

1. $y'' - x^2y' - xy = 0$

2. $y''' = y'' - x^2(y')^2$

3. Aim to get this form:
$$\begin{cases} \frac{dx}{dt} = F(t, x, y), \\ \frac{dy}{dt} = G(t, x, y). \end{cases}$$

4. The system
$$\begin{cases} \frac{dx}{dt} = 4x - y, \\ \frac{dy}{dt} = 2x + y \end{cases}$$
 has the independent solutions
 $\{x = e^{3t}, y = e^{3t}\}$ and $\{x = e^{2t}, y = 2e^{2t}\}$.

Will focus on the simple cases (Linear Systems):

5. Non-Homogeneous:
$$\begin{cases} \frac{dx}{dt} = a_1(t)x + b_1(t)y + f_1(t), \\ \frac{dy}{dt} = a_2(t)x + b_2(t)y + f_2(t) \end{cases}$$

6. Homogeneous:
$$\begin{cases} \frac{dx}{dt} = a_1(t)x + b_1(t)y + f_1(t), \\ \frac{dy}{dt} = a_2(t)x + b_2(t)y + f_2(t) \end{cases}$$