

SCHOOL OF APPLIED SCIENCE & HUMANITIES DEPARTMENT OF MATHEMATICS

Subject: Foundations of Engineering Mathematics

Subject Code: 25MT101

Sem.: Pre-Semester

Academic Year: 2025-2026

Section: 20,26,31,32 Regulation: R25

Instructor: D Bhanu Prakash, Department of Mathematics and Statistics

Unit 2: Functions Tutorial Answers

- 1. A function maps each element in the domain to exactly one element in the range. Example: $f(x) = x^3 + 1$ is neither even nor odd.
- 2. Even, because f(-x) = |-x| = |x| = f(x).
- 3. f(-2) = 3(-2) + 2 = -6 + 2 = -4.
- 4. If $f(x_1) = f(x_2)$ implies $x_1 = x_2$ for all x_1, x_2 in the domain.
- 5. No, because f(2) = f(-2) = 4.
- 6. All real numbers except x = 3.
- 7. Range: $[0, \infty)$.
- 8. $x + 4 > 0 \rightarrow x > -4$.
- 9. $-3 \le x \le 3$.
- 10. Range: [−1, 1).
- 11. $(f \circ g)(x) = f(g(x)) = 2x^2 + 3$.
- 12. $(g \circ f)(x) = g(\sqrt{x}) = \sqrt{x} 2$.
- 13. $(f \circ g)(2) = 1/(2 + 5) = 1/7$.
- 14. $(g \circ f)(x) = (3 x)^2$.
- 15. Not necessarily. In general, $f \circ g \neq g \circ f$.
- 16. $f(x) = 2x^3 x^2 + 5x 7$.
- 17. $f(x) = 5^x$.
- 18. $f(x) = (x^2 + 1)/(x 4)$.
- 19. $f(x) = \{x^2, x < 0; 2x + 1, x \ge 0\}.$
- 20. $f(x) = \sin(x)$.
- 21. The inverse of f, denoted f^{-1} , is a function such that $f(f^{-1}(x)) = x$.
- 22. $y = 2x + 5 \rightarrow x = (y 5)/2 \rightarrow f^{-1}(x) = (x 5)/2$.
- 23. Yes, because it is strictly increasing on \mathbb{R} .
- 24. $y = (x-3)/(x+2) \rightarrow xy + 2y = x-3 \rightarrow xy x = -3 2y \rightarrow x(y-1) = -(3+2y) \rightarrow x = -(3+2y)/(y-1).$
- 25. $f(f^{-1}(x)) = e^{(\ln(x))} = x$, and $f^{-1}(f(x)) = \ln(e^x) = x$.
- 26. (x-3)(x+3).

27.
$$(x-2)(x^2+2x+4)$$
.

28.
$$(x + 2)(x + 3)$$
.

29.
$$(x + 3)(x^2 - 3x + 9)$$
.

30.
$$(x^2-4)(x^2+4) = (x-2)(x+2)(x^2+4)$$
.

31.
$$x = 2$$
 or $x = 3$.

32.
$$x = (-3 \pm \sqrt{9 + 16})/4 = (-3 \pm 5)/4 \rightarrow x = 1/2 \text{ or } x = -2.$$

33. D =
$$(-4)^2 - 4(1)(4) = 0$$
, so one repeated real root.

34.
$$x = (-1 \pm i\sqrt{3})/2$$
.

35.
$$x = 1/2$$
 (repeated root).

37.
$$x \le 2$$
.

38.
$$-5 < x - 2 < 5 \rightarrow -3 < x < 7$$
.

39.
$$x \ge 11$$
.

$$40. -2x < 4 \rightarrow x > -2.$$

- 41. Because by definition, a function assigns exactly one output to each input.
- 42. No, by the vertical line test.

$$43. 2 + 2 = 4.$$

44.
$$x^3 - x = -x^3 + x \rightarrow 2x^3 - 2x = 0 \rightarrow 2x(x^2 - 1) = 0 \rightarrow x = 0, \pm 1.$$

45.
$$(2 + 1/2) + (1/2 + 2) = 2.5 + 2.5 = 5$$
.

46.
$$\sqrt{(x+1)} - \sqrt{x} = 1 \rightarrow \text{Let } \sqrt{x} = t \rightarrow \sqrt{(t^2+1)} - t = 1 \rightarrow \sqrt{(t^2+1)} = t + 1 \rightarrow t^2 + 1 = t^2 + 2t + 1 \rightarrow 2t = 0 \rightarrow t = 0 \rightarrow x = 0.$$

47. Inverse formula:
$$f^{-1}(x) = (x - b)/a = 2x - 3 \rightarrow 1/a = 2 \rightarrow a = 1/2$$
, and $-b/a = -3 \rightarrow b = 3/2$.

- 48. Not over \mathbb{R} , only over $[0, \infty)$ because f is not one-to-one over \mathbb{R} .
- 49. Equal roots when $k^2 16 = 0 \rightarrow k = \pm 4$.

50.
$$f(1) = 2 - 3 + 1 = 0$$
, $f(-1) = 2 + 3 + 1 = 6 \rightarrow sum = 6$.