

# Survey of Scientific Computing (SciComp 301)

Dave Biersach
Brookhaven National
Laboratory
dbiersach@bnl.gov

Session 18
Computational Biology,
Earth Science

#### **Session Goals**

- Gain an appreciation for a suffix sort to find the longest repeated substring (LRSS) in a sequence
  - Consider the use of this algorithm in the realm of bioinformatics and genetic sequence alignment
  - Consider interesting research questions that stem from using the algorithm to explore DNA
- Assess the value of considering in DNA, not just the single longest repeated substring, but also the most (and least) frequently repeated substrings of a given length

# What is the Longest Repeated Substring?

#### input string

0 1 2 3 4 5 6 7 8 91011121314 a a c a a g t t t a c a a g c

#### Step 1 - Form the Suffixes array

```
suffixes
 0 aacaagtttacaagc
 1 acaagtttacaagc
 2 caagtttacaagc
 3 aagtttacaagc
 4 agtttacaagc
 5 gtttacaagc
 6 tttacaagc
 7 ttacaagc
 8 tacaagc
 9 acaagc
10 caagc
11 aagc
12 a g c
13 g c
```

# Step 2 – Sort the Suffixes array

```
sorted suffixes
  aacaagtttacaagc
11 a a g c
 3 aagtttacaagc
 9 acaagc
 1 acaagtttacaagc
12 a g c
 4 agtttacaagc
14 C
10 caage
 2 caagtttacaagc
13 g c
 5 gtttacaagc
 8 tacaage
 7 ttacaagc
 6 tttacaagc
```

```
sorted suffixes
  aacaagtttacaagc
 11 a a g c
 3 aagtttacaagc
 9 acaagc
 1 acaagtttacaagc
12 a g c
 4 agtttacaagc
14 C
10 caage
   caagtttacaagc
13 g c
 5 gtttacaagc
 8 tacaage
 7 ttacaagc
 6 tttacaagc
```

```
sorted suffixes
  <u>aac</u>aagtttacaagc
11 a a g c
 3 aagtttacaagc
 9 acaagc
 1 acaagtttacaagc
12 a g c
 4 agtttacaagc
14 C
10 caage
   caagtttacaagc
13 g c
 5 gtttacaagc
 8 tacaage
 7 ttacaagc
 6 tttacaagc
```

```
sorted suffixes
   aacaagtttacaagc
 11 aagc
 3 aagtttacaagc
  acaagc
   a c a a g t t t a c a a g c
 12 a g c
 4 agtttacaagc
 14 C
 10 caage
   caagtttacaagc
 13 g c
 5 gtttacaagc
 8 tacaage
 7 ttacaagc
 6 tttacaagc
```

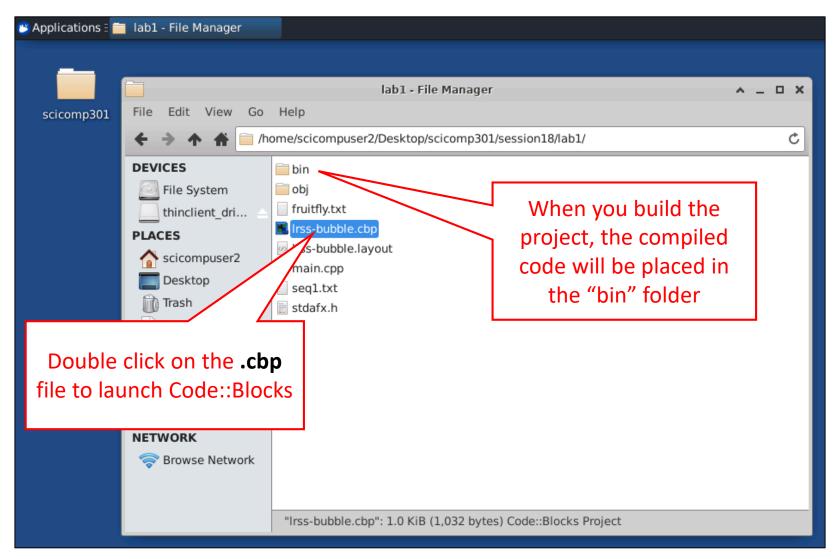
```
sorted suffixes
  aacaagtttacaagc
11 aagc
 3 aagtttacaagc
 9 acaagc
 1 acaagtttacaagc
  a g c
  agtttacaagc
14
  caagc
   caagtttacaagc
13 q C
 5 gtttacaagc
 8 tacaage
 7 ttacaagc
 6 tttacaagc
```

```
sorted suffixes
  aacaagtttacaagc
11 aagc
 3 aagtttacaagc
 9 acaagc
 1 acaagtttacaagc
12 a g c
 4 <u>ag</u>tttacaagc
14
10 c a a g c
   caagtttacaagc
13 q C
 5 gtttacaagc
 8 tacaage
 7 ttacaagc
 6 tttacaagc
```

```
sorted suffixes
   aacaagtttacaagc
11 aagc
 3 aagtttacaagc
 9 acaagc
 1 acaagtttacaagc
12 a g c
 4 agtttacaagc
14 C
10 caage
   caagtttacaagc
13 q C
 5 gtttacaagc
 8 tacaage
  ttacaagc
   tttacaagc
```

```
sorted suffixes
   aacaagtttacaagc
 11 a a g c
 3 aagtttacaagc
   acaagc
   a c a a g t t t a c a a g c
 12 a g c
   a g t t t a longest repeated substring
 14 C
                  aacaagtttacaagc
 10 caage
   caagtttacaagc
 13 q C
 5 gtttacaagc
 8 tacaage
 7 ttacaagc
 6 tttacaagc
```

# Open Lab 1 – Longest Repeated Substring



# View Lab 1 – Longest Repeated Substring

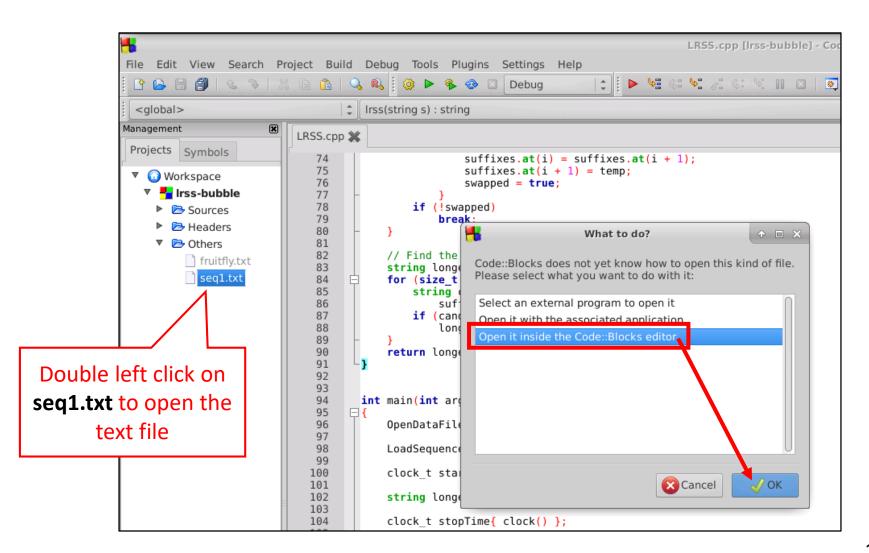
```
main.cpp 🗷
                       longest = candidate;
  95
  96
  97
              return longest;
  98
  99
 100
          int main(int argc, char *argv[])
 101
 102
        103
              OpenDataFile(argc, argv);
 104
              LoadSequence();
 105
 106
              boost::timer timer;
 107
 108
              string longest = lrss(*seq);
 109
 110
 111
              cout << "The longest repeated substring in "</pre>
                    << "\"" << filename << "\" is: "
 112
                    << longest << endl << endl;</pre>
 113
 114
 115
              cout.imbue(std::locale(""));
              cout << "Total run time: "</pre>
 116
                    << timer.elapsed() << "s" << endl;</pre>
 117
 118
              CloseDataFile();
 119
 120
 121
              return 0;
 122
```

```
string lrss(string s)
    // Create the suffix array
    vector<string> suffixes(s.size());
    for (size t i{}; i < suffixes.size(); ++i)</pre>
        suffixes.at(i) = s.substr(i, s.size() - i);
    // Bubble sort the suffix array
    while (true)
        bool swapped = false;
        for (size t i{}; i < suffixes.size() - 1; ++i)</pre>
            if (suffixes.at(i) > suffixes.at(i + 1))
                string temp = suffixes.at(i);
                suffixes.at(i) = suffixes.at(i + 1);
                suffixes.at(i + 1) = temp;
                swapped = true;
        if (!swapped)
            break:
    // Find the longest repeated substring (lrss)
    string longest{};
    for (size t i{}; i < suffixes.size() - 1; ++i)</pre>
        string candidate = match(suffixes.at(i),
                                  suffixes.at(i + 1)):
        if (candidate.size() > longest.size())
            longest = candidate;
    return longest;
```

