

2

4

7

6

19

☐ Logic

Given two Boolean Variables P and Q, there are 4 possible combinations of values that can produce 16 possible outcomes.

☐ Inputs P and Q to the operators:

```

P | Q
---+---
T | T
T | F
F | T
F | F

```

☐ Enumerating the 16 possible outcomes of Boolean Operations
Table is labeled in hexadecimal

```

0 1 2 3 4 5 6 7 8 9 a b c d e f
T T T T T T T T F F F F F F F F
T T T T F F F F T T T T F F F F
T T F F T T F F T T F F T T F F
T F T F T F T F T F T F T F T F

```

☐ NAMING AND PROVING THE SIXTEEN OPERATORS

```

operator 0 is = not(f(P,Q)) = NXAOPQ = not(xor(and( or(P , Q))))
operator 1 is = not(e(P,Q)) = OPQ = or(P , Q)
operator 2 is = not(d(P,Q)) = OPNQ = or(P , not(Q))
operator 3 is = not(c(P,Q)) = P = P
operator 4 is = not(b(P,Q)) = ONPQ = or(not(P), Q)
operator 5 is = not(a(P,Q)) = Q = Q
operator 6 is = not(9(P,Q)) = NXPQ = not(xor( P , Q ))
operator 7 is = not(8(P,Q)) = APQ = and( P , Q )
operator 8 is = not(7(P,Q)) = NAPQ = not(and( P , Q ))
operator 9 is = not(6(P,Q)) = XPQ = xor( P , Q )
operator a is = not(5(P,Q)) = NQ = not( Q )
operator b is = not(4(P,Q)) = NONPQ = not( or(not( P), Q ))
operator c is = not(3(P,Q)) = NP = not( P )
operator d is = not(2(P,Q)) = NOPNQ = not( or( P , not(Q)) )
operator e is = not(1(P,Q)) = NOPQ = not( or( P , Q ))
operator f is = not(0(P,Q)) = XAOPQ = xor(and( or(P , Q)))

```

☒ Words are chords of letters

Three-state logic is equivalent to yes/no/maybe, white/black/gray
 if-then-else is a non-commutative ternary operator
 $d = \text{ifThenElse}(a,b,c)$ // A whole theory of computation emerges...