25MT103: Linear Algebra

Unit 1: Matrices

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Matrices - Tutorial

Syllabus

- Elementary row and column operations
- Elementary Matrices
- Similar Matrices
- Echelon form
- Row reduced echelon form
- Rank of a matrix
- Inverse of a matrix by Gauss-Jordan Method
- LU decomposition

REF+RREF+Rank

1 Determine the rank of the matrix:

$$\begin{bmatrix} -1 & -2 & -1 \\ 2 & 4 & 3 \\ 3 & 6 & 3 \end{bmatrix}$$

Upper Triangular Matrix

• Reduce the matrix to upper triangular form

$$A = \begin{bmatrix} -2 & -1 \\ -4 & -3 \end{bmatrix}.$$

Decompose to LU form

Decompose the matrix into LU form

$$A = \begin{bmatrix} 4 & 3 \\ -1 & 1 \end{bmatrix}.$$

Gauss-Jordan elimination

 Show the steps of Gauss-Jordan elimination to find the inverse of the matrix

$$A = \begin{bmatrix} -1 & -2 \\ -3 & -4 \end{bmatrix}.$$

A few more...

- For the matrix $B = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 4 \\ 5 & 6 & 0 \end{bmatrix}$ compute its LU decomposition (if possible) and its determinant.
- ② Use Gauss–Jordan to find the inverse of $C = \begin{bmatrix} 1 & 2 & 0 \\ 0 & 1 & 1 \\ 2 & 3 & 1 \end{bmatrix}$.
- **3** Explain the relationship between the rank of *A* and the solution set of Ax = 0.

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Thank You!

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I can't change the direction of the wind, but I can adjust my sails to always reach my destination.

(Jimmy Dean)