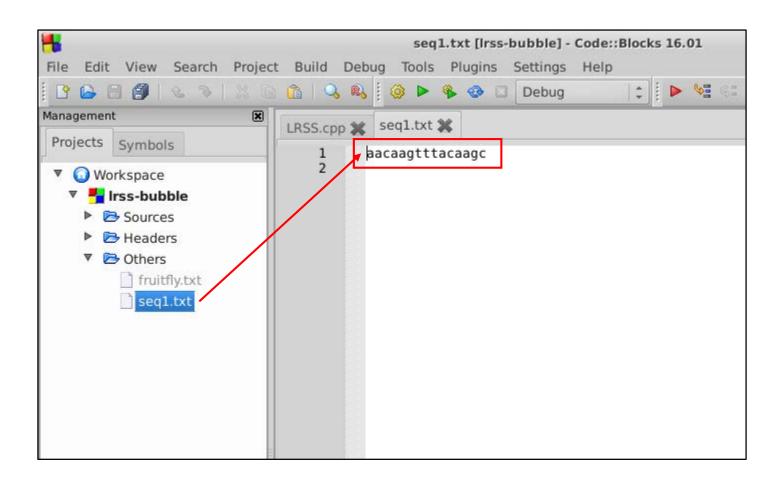
# Lab 1

Longest Repeated Substring

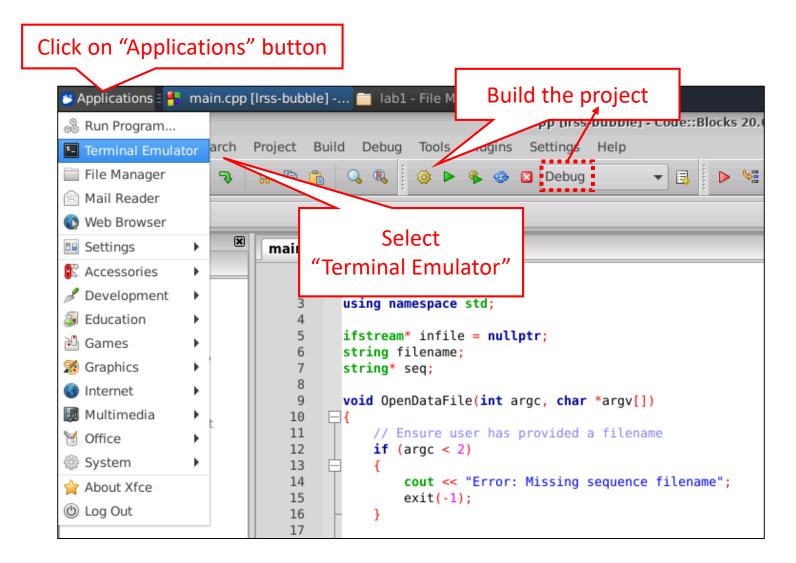
# View Lab 1 – Longest Repeated Substring



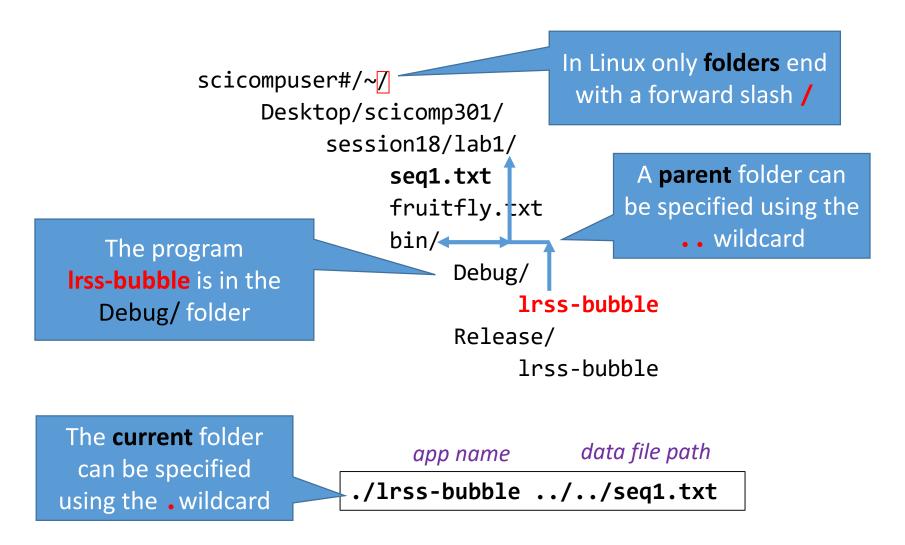
# View Lab 1 – Longest Repeated Substring



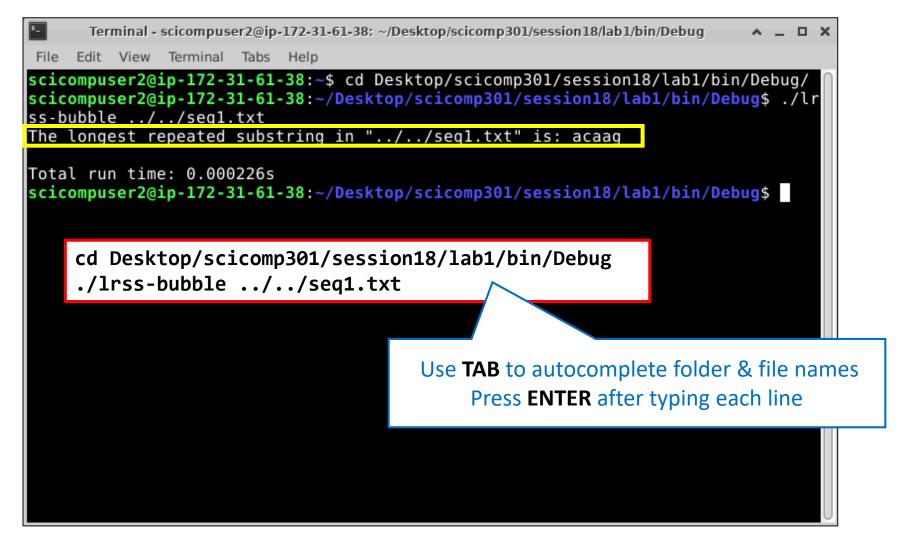
# **Build** Lab 1 – Longest Repeated Substring



# **Build** Lab 1 – Longest Repeated Substring



#### Run Lab 1 – Longest Repeated Substring

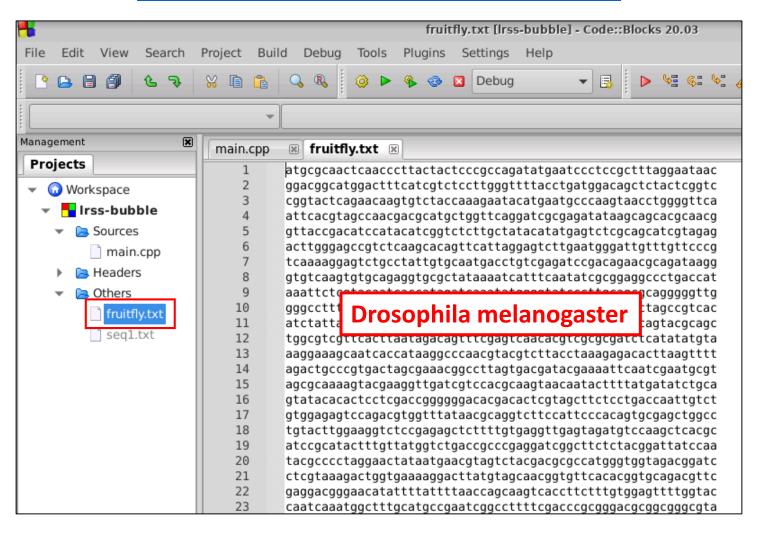


# **Check** Lab 1 – Longest Repeated Substring

```
Terminal - scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab1/bin/Debug
    Edit View Terminal Tabs Help
scicompuser2@ip-172-31-61-38:~$ cd Desktop/scicomp301/session18/lab1/bin/Debug/
scicompuser2@ip-172-31-61-38:~/Desktop/scicomp301/session18/lab1/bin/Debug$ ./lr
ss-bubble ../../seq1.txt
The longest repeated substring in "../../seq1.txt" is: acaag
Total run time: 0.000226s
scicompuser2@ip-172-31-61-38:~/Desktop/scicomp301/ses_con18/lab1/bin/Debug$
                input string
                        aacaagtttacaag
```

# View Lab 1 – Longest Repeated Substring

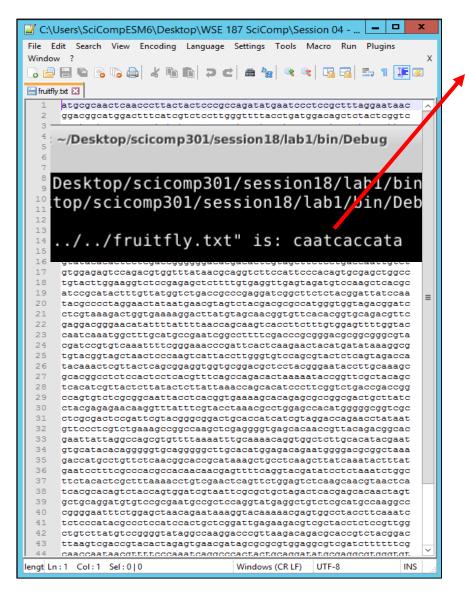
http://www.fruitfly.org/sequence/download.html

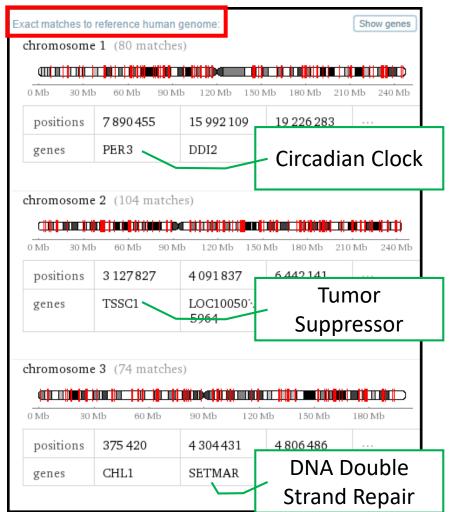


#### Run Lab 1 – Longest Repeated Substring

```
Terminal - scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab1/bin/Debug
     Edit
        View
              Terminal
scicompuser2@ip-172-31-61-38:~$ cd Desktop/scicomp301/session18/lab1/bin/Debug
scicompuser2@ip-172-31-61-38:~/Desktop/scicomp301/session18/lab1/bin/Debug$ ./lr
ss-bubble ../../fruitfly.txt
The longest repeated substring in "../../fruitfly.txt" is: caatcaccata
Total run time: 2.09754s
scicompuser2@ip-172-31-61-38:~/Desktop/scicomp301/session18/lab1/bin/Debug$
            cd Desktop/scicomp0301/session18/lab1/bin/Debug
            ./lrss-bubble ../../fruitfly.txt
```

