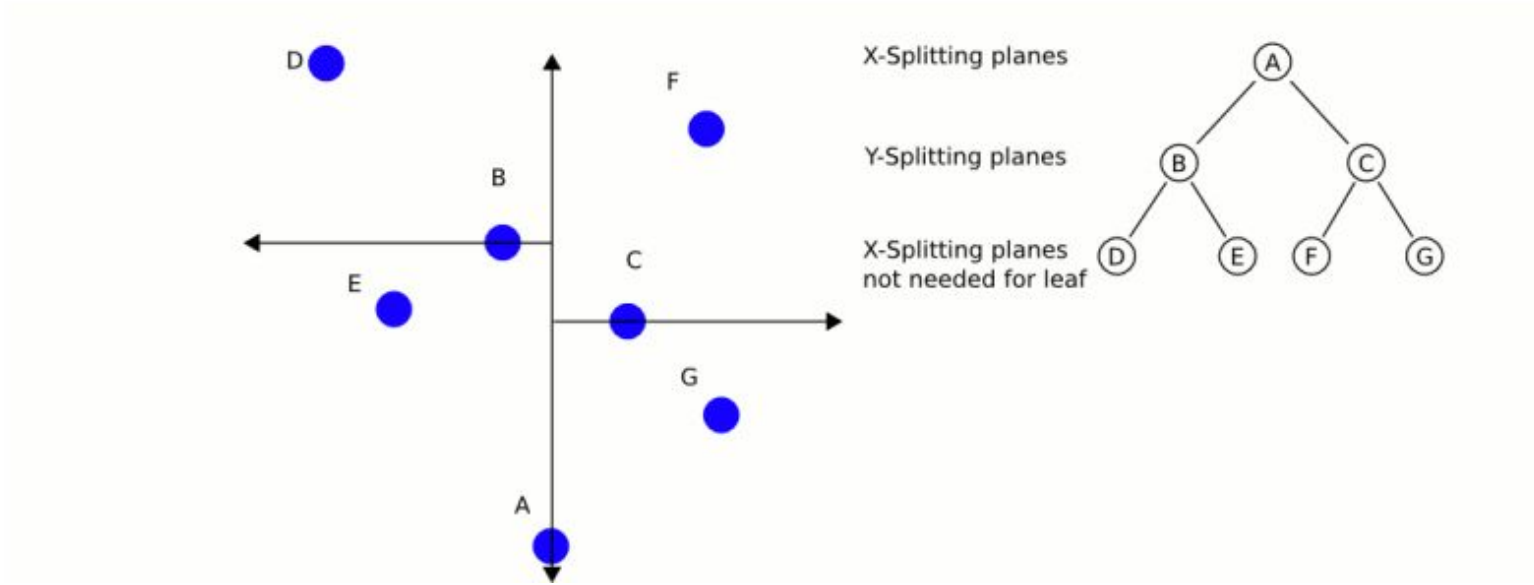


Resulting k-d tree

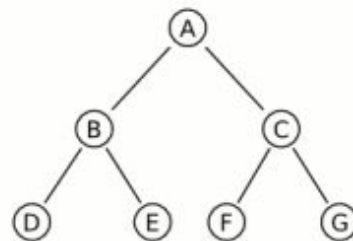
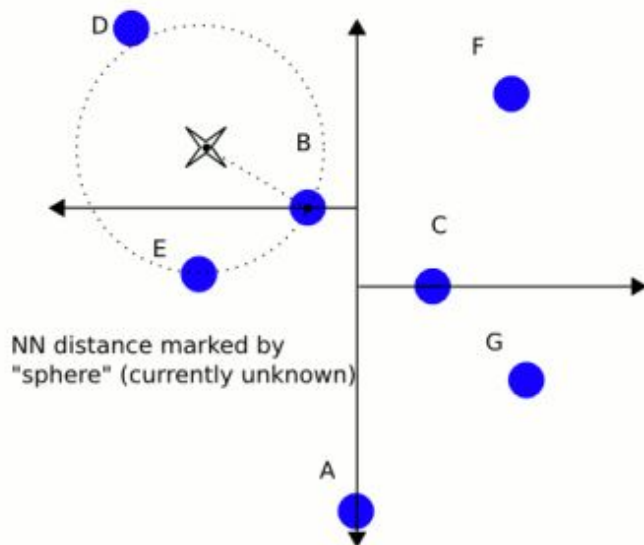
K-D tree in 3 dimensions



