

## SCHOOL OF APPLIED SCIENCE & HUMANITIES DEPARTMENT OF MATHEMATICS

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## **Unit 2: Functions Tutorial Questions**

1. Define a function and give an example of a function that is neither even nor odd.

- 2. Determine whether f(x) = |x| is even, odd, or neither.
- 3. If f(x) = 3x + 2, find f(-2).
- 4. State the condition for a function to be one-to-one.
- 5. Determine if  $f(x) = x^2$  is one-to-one over the set of real numbers.
- 6. Find the domain of f(x) = 1 / (x 3).
- 7. Find the range of  $f(x) = \sqrt{(x-1)}$ .
- 8. Determine the domain of  $f(x) = \ln(x + 4)$ .
- 9. If  $f(x) = \sqrt{9 x^2}$ , find the domain.
- 10. Find the range of  $f(x) = (x^2 1)/(x^2 + 1)$ .
- 11. If f(x) = 2x + 3 and  $g(x) = x^2$ , find  $(f \circ g)(x)$ .
- 12. If  $f(x) = \sqrt{x}$  and g(x) = x 2, find  $(g \circ f)(x)$ .
- 13. Given f(x) = 1/x and g(x) = x + 5, find  $(f \circ g)(2)$ .
- 14. If f(x) = 3 x and  $g(x) = x^2$ , find  $(g \circ f)(x)$ .
- 15. Determine if composition of functions is commutative.
- 16. Give an example of a polynomial function of degree 3.
- 17. Give an example of an exponential function.
- 18. Give an example of a rational function.
- 19. Give an example of a piecewise-defined function.
- 20. Give an example of a periodic function.
- 21. Define the inverse of a function.
- 22. Find the inverse of f(x) = 2x + 5.
- 23. Determine if  $f(x) = x^3 + 2$  has an inverse.
- 24. Find the inverse of f(x) = (x-3)/(x+2).
- 25. Show that  $f(x) = e^x$  and  $f^{-1}(x) = \ln(x)$  are inverses.
- 26. Factorize  $x^2 9$ .
- 27. Factorize  $x^3 8$ .
- 28. Factorize  $x^2 + 5x + 6$ .

- 29. Factorize  $x^3 + 27$ .
- 30. Factorize  $x^4 16$ .
- 31. Solve  $x^2 5x + 6 = 0$ .
- 32. Solve  $2x^2 + 3x 2 = 0$ .
- 33. Find the discriminant of  $x^2 4x + 4 = 0$  and comment.
- 34. Solve  $x^2 + x + 1 = 0$ .
- 35. Find the roots of  $4x^2 4x + 1 = 0$ .
- 36. Solve x 3 > 0.
- 37. Solve  $2x + 5 \le 9$ .
- 38. Solve |x-2| < 5.
- 39. Solve  $3x 7 \ge 2x + 4$ .
- 40. Solve -2x + 1 < 5.
- 41. Explain why a function can't have two different outputs for the same input.
- 42. Can the graph of a function intersect a vertical line more than once?
- 43. If  $f(x) = x^2$ , what is  $f(\sqrt{2}) + f(-\sqrt{2})$ ?
- 44. Find all x such that f(x) = f(-x) for  $f(x) = x^3 x$ .
- 45. If f(x) = x + 1/x, find f(2) + f(1/2).
- 46. Solve for x:  $\sqrt{(x + 1)} \sqrt{x} = 1$ .
- 47. If f(x) = ax + b and  $f^{-1}(x) = 2x 3$ , find a and b.
- 48. If  $f(x) = x^2$  and  $g(x) = \sqrt{x}$ , is g the inverse of f?
- 49. For which values of k is  $x^2 + kx + 4 = 0$  having equal roots?
- 50. If  $f(x) = 2x^2 3x + 1$ , find f(1) + f(-1).