#### http://www.wolframalpha.com/input/?i=CAATCACCATA





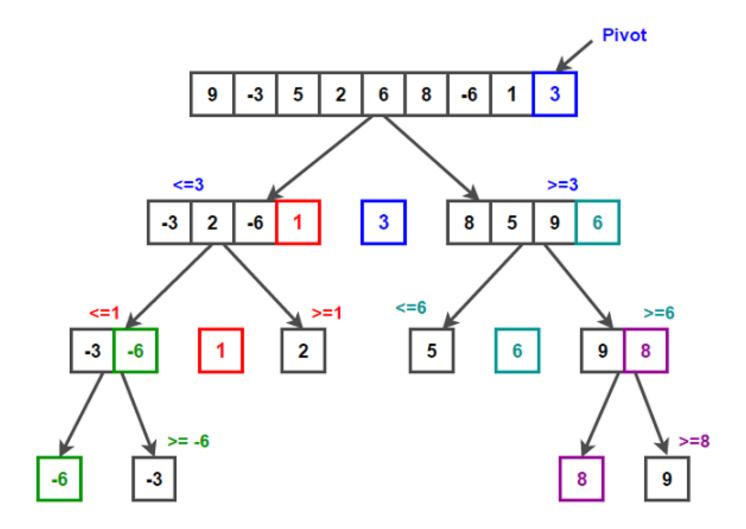
#### The Bubble Sort Algorithm

- The Bubble Sort is not very efficient because it can "move" only one element only one slot during one pass
  - The code spends a lot of time scanning through the array, mostly reconfirming that no swaps are needed between adjacent elements – little new information is gleamed from each pass
  - Therefore it wastes time constantly **rediscovering** that two elements are already in the right order this is the culprit
- What if we could move an item with a higher value farther to the end of the array in one big jump, rather than only a single slot each pass?
  - And can we stop wasting time scanning through groups of elements we have already proven to be in order?

#### The Quicksort Algorithm

- Invented by Tony Hoare in 1959, Quicksort is an efficient sorting algorithm that uses a divide & conquer strategy to overcome the problems of Bubble Sort
  - On each pass, a portion of the vector is split according to a pivot value those elements with a value <= the pivot are swapped with those elements with a value > the pivot
  - This act of partitioning separates the current section of the vector into a "left" portion having smaller values than the pivot, and a "right" portion having larger values than the pivot
- The left and right portions are then sorted (conquered) independently, and each portion is further split (divided) into smaller and smaller sized sub-portions, until the whole vector is eventually sorted

# The Quicksort Algorithm



#### Open Lab 2 – LRSS Quicksort

#### **Bubble Sort**

Quicksort requires longer and more complex code than bubble sort...

#### Is it worth it?

#### Quicksort

```
template<typename T>
int partition(vector<T>& v, size t left, size t right)
   T pivot = v.at(right);
    size t i = left;
    for (size t j = left; j < right; ++j)</pre>
        if (v.at(j) <= pivot)</pre>
            v.at(i).swap(v.at(j));
            i++:
   v.at(right) = v.at(i);
   v.at(i) = pivot;
    return i:
template<typename T>
void guicksort(vector<T>& v, int left, int right)
    if (left < right)</pre>
        int q = partition(v, left, right);
        quicksort(v, left, q - 1);
        quicksort(v, q + 1, right);
```

#### **Build** Lab 2 – LRSS **Quicksort**

```
main.cpp [Irss-qsort] - Code::Blocks 20.
                                       Debug Tools Plugins Settings Help
      Build the application
                                                            ☑ Debug
                                                                              ▼ 🖪 🕨 🦠
                                    LoadSequence(): void
 <alobal>
Management
                           main.cpp 🗵
Projects
                               1
                                     #include "stdafx.h"

▼ Morkspace

                                    using namespace std;
    - Irss-qsort
                                    ifstream* infile = nullptr;
       Sources
                                    string filename;
       Headers
                                    string* seq;
       Others
                              9
                                    void OpenDataFile(int argc, char *argv[])
                             10
                                  □{
                             11
                                        // Ensure user has provided a filename
                                         if (argc < 2)
                             12
                             13
                             14
                                             cout << "Error: Missing sequence filename";</pre>
                             15
                                             exit(-1);
                             16
                             17
                             18
                                         filename = argv[1];
                                         infile = new ifstream(filename);
                             19
                             20
                             21
                                         // Ensure the input file can be read
                             22
                                         if (!infile->is_open())
                             23
                                             cout << "Error: Unable to open file "</pre>
                              24
                                                  "\"" << filename << "\"" << endl;
                              25
                              26
                                             exit(-1):
                              27
                             28
```

#### Run Lab 2 – LRSS Quicksort

```
Terminal - scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab2/bin/Debug
     Edit View
             Terminal Tabs Help
scicompuser2@ip-172-31-61-38:~$ cd Desktop/scicomp301/session18/lab2/bin/Debug
scicompuser2@ip-172-31-61-38:~/Desktop/scicomp301/session18/lab2/bin/Debug$ ./lr
ss-gsort ../../fruitfly.txt
The longest repeated substring in "../../fruitfly.txt" is: caatcaccata
Total run time: 0.031733s
scicompuser2@ip-172-31-61-38:~/Desktop/scicomp301/session18/lab2/bin/Debug$
          cd Desktop/scicomp301/session18/lab2/bin/Debug
           ./lrss-qsort ../../fruitfly.txt
```

#### Check Lab 2 – LRSS Quicksort

#### **Bubble Sort**

```
Terminal - scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab1/bin/Debug  

File Edit View Terminal Tabs Help

scicompuser2@ip-172-31-61-38: ~$ cd Desktop/scicomp301/session18/lab1/bin/Debug  
scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab1/bin/Debug$ ./lr  
ss-bubble ../../fruitfly.txt  
The longest repeated substring in "../../fruitfly.txt" is: caatcaccata

Total run time: 2.09754s  
scicompuser2@ip-172-31-01-38: ~/Desktop/scicomp301/session18/lab1/bin/Debug$
```

#### Quicksort

```
Terminal - scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab2/bin/Debug

File Edit View Terminal Tabs Help

scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab2/bin/Debug
scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab2/bin/Debug$ ./lr
ss-qsort ../../fruitfly.txt
The longest repeated substring in "../../fruitfly.txt" is: caatcaccata

Total run time: 0.031733s
scicompuser2@ip-1/2-31-01-38: ~/Desktop/scicomp301/session18/lab2/bin/Debug$ ./Debug$

| Debug$ | De
```

The Role of Lecithin-Retinol Acyl Transferase in Keratinocyte Mechanics

**Emily Peterson** 

Smithtown High School East

Project ID 2250

#### LRAT and Skin Cancer

- ↓ Cell membrane ⇒ ↑ cancer
- ↓ Keratin ⇒ ↓ Cell membrane
- $\downarrow$  K5  $\Longrightarrow$   $\downarrow$  Keratin
- $\uparrow$  RA  $\Longrightarrow \downarrow$  K5
- $\uparrow$  Retinol  $\Longrightarrow \uparrow$  RA
- ↓ LRAT ⇒ ↑ Retinol
- ↓ LRAT ⇒ ↑ skin cancer

- Cancer is invasive
- Cytoskeleton filaments
- K5 is a gene
- Retinoic Acid regulates K5
- Retinol is Vitamin A
- LRAT moderates Retinol
- LRAT controls cell stiffness?