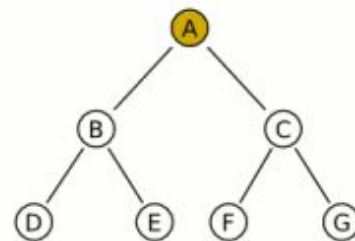
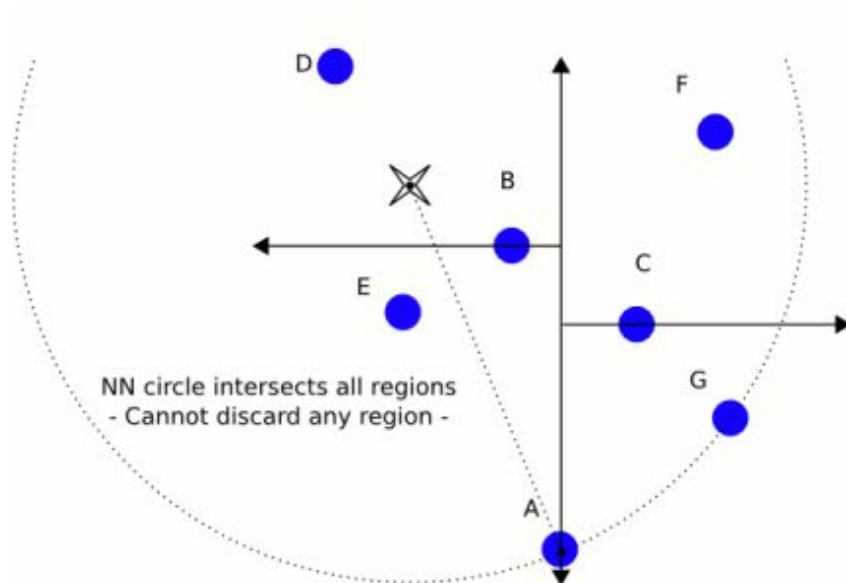
Nearest Neighbor Search



Nearest Neighbor Search

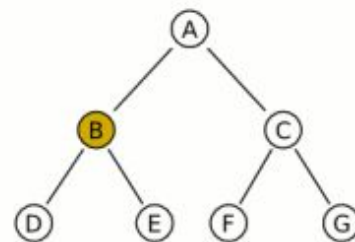
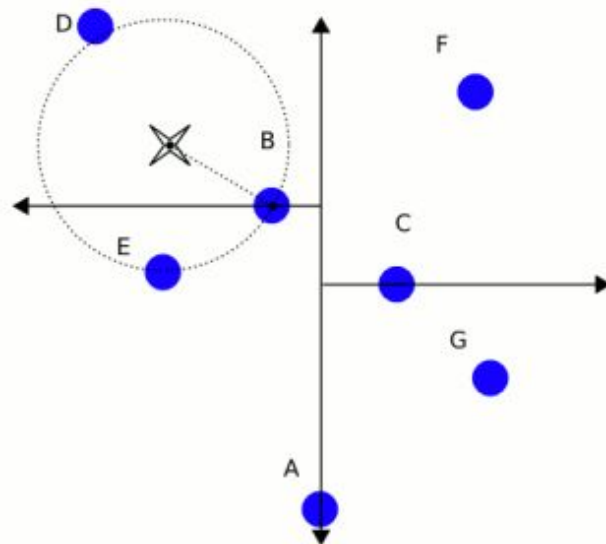