#### **LRAT**

TCTGCTCCTCGGGCGGCCTTGAGCAGTGCCTAACGTTGAGCGTGAGGCTCGTGCTCCGGGTCTCGCGGGCCGCCTCGGGCGTCGAGTCCCGGAG ATTGGACAGACACCAGAGCCTGGGGACCGCGGAGTGACCGGGTGGGGGCTGGAGGCCGCCGCCCTTCTGGGGAGACGCGGAGGTATCAGGACCT GGGCTATGCTCCTGATTTTATACAGACTGCCATGGCTCCAGATATAAAAGACCAAATAAAAAGATAAGAATTGCTGGCAACATATGCACTAAACTTC GTTTTGAAAAATCCCCTTGATGCCGATCACTGAGAAGTGATCCACAGGATGAAGAACCCCATGCTGGAGGTGGTGTCTTTACTACTGGAGAAGCTGC TCCTCATCTCCAACTTCACGCTCTTTAGTTCGGGCGCGCGGGGGGGAAGACAAGGGAAGACAGTTTTTATGAAACCAGCTCTTTCCACCGAGGCGA CGTGCTGGAGGTGCCCCGGACCCACCTGACCCACTATGGCATCTACCTAGGAGACAACCGTGTTGCCCACATGATGCCCGACATCCTGTTGGCCCTG ACAGACGACATGGGGCGCACGCAGAAGGTGGTCTCCAACAAGCGTCTCATCCTGGGCGTTATTGTCAAAGTGGCCAGCATCCGCGTGGACACAGTGG AGGACTTCGCCTACGGAGCTAACATCCTGGTCAATCACCTGGACGAGTCCCTCCAGAAAAAGGCACTGCTCAACGAGGAGGTGGCGCGGAGGGCTGA AAAGCTGCTGGGCTTTACCCCCTACAGCCTGCTGGGAACAACTGCGAGCACTTCGTGACCTACTGCAGATATGGCACCCCGATCAGTCCCAGTCC GACAAGTTTTGTGAGACTGTGAAGATAATTATTCGTGATCAGAGAAGTGTTCTTGCTTCAGCAGTCTTGGGGATTGGCGTCTATAGTCTGTACGGGCT GTAAATATGTTTATATTTATAGAGCATCAATCAATATAAGCATTATTGAGAAAAATGTGACCCGTAACACTGTGTTCTGGATAAAAATGTGATTAGG AATCACGCAAAGTGCTTACTGTGTAAGCCCAAGAACAAAGGCTTTCTGAATCTTCTCAGGCAGTTCAGATTTAAAGCACCATCCAAACCTTGGAAAT TGTACTGTTCGGCTGAATTTGAAGATTGGAAGACTTATATTGAGACCAGTAACTTTACTGTAAATTTACTTTGTTTCATTGAAAAAAACAAATTGATA AACATATTAAACTGGAAGAATTTTCTTTATTCAAATGAAAACATGTTTGATGACTGGTCAAAAAATAAGCTCATAATCTATTTTTTTCATGTAGTAT ATAAGTCAAGAATGTTTTATTGTCATTATGTGAAACCAATATTGGCAAATAGTACTTTAATGATGAAGTAAATGACCAGAAATTATAGAAATCTGTG TAGTCACATATACACAGACTGAGAGATAAATTGTTCTTGATTGCTTTATTATCATCATACTAGTGTGTTCATTATAGAGTATCTGTAGAGGTGAATG TAAAAGTAAGTCCAATCTATTTTCTTATGTCATTGAATTTGTAGTGTTAACTTGCATATATGTTATTGGATGGGTTGTCTTTTAAAGCATTTACTAA TGTACTCTGAAATTTTTAAAAGCCTTCAGATTTGTTTTCTAGTCACTTTTTTCCATATCATTTCTAATTATAGTTTATATCCTTAAAAGAAGGATGC CACAGTAGTATGTAAAACCCAAACAAGTAGAACCCAAGCAAATAAAATTATTTAAAATAATTTTAAAGTGGCTTAGTACTGCCAGTCATGTAAATTG ATTCTGCTGAGGGTCTTATAAGAATTGAGATATAACAATGGTAAAACAAGCATTCAAGCACTTTTACAAAATTACCAAATTCTTAAAATGAAGCCAC AGCTAGACTTGCATTTCAGGTATTAAAATTGCTTTCTTAACTGTCAAGAATCACAAAATAACAAATCATATTATGAGTGAATATGGGGAGGGCGGGG CCAATCAGTCAATGATAATCTGAACAAATTTTAAGAGCAGATTTTAGATTAATAATGTTTTATCACCACTAATTTGCCCACAACAACTCAGTATTT AATTTTTCAAATTAAATATTAAATTATTTAAGTATTTTAAATAATTAAAACATTAAAATGGCAACACCATAGAATATAGGTGTTCTCTGGACCTATTC TAACCACTTAAAATTATCTTAAGTATGCATACATAAAAGCAACCACTATGAGAACTACCGTGTTAGTGGTTTTTCACTTACTGTATATTACCCTTGT CATTAAAGCAAGATTCAATTCCT

#### Open Lab 3 – Substring Frequency

```
void WriteSubstrings()
                              cout << "Creating file \""</pre>
                                   << filename << "\" ...";
                              *outfile << "length,count,freq,seq,proteins"
                                       << endl;
                              map<string, int> table;
                             for (int len{ 3 }; len < 19; ++len)</pre>
                                  table.clear();
                                  for (size t pos{}; pos <= seq->length() - len; ++pos)
                                      string key = seq->substr(pos, len);
                                      auto p = table.find(key);
                                      if (p == table.end())
occurrences in which
                                          table.insert(pair<string, int>(key, 1));
                                      else
each substring of the
                                          p->second++;
given length appears
                                  // Copy sorted map to an unsorted list
                                  vector<pair<string, int>> list;
                                  for (auto& p : table)
                                      list.push back(p);
                                  WriteFreq(list, len, true, 5);
                                  WriteFreq(list, len, false, 5);
                              cout << " done!" << endl;</pre>
```

We sum the

#### **View** Lab 3 – Substring Frequency

```
void WriteFreg(vector<pair<string, int>>& list, int len,
               bool topmost, size t limit)
    string freqLabel;
    if (topmost)
        freqLabel = "Most";
        // Sort list by decreasing substring frequency
        sort(list.begin(), list.end(),
             [](const pair<string, int> &a,
                const pair<string, int>& b)
            return a.second > b.second;
    else
        fregLabel = "Least";
        // Sort list by increasing substring frequency
        sort(list.begin(), list.end(),
             [](const pair<string, int> &a,
                const pair<string, int>& b)
            return a.second < b.second;</pre>
        });
    list.size() > limit ? limit : list.size();
    for (size_t row{); row < limit; ++row)</pre>
      *outfile << len << "," << list.at(row).second</pre>
                 << "," << freqLabel << "," << list.at(row).first</pre>
                 << "," << GetCodons(list.at(row).first) << endl;</pre>
```

Instead of targeting cout, we can insert into a file stream to create a CSV file

#### **DNA Codon Table**

#### Standard genetic code

| 1st  | 2nd base           |                            |     |                   |                    |   |                    |                    | 3rd |
|------|--------------------|----------------------------|-----|-------------------|--------------------|---|--------------------|--------------------|-----|
| base |                    | Т                          | С   |                   |                    | Α   |                    | base               |     |
| т    | TTT                | (Phe/F) Phenylalanine      | TCT |                   | TAT                | (Tyr/Y) Tyrosine                            | TGT                | (Cys/C) Cysteine   | Т   |
|      | TTC                | (File/F) Fileliyialalilile | TCC | (Sar/S) Sarina    | TAC                | (Tyl/T) Tyrosine                            | TGC                | (Cys/C) Cystelle   | С   |
|      | TTA                |                            | TCA | (Ser/S) Serine    | TAA <sup>[B]</sup> | Stop (Ochre)                                | TGA <sup>[B]</sup> | Stop (Opal)        | Α   |
|      | TTG                |                            | TCG |                   | TAG <sup>[B]</sup> | Stop (Amber)                                | TGG                | (Trp/W) Tryptophan | G   |
| С    | CTT                | (Leu/L) Leucine            | CCT | (Pro/P) Proline   | (His/H) Histidine  | CGT   |                    | Т                  |     |
|      | CTC                |                            | CCC |                   | CAC                | (Fils/FI) Filstidine                        | CGC                | (Arg/R) Arginine   | С   |
|      | CTA                |                            | CCA |                   | CAA                | (Gln/Q) Glutamine                           | CGA                |                    | Α   |
|      | CTG                |                            | CCG |                   | CAG                | (GIII/Q) Gidtarrille                        | CGG                |                    | G   |
| A    | ATT                | (Ile/I) Isoleucine         | ACT | (Thr/T) Threonine | AAT                | (Asn/N) Asparagine (Lys/K) Lysine           | AGT                | (Ser/S) Serine     | Т   |
|      | ATC                |                            | ACC |                   | AAC                |   | AGC                | (Sel/S) Sellife    | С   |
| ^    | ATA                |                            | ACA |                   | AAA                |   | AGA                | (Arg/R) Arginine   | Α   |
|      | ATG <sup>[A]</sup> | (Met/M) Methionine         | ACG |                   | AAG                |   | AGG                | (Alg/R) Algillille | G   |
| G    | GTT                |                            | GCT |                   | GAT                | (Asp/D) Aspartic acid (Glu/E) Glutamic acid | GGT                |                    | Т   |
|      | GTC                | (Val/V) Valine             | GCC | (Ala/A) Alanine   | GAC                |   | GGC                | (Gly/G) Glycine    | С   |
|      | GTA                |                            | GCA |                   | GAA                |   | GGA                |                    | Α   |
|      | GTG                |                            | GCG |                   | GAG                |   | GGG                |                    | G   |

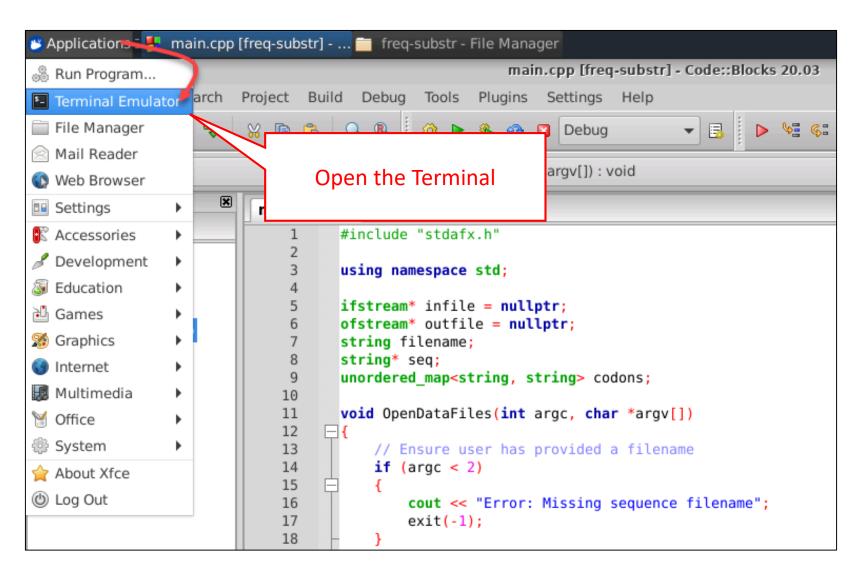
#### View Lab 3 – Substring Frequency

```
void AddCodon(string label, vector<string> segs)
    for (auto& s : segs)
        codons.insert(pair<string, string>(s, label))
void InitCodons()
    AddCodon("Ala", { "GCT", "GCA", "GCC", "GCG" });
                                                              // Alanine (Ala/A)
   AddCodon("Arg", { "CGT", "CGC", "CGA", "CGG", "AGA", "AGG" }); // Arginine (Arg/R)
    AddCodon("Asn", { "AAT", "AAC" });
                                                                // Asparagine (Asn/N)
    AddCodon("Asp", { "GAT", "GAC" });
                                                                // Aspartic Acid (Asp/D)
    AddCodon("Cys", { "TGT", "TGC" });
                                                                // Cvsteine (Cvs/C)
    AddCodon("Gln", { "CAA", "CAG" });
                                                                // Glutamine (Gln/0)
    AddCodon("Glu", { "GAA", "GAG" });
                                                                // Glutamic Acid (Glu/E)
    AddCodon("Gly", { "GGT", "GGC", "GGA", "GGG" });
                                                                // Glycine (Gly/G)
    AddCodon("His", { "CAT", "CAC" });
                                                                // Histidine (His/H)
    AddCodon("Ile", { "ATT", "ATC", "ATA" });
                                                                // Isoleucine (Ile/I)
    AddCodon("Leu", { "TTA", "TTG", "CTT", "CTC", "CTA", "CTG" });
                                                                // Leucine (Leu/L)
    AddCodon("Lys", { "AAA", "AAG" }):
                                                                // Lysine (Lys/K)
    AddCodon("Met/Start", { "ATG" });
                                                                // Methionine (Met / M) & Start
    AddCodon("Phe", { "TTT", "TTC" });
                                                                // Phenylalanine (Phe/F)
    AddCodon("Pro", { "CCT", "CCC", "CCA", "CCG" });
                                                                // Proline (Pro/P)
    AddCodon("Ser", { "TCT", "TCC", "TCA", "TCG", "AGT", "AGC" });
                                                                // Serine (Ser/S)
    AddCodon("Thr", { "ACT", "ACC", "ACA", "ACG" });
                                                                // Threonine (Thr / T)
    AddCodon("Trp", { "TGG" });
                                                                // Tryptophan (Trp/W)
    AddCodon("Tyr", { "TAT", "TAC" });
                                                                // Tyrosine (Tyr/Y)
    AddCodon("Val", { "GTT", "GTC", "GTA", "GTG" });
                                                                // Valine (Val/V)
    AddCodon("Stop", { "TAA", "TGA", "TAG" });
                                                                // Stop
```

#### **Build** Lab 3 – Substring Frequency

```
👺 Applications 🗄 👭 main.cpp [freq-substr] - ... 🚞 freq-substr - File Manager
                                                        main.cpp [freq-substr] - Code::Blocks 20.03
     Edit
         View
                         Project
                                Build
                                       Debug
                                              Tools Plugins Settings Help
                 Search
 P 🕒 🔒 🗐
                            Q R
                                                    A Debug
                                                                             ▼ 3
 <global>
                                   AddCodon(string labor
Management
                                                               Build the application
                           main.cpp
 Projects
                                    #include "stdafx.h"
   using namespace std;
     freq-substr
       Sources
                                    ifstream* infile = nullptr;
                              6
                                    ofstream* outfile = nullptr;
         main.cpp
                                    string filename;
       Headers
                                    string* seq;
                                    unordered map<string, string> codons;
       Others
                              9
                             10
                             11
                                    void OpenDataFiles(int argc, char *argv[])
                             12
                                  ⊟{
                             13
                                        // Ensure user has provided a filename
                                        if (argc < 2)
                             14
                             15
                             16
                                            cout << "Error: Missing sequence filename";</pre>
                                            exit(-1);
                             17
                             18
                              19
```

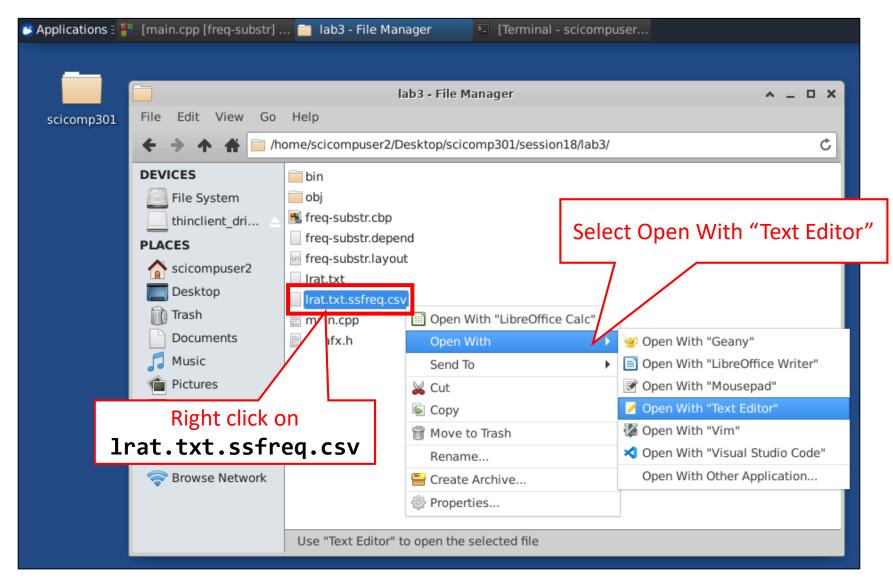
## Run Lab 3 – Substring Frequency



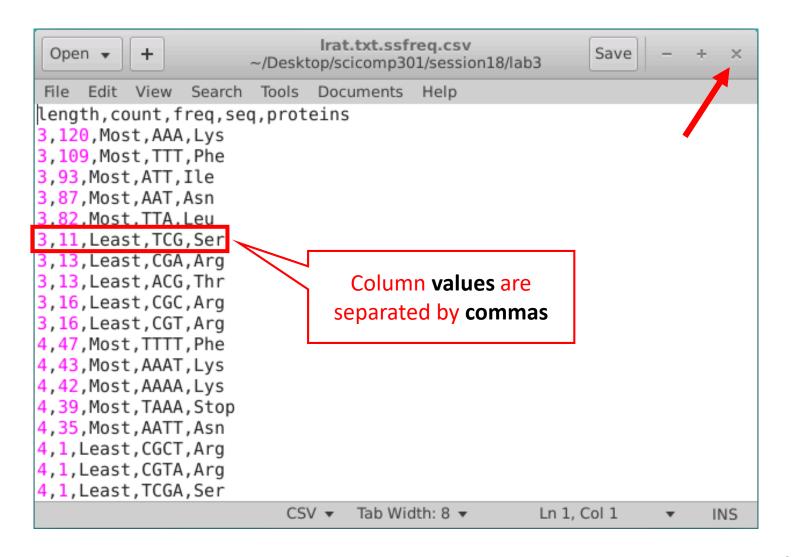
#### **Check** Lab 3 – Substring Frequency

```
Terminal - scicompuser2@ip-172-31-61-38: ~/Desktop/scicomp301/session18/lab3/bin/Debug
    Edit View Terminal Tabs Help
scicompuser2@ip-172-31-61-38:~$ cd Desktop/scicomp301/session18/lab3/bin/Debug
scicompuser2@ip-172-31-61-38:~/Desktop/scicomp301/session18/lab3/bin/Debug$ ./fr
Creating file "../../lrat.txt.ssfreq.csv" ... done!
scicompuser2@ip-172-31-61-38:~/Desktop/scicomp301/session18/lab3/bin/Debug$
            cd Desktop/scicomp301/session18/lab3/bin/Debug
            ./freq-substr ../../lrat.txt
```

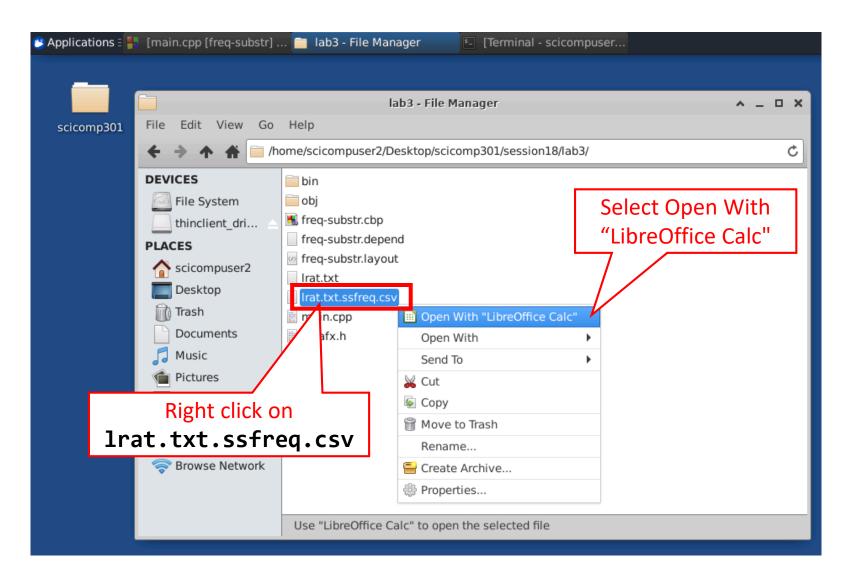
#### **Check** Lab 3 – Substring Frequency



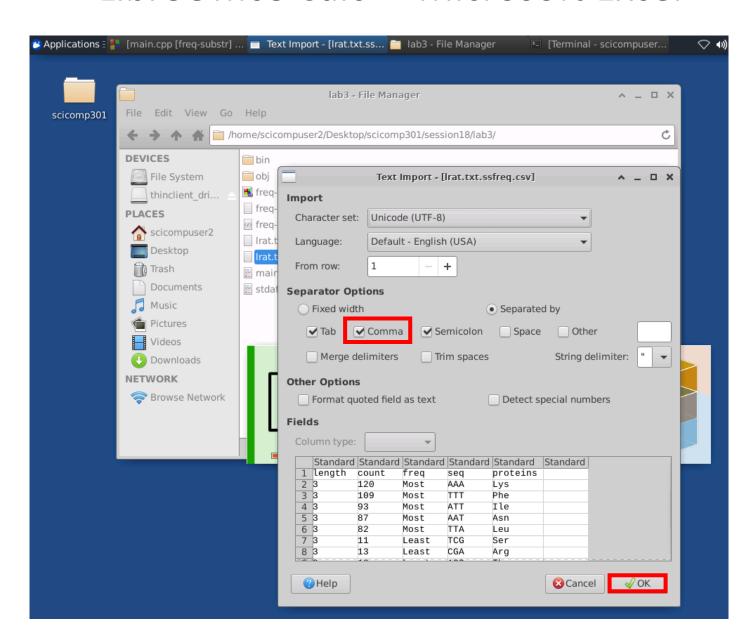
#### Comma Separated Value Files (.CSV)