Nearest Neighbor Search



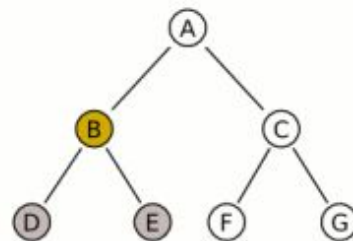
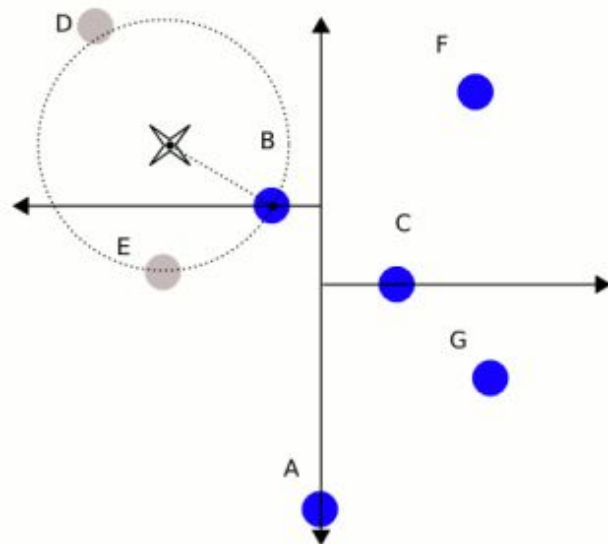
Start at A, then proceed in depth-first search (maintain a stack of parent-nodes if using a singly-linked tree). Set best estimate to A's distance. Then examine left child node

Nearest Neighbor Search



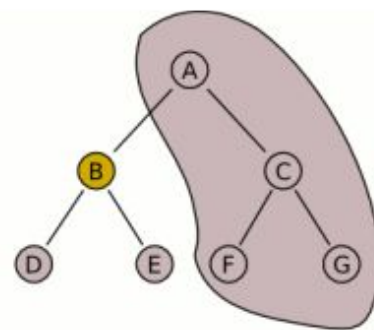
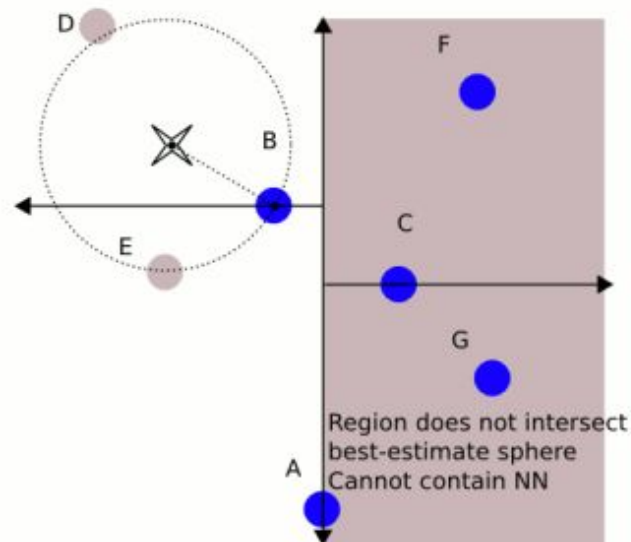
Calculate B's distance and compare against best estimate
- It is smaller distance, so update best estimate. Examine children (left then right)

Nearest Neighbor Search



D & E Discarded as B
(already visited) is closer.
B is the best estimate for B's sub-branch
Proceed back to parent node