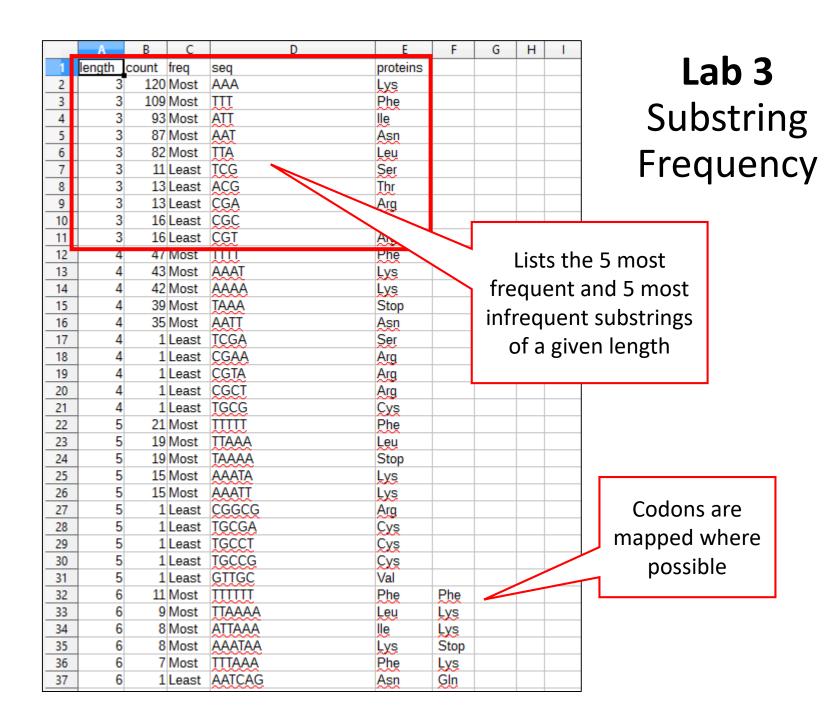


#### **Check** Lab 3 – Substring Frequency



#### LibreOffice Calc ≈ Microsoft Excel





# **Check** Lab 3 – Substring Frequency

| 17 | 1 | LCUST | AAGCAAGATTCAATTCC   | cys, om, Asp, scr, nc         |      |    |   |            |                |      |   |  |  |
|----|---|-------|---------------------|-------------------------------|------|----|---|------------|----------------|------|---|--|--|
| 17 | 1 | Least | AGCAAGATTCAATTCCT   | Ser, Lys, Ile, Gln, Phe       |      |    | Dave Biersac  | h:         |                |      |   |  |  |
| 18 | 1 | Most  | TCTGCTCCTCGGGCGGCC  | Ser, Ala, Pro, Arg, Ala, Ala  | FGG  | •  | This protein is important for blood clot formation (coagulation), which is needed to stop excessive |            |                |      |   |  |  |
| 18 | 1 | Most  | CTGCTCCTCGGGCGGCCT  | Leu, Leu, Leu, Gly, Arg, Pro  | FGG  |    |   |            |                |      | 9 |  |  |
| 18 | 1 | Most  | TGCTCCTCGGGCGGCCTT  | Cys, Ser, Ser, Gly, Gly, Leu  | FGG  |    | bleeding after injury   |            |                |      |   |  |  |
| 18 | 1 | Most  | GCTCCTCGGGCGGCCTTG  | Ala, Pro, Arg, Ala, Ala, Leu  | FGG  | -  |   |            |                |      |   |  |  |
| 18 | 1 | Most  | CTCCTCGGGCGGCCTTGA  | Leu, Leu, Gly, Arg, Pro, Stop | FGG  |    |   |            |                |      |   |  |  |
| 18 | 1 | Least | ATTAAAGCAAGATTCAAT  | Ile, Lys, Ala, Arg, Phe, Asn  | LRAT |    |   |            |                |      |   |  |  |
| 18 | 1 | Least | TTAAAGCAAGATTCAATT  | Leu, Lys, Gln, Asp, Ser, Ile  | LRAT |    |   |            |                |      |   |  |  |
| 18 | 1 | Least | TAAAGCAAGATTCAATTC  | Stop, Ser, Lys, Ile, Gln, Phe | LRAT |    |   | Dave Biers |                | ach: |   |  |  |
| 18 | 1 | Least | AAAGCAAGATTCAATTCC  | Lys, Ala, Arg, Phe, Asn, Ser  | LRAT | MN | ИΕ  | ١ ١        | A common act   | cute |   |  |  |
| 18 | 1 | Least | AAGCAAGATTCAATTCCT  | Lys, Gln, Asp, Ser, Ile, Pro  | LRAT |    |   |            | lymphocytic le |      |   |  |  |
| 19 | 1 | Most  | TCTGCTCCTCGGGCGGCCT | Ser, Ala, Pro, Arg, Ala, Ala  |      |    |   | antigen    |                |      |   |  |  |
| 19 | 1 | Most  | CTGCTCCTCGGGCGGCCTT | Leu, Leu, Leu, Gly, Arg, Pro  |      |    |   | l          |                |      |   |  |  |
| 19 | 1 | Most  | TGCTCCTCGGGCGGCCTTG | Cys, Ser, Ser, Gly, Gly, Leu  |      |    |   |            |                |      |   |  |  |

#### **LRAT Genetic Homologs**

#### **FGG**

From Wikipedia, the free encyclopedia

**Fibrinogen gamma chain**, also known as **FGG**, is a human gene found on Chromosome 4.

The protein encoded by this gene is the gamma component of fibrinogen, a blood-borne glycoprotein composed of three pairs of nonidentical polypeptide chains. Following vascular injury, fibrinogen is cleaved by thrombin to form fibrin which is the most abundant component of blood clots. In addition, various cleavage products of fibrinogen and fibrin regulate cell adhesion and spreading, display vasoconstrictor and chemotactic activities, and are mitogens for several cell types. Mutations in this gene lead to several disorders, including dysfibrinogenemia, hypofibrinogenemia and thrombophilia. [1] Alternative splicing of the mRNA chain results in two transcript variants; the common  $\gamma A$  chain and the alternatively spliced  $\gamma$ ' chain. Approximately 10% of the total plasma fibrinogen consists of  $\gamma A/\gamma$ ' fibrinogen, with <1% consisting of  $\gamma$ '/ $\gamma$ ' fibrinogen. Increased and decreased levels of  $\gamma A/\gamma$ ' fibrinogen have been associated with CAD and DVT respectively.

#### FGG

AGGTGTCTGTGCAGAAGTCTACTAGCAACCCCAAGTTCCAGCTGTCCGAAACGCTCCCACTCACCTTCAGATACCCCAGGTCTCCCTTCAGTTTGCTGGTTCTGGCAACCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCCTGACCAGAACGTGAACCTG GGTGTGGCAATGTCTACTGAGTGAAGGGTGAAGAGGTCAAGATGGACTCCAAGATCCAGGTTTTATCCAAAGGGTTGAATTCCGGCAGCCCCACATCCTGGACGCCCAGAAGATGCTGTGGAACCACACGGGACAGGAACCAGGAACCTGCCTCCTCTGGCCC TAACTCTTGGCTGAAGCTCTTACACCAATGCTGGGGGACATGTACCTCCCAGGGGCCCAGGAAGACTACGGGAGGCTACACCAACGTCAATCAGAGGGGCCTGTGTAGCTACCGATAAGCGGACCCTCAAGAGGGGCATTAGCAATAGTGTTTATAAGG CCCCCTTGTTAACCCTAAACGGGTAGCATATGCTTCCCGGGTAGTAGTATATACTATCCAGACTAACCCTAATTCAATAGCATATGTTACCCCAACGGGAAGCATATGCTATCGAATTAGGGTTAGTAAAAGGGTCCTAAGGAACAGCGATATCTCCCA CCCCATGAGCTGTCACGGTTTTATTTACATGGGGTCAGGATTCCACGAGGGTAGTGAACCATTTTAGTCACAAGGGCAGTGGACTGAACATCACGGGGCAGTGAACCTCTCCTGAATCTTCGCCTGCTTCTTCATTCTCCTTCGTTTAGCTAATAG AATAACTGCTGAGTTGTGAACAGTATGTGAGGTGCTCGAAAACAAGGTTTCAGGTGACGCCCCCAGAATAAAATTTGGACGGGGGGTTCAGTGGCATTGTGCTATGACACCAATATAACCCTCACAAAACCCTTGGGCAATAAAATACT AGTGTAGGAATGAAACATTCTGAATATCTTTAACAATAGAAATCCATGGGGTGGGGACAAGCCGTAAAGACTGGATGTCCATCTCACACGAATTTATGGCTATGGGCAACACATAATCCTAGTGCAATATGATACTGGGGTTATTAAAGATGTGTCCCA GGCCACTCTTTTTTTTGAAATTGTGGAGTGGGGCACGCGTCAGCCCCCACACGCCGCCTCGCGGTTTTGGACTGTAAAATAAGGGTGTAATAACTTGGCTGATTGTAACCCCCGCTAACCACTGCCGGTCAAACCACTTGCCCACAAAACCACTAATGG AGCATAGGCTATCCTAATCTAATCTGGGTAGCATATGCTATCCTAATCTGGGTAGCATATCTGATATCTGGGTAGCATATCCTAATCTGATACCTAATCTAATCTGAGTAGCATATCTAATCTAATCTAATCTGAGTAGCATATCTAATCTGAGTAGCATATCTAATCTGAGTAGCATATCTAATCTAATCTGAGTAGAATCTAATCTAATCTGAGTAGAATCTAATCA CTACCCAAATATCTGGATAGCATATGCTATCCTAATCTATATCTGGGTAGCATATGCTATCCTAATCAAT GGCCTCGTGATACGCCTATTTTTATAGGTTAATGTCATGATAATAATGGTTTCTTAGACGTCAGGTGGCACTTTTCGGGGAAATGTGCGCGGAACCCCTATTTGTTTATTTTTCTAAATACATTCAAATATGTATCCGCTCATGAGACAATAACCCTG ATAAATGCTTCAATAATATTGAAAAAGGAAGGTATTCAACATTTCCGTGTCGCCCCTTATTCCCTTTTTTGCGGCATTTTTGCTCACCCAGAAACGCTGGTGAAAGTAAAAGATGCTGAAGATCAGTTCGGTGCACCAGA TGGGTTACATCGAACTGGATCTCAACAGCGGTAAGATCCTTGAGAGTTTTCGCCCCGAAGAACGTTTTCCAATGATGAGCACTTTTAAAGTTCTGCTATGTGGCGCGGGTATTATCCCGTGTTGACGCCGGGCAAGAGCAACTCGGTCGCCGCATACAC TTAATTTAAAAGGATCTAGGTGAAGATCCTTTTTGATAATCTCATGACCAAAATCCCTTAACGTGAGTTTTCGTTCCACTGAGCGTCAGACCCCGTAGAAAAGGATCTACTTCTTGAGATCCTTTTTTTCTGCGCCGTAATCTGCTGCTTGCAAA CAAAAAAACCACCGCTACCAGCGGTGGTTTGTTTGCCGGATCAAGAGCTACCAACTCTTTTTCCGAAGGGTAACTGGCTTCAGCAGAGCGCAGATACCAAATACTGTTCTTCTAGTGTAGCCCGCTAGTTAGGCCACCACTCTAAGAACCTCTGTTAGCACCG CCTACATACCTCGCTCTGCTAATCCTGTTACCAGTGGCTGCCAGTGGCGATAAGTCGTGTCTTACCGGGTTGGACCCAGCCGATAGTTACCGGGTTAACCGGGTTAACCGGGTTGCACAGACGGGGGTTCGTGCACAGCCCAGCCTTGGAGCGAAC GACCTACACCGAACTGAGATACCTACAGCGTGAGCTATGAGAAAGCGCCACGCTTCCCGAAGGGGAGAAAGGCGGAGAGAGGGTATCCGGTAAGCGGCAGGGTCGGAACAGGAGGGGCGCACGAGGGAGCTTCCAGGGGGAAACGCCTGGTATCTTTATAGTC TAGTCATTGGTTATATAGCATAAATCAATATTGGCCATTGCCATGCCATGCATACGTTGTATCATATCATAATATGTACATTTATATTGGCCCATGTCCAATATGACCGCCATGTTGACATTATTGACTAGTTATTAATAGTAATCAATTACGGGG GGAGTATTTACGGTAAACTGCCCACTTGGCAGTACATCAAGTGTATCATATGCCAAGTCCGCCCCTATTGACGTCAATGACGGTAAATGGCCCGCCTGGCATTATGCCCAGTACATGACCTTACGGGACTTTCCTACTTGGCAGTACATCTACGTAT TAGTCATCGCTATTACCATGGTGATGCGGTTTTGGCAGTACACCAATGGGCGTGGATACGCGGTTTGACTCCACGGGGATTTCCAAGTCTCCACCCCATTGACGTCAATGGGGAGTTTTGTTTTGGCACCAAAATCAACGGGACTTTCCAAAATGTCGTAAT AACCCCGCCCGTTGACGCAAATGGGCGGTAGGCGTGTACGGTGGGAGGTCTATATAAGCAGAGCTCGTTTAGTGAACCGTCAGATCCTCACTCTCTCCCGCATCGCTGTCTGCGAGGGCCCAGCTGTTGGGCTCGCGGTTGAGGACAACTCTTCGCG GTCTTTCCAGTACTCTTGGATCGGAAACCCGTCGGCCTCCGAACGGTACTCCGCCACCGAGGGACCTGAGCGAGTCCGCATCGACCGGATCGGAAAACCTCTCGAGAAAGGCGTCTAACCAGTCGCAAGGTAGGCTGAGCACCGTGGCGGGC GGCAGCGGGTGGCGGTCGGGGTTGTTTCTGGCGGAGGTGCTGCTGATGATGTAATTAAAGTAGGCGGTCTTGAGACGGCGGATGGTCGAGGTGGGGGTGGCAGGCTTGAGATCCAGCTGTTGGGGTGAGTACTCCCTCTCAAAAGCGGGCATTACTT CTGCGCTAAGATTGTCAGTTTCCAAAAACGAGGAGGATTTGATATTCACCTGGCCCGATCTGGCCATACACTTGAGTGACATGACATTGCCTTTCTCCCACAGGTGTCCACTCCCAGGTCCAAGTTTAAACTGCGGCCGCCACCATGGTC GAGCACCTATCAGACTAAGGTCGACAAGGATCTGCAGAGCCTGGAAGATATCCTGCACCAGGTGGAGAACAAGACCAGCGAAGTGAAGCCGACCTACCAGCCTGACCTACCAGCCTACCAACCCCGACGAGAGCAGCAAGCCCAACATGATCGACCCCG CGGCGTGTACTACCAGGGCGGCACCTACAGCAAGGCCAGCACCCCCAACGGCTACGACAACGGCATCATCTGGGCCACCTGGAAAACCCGGTGGTACAGCATGAAGAAAACCCACCATGAAGATCATCCTTTCAACAGACTGACCATCGGCGAGGGCC AGCAGCATCACCTGGGCGGAGCCAAACAGGTCCGGCCTGAGCACCCTGCCGAGACAGAGTACGACAGCCTGTACCCCGAGGACGACCTGTGAGGCGCGCCC

#### Trail of Discovery

#### Resistance of cancer cells to immune recognition and killing.

Lipinski B<sup>1</sup>, Eavud LG.

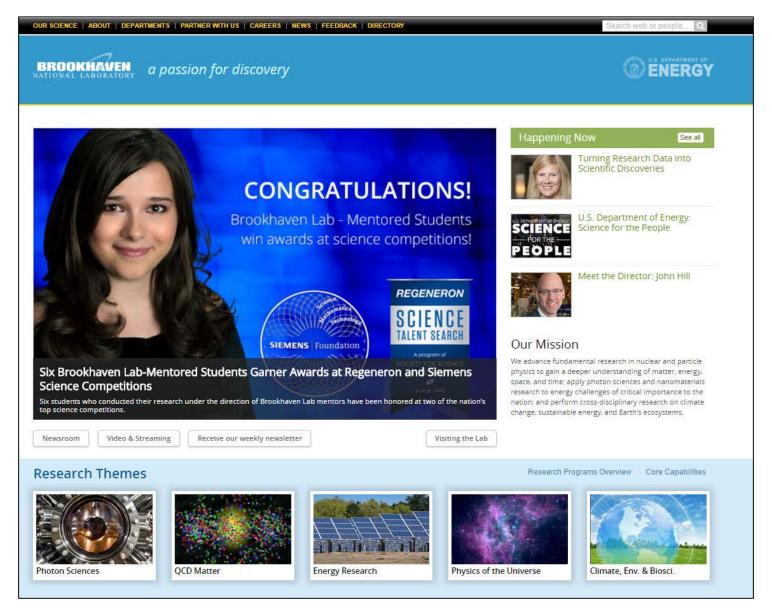
**Author information** 

#### Abstract

It is well recognized that, in order for a wound to heal, the fibrin clot must be eliminated by fibrinolytic enzymes. In certain instances, however, fibrin is ineffectively degraded or even not degraded. For example, in pregnancy, the placenta contains a layer of fibrin (Nitabuck's layer) which presents as 'self' to the immune system. Similar situations have been observed in many solid tumors. A hypothesis is presented according to which tumor cells can escape detection and attack by the immune system in most cancer patients. The tumor dons a 'coat' of the host's own protein on its cell surface. The coat is composed of fibrin and of a polymeric form of human serum albumin (HSA) which, by contrast to pure fibrin, is resistant to fibrinolytic degradation. Such a coated tumor appears as 'self' to the immune system, and thus is not detected as a tumor by the immune system (i.e. natural killer cells). When tumors are prepared for in vitro assays against drugs, they are routinely treated with proteolytic enzymes (e.g. pepsin, or chymotrypsin, etc.) which dissolve the protein coat, exposing the tumor cell surface to the drug. Thus, the in vivo existence of a coat on the tumor surface may explain why some drugs have little or no effect in vivo, while the same drugs are active in vitro.

Prior thought: Cancer evades phagocytosis
New thought: Cancer evades **fibrinolysis** 

#### **Applied Scientific Computing**



## **Applied Scientific Computing**

#### Meet the Regeneron Scholars:

Finalist Emily Peterson: Smithtown High School East
Mentor: David Biersach, Information Technology Division
Title of Project: "Lecithin-Retinol Acyltransferase in Squamous Cell
Carcinoma: The Relationship Between Oncology and Wound Repair"

Emily Peterson met Brookhaven Lab mentor David Biersach at a scientific computing seminar he was giving at her high school, where he learned of her research on skin cancer. Emily's research, conducted as a Simons Fellow under the guidance of Stony Brook University Professor Marcia Simon, focused on the possibility that a gene expression problem might inhibit the production of an enzyme responsible for strengthening cell walls. As cancer is invasive, skin cells with weak walls are more susceptible to becoming tumorous. Biersach showed Emily how a classic



Finalist Emily Peterson

+ ENLARGE

computer algorithm that looks for repeated substrings can be used in a novel way to determine if DNA sequences are likely to have important biological functions. This is accomplished by searching the human genome for other occurrences of these repeated sequences. They discovered that this enzyme's sequence also occurs in an enzyme involved in blood clotting. When blood clots form to heal a wound, the human body knows to leave the clot alone until the wound is fully repaired. After healing, a chemical signal triggers the body to break down the clot. The similarity in gene sequences that Peterson discovered suggests that cancer cells potentially use the same "don't bother me" signaling mechanism as blood clots, thus allowing the tumor to continue to grow in stealth mode. This collaboration is an excellent example of how students can apply skills in scientific computing directly to their research projects. Peterson hopes to continue her research by studying the enzyme's 3D atomic structure.