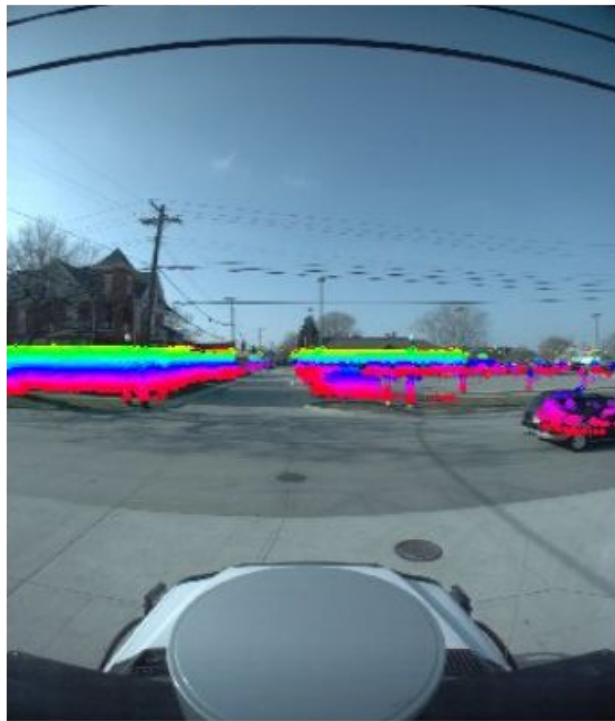
Nearest Neighbor Search



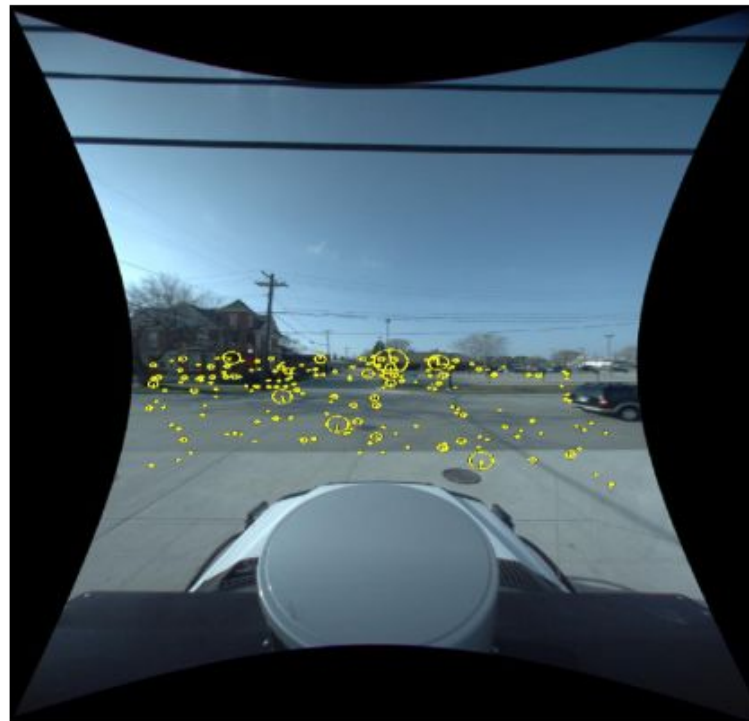
A's children have all been searched,
B is the best estimate for entire tree

Camera+ICP Fused Algorithm

Assign SIFT descriptors to the 3-D LIDAR for robust point-cloud matching

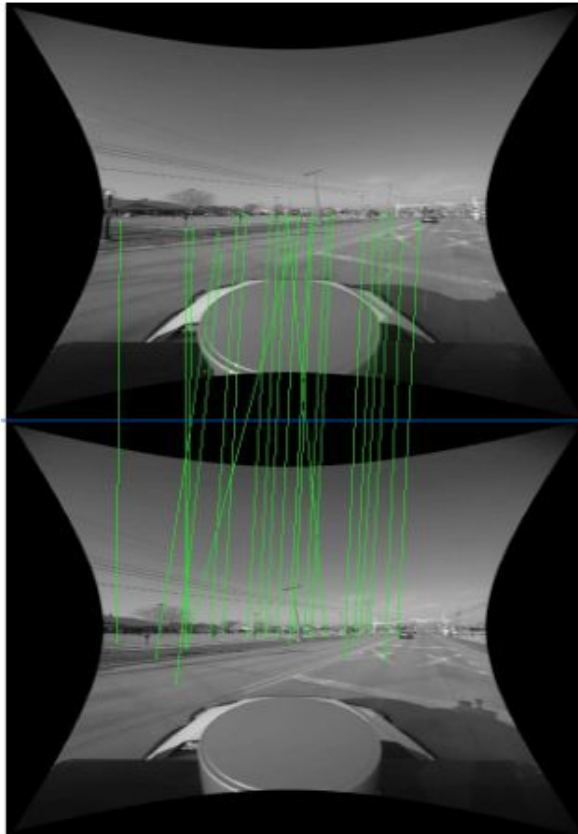


LIDAR projected into imagery
(ground-plane not rendered for visual clarity)



SIFT camera feature detections
(coincident with LIDAR data)

Camera+ICP Fused Algorithm



Frame to frame SIFT matching

RANSAC algorithm that uses SIFT matches to seed ICP registration, resulting in faster and more robust point-cloud registration