#### **Applied Scientific Computing**

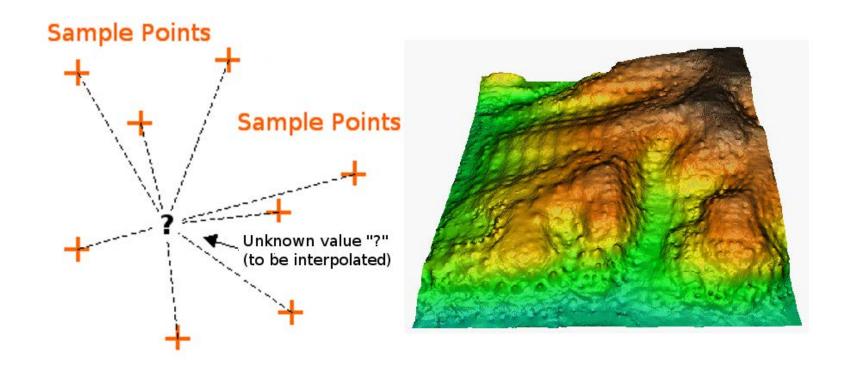


#### Trail of Discovery

- By considering not just the longest repeated substring, but also the five most (and five least) frequent substrings, Emily determined LRAT and FGG share common encodings
- FGG signals your body to remove blood clots after any damage is healed – it disposes healthy cells that are no longer needed
- Perhaps cancer tricks your immune system into thinking the cancerous cells are healthy and should not be disposed
- It may not be that the lack of LRAT results in a loss of cell membrane integrity (hence a greater chance of cancer spreading) – but there could be a link between something in LRAT and enabling cancer cell "stealth mode"

#### **Session Goals**

- Understand methods for interpolating multi-dimensional data taken from random sample locations
- Analyze the mathematics of the Inverse Distance Weighting (IDW) method
- Convert non-uniformly measured spatial data to a regular conforming mesh
- Develop approaches for estimating "goodness of fit" for predicted interpolated data points
- Use the Root Mean Square Deviation (RMSD) statistic as a measure of model accuracy



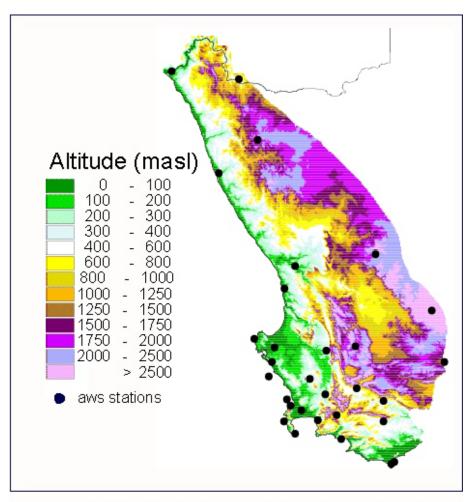
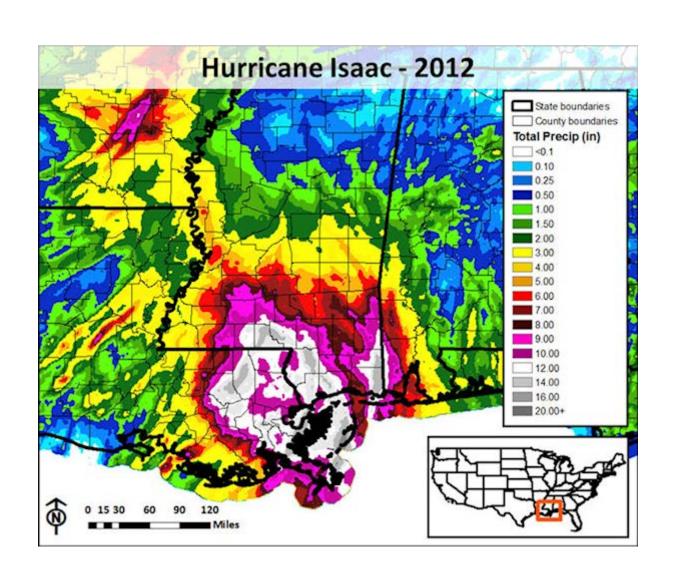
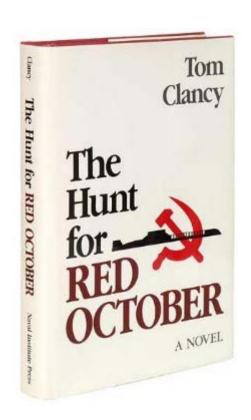
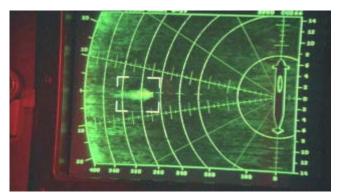


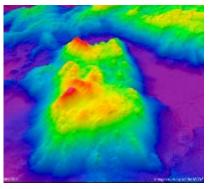
Figure 6 Altitude (200x200m) over the winter rainfall region of South Africa (after Directorate of Land Surveys and Information, 1996)



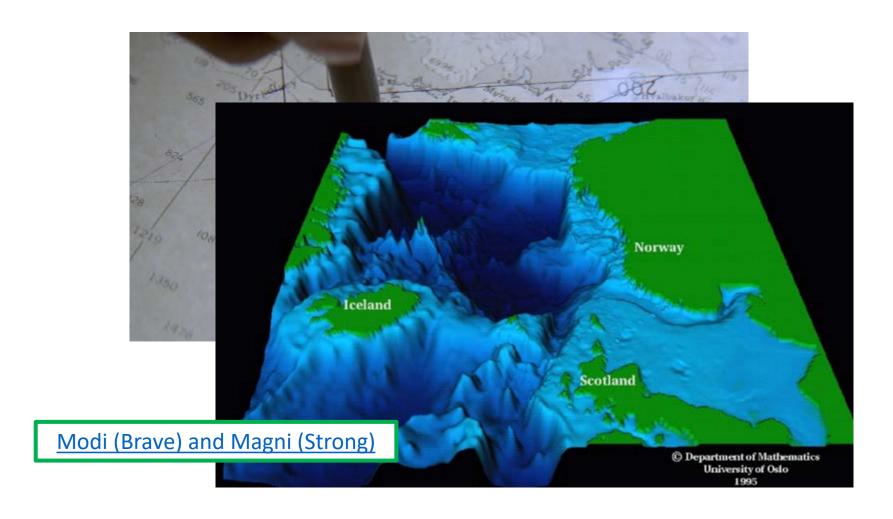


Jonsey Reports





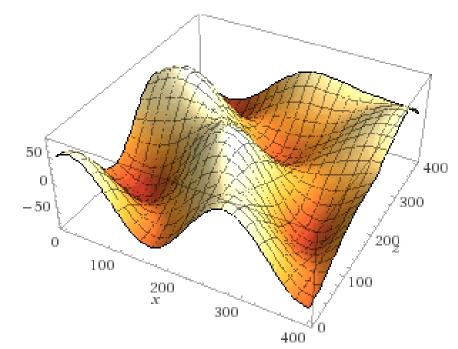




#### An "Actual" Ocean Floor

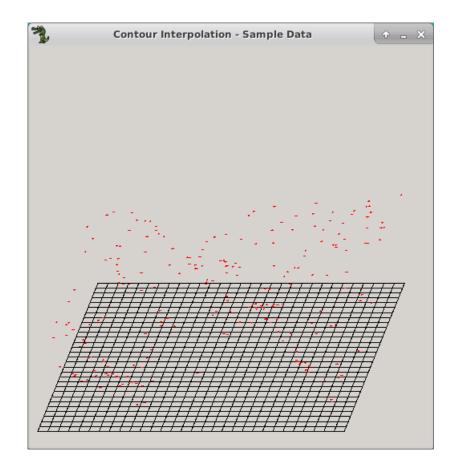
$$y = 30\sin\left(\frac{x}{4}\right)\cos\left(\frac{z}{4}\right) + 50\cos\left(\frac{\sqrt{x^2 + z^2}}{4}\right)$$





## Sample Ocean Depth Soundings

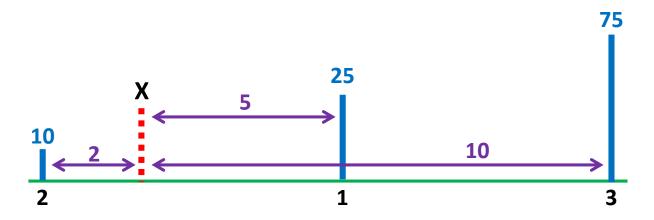
- Ocean area is 400 units square, partitioned into grid of 30 x 30 intervals
- Depth samples were taken from 220 random locations
- Floor reference grid has height y = -80
- Oblique projection



#### Sample Ocean Depth Soundings

```
void InitSamples()
   seed_seq seed{ 2017 }:
   default random engine prng{ seed };
    uniform int distribution<int> dist{ 0, oceanSize };
   // Generate random sample points
    for (size t i{};i < numSamples;++i) {</pre>
        samples[i].x = dist(prng);
        samples[i].z = -dist(prng);
        samples[i].y = GetActHeight(samples[i].x, samples[i].z);
   // Create a small marker at each sample point (a horizontal facet)
    for (size t i{};i < numSamples;++i)</pre>
        size_t v0 = vSamples.add(samples[i].x, samples[i].y, samples[i].z + 2);
        size t v1 = vSamples.add(samples[i].x + 2, samples[i].y, samples[i].z);
        size t v2 = vSamples.add(samples[i].x, samples[i].y, samples[i].z - 2);
        size t v3 = vSamples.