Visually bootstrapped ICP Algorithm:

Extract SIFT features and re-project onto to lidar

Assign putative lidar correspondences based upon visual similarity

While (# trials)

- Draw 3 random putative correspondence pairs

- Fit rigid body transform, RBT

- Test for model consensus

- Keep RBT model with best consensus

endWhile

Refine RBT using generalized ICP

This algorithm generates more robust results with less spatial data

Visually Bootstrapped ICP Results

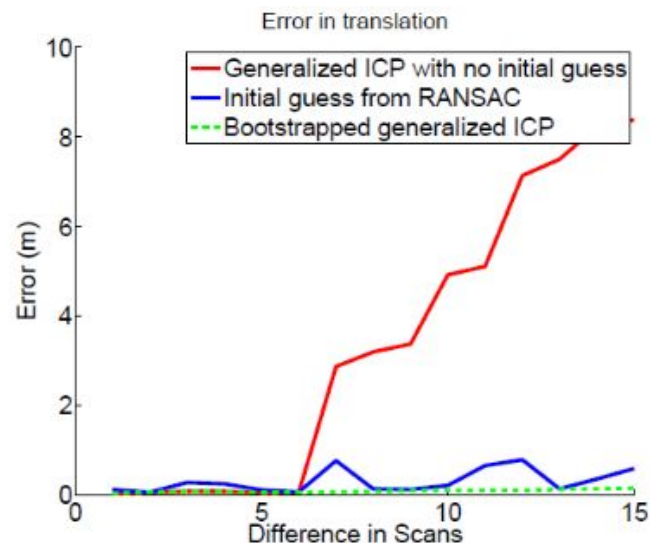


TABLE I

THIS TABLE SUMMARIZES THE ERROR IN SCAN ALIGNMENT. WE SHOW HERE THE TRANSLATION AND ROTATIONAL ERROR BETWEEN SCAN PAIRS {1-2, 1-5, 1-10, 1-15} OBTAINED AT DIFFERENT LOCATIONS. HERE WE HAVE USED THE POSE OF THE VEHICLE OBTAINED FROM A HIGH END IMU AS GROUND TRUTH TO CALCULATE ALL THE ERRORS.

Scans	Generalized ICP with no initial guess						Initial guess from RANSAC						Bootstrapped generalized ICP					
	T (m)		Ax (degrees)		An (degrees)		T (m)		Ax (degrees)		An (degrees)		T (m)		Ax (degrees)		An (degrees)	
	Err	Std	Err	Std	Err	Std	Err	Std	Err	Std	Err	Std	Err	Std	Err	Std	Err	Std
1-2	.047	.011	0	0	.05	.02	.15	.02	0	0	.223	.0003	.04	.010	0	0	.057	.110
1-5	.546	.173	.570	.20	1.15	.344	.20	.03	.43	.15	.230	.0001	.084	.010	.025	.090	.058	.006
1-10	6.37	.868	.710	.25	1.72	.573	.51	.09	.59	.01	.745	.0044	.145	.015	.030	.010	.057	.012
1-15	10.34	.834	1.86	.13	2.86	.057	1.02	.02	1.35	.54	1.15	.0021	.220	.008	.042	.015	.070	.017

T – Error in translation (meters); Ax – Error in rotation axis (degrees); An – Error in rotation angle (degrees)

Err = Average Error; Std = Standard Deviation

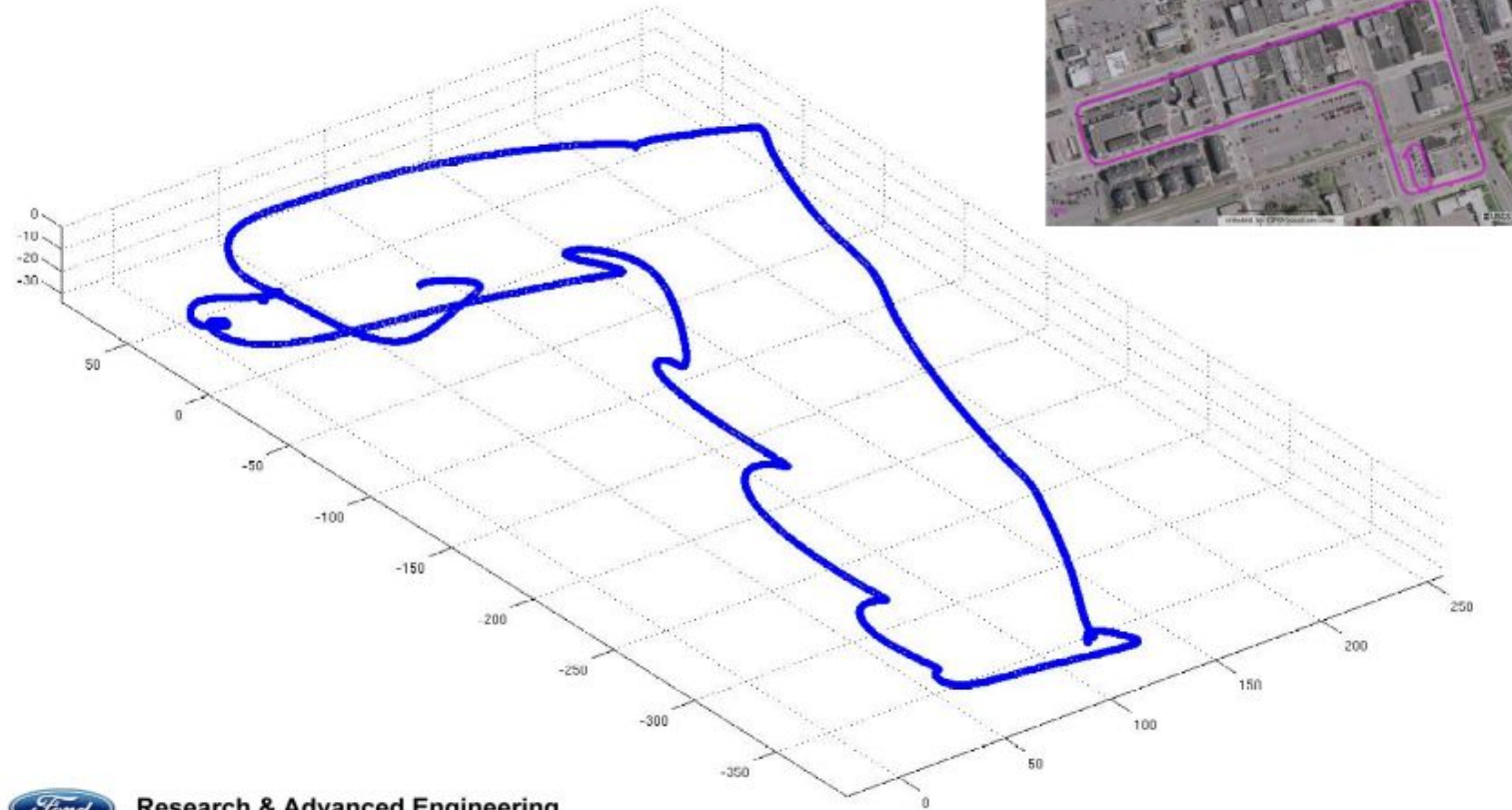
SLAM GPS-Denied Demonstration

*OmniSTAR HP GPS ground-truth and Applanix POS-LV IMU
1.6 km loop around Dearborn*



Dead Reckoning

No GPS Reception – Velocity Integration of MEMs-based XSENS MTi-G IMU Data



SLAM Demonstration

Ground Truth vs. Laser Odometry

No GPS Reception – Intra-frame Motion Compensated by XSENS MTi-G IMU



Summary:

Feature vs. non-feature matching

- ▶ Features (pros)
 - ▶ Data reduction
 - ▶ Noise filtering
 - ▶ Extraction + Matching is often fast
 - ▶ Can handle from large prior uncertainties.
- ▶ Non-Feature Matching (pros)
 - ▶ General purpose: don't require world to contain our features
 - ▶ ICP/ICL:
 - ▶ Very fast, easy to implement. Local maxima problems.
 - ▶ Correlation
 - ▶ Fast enough, very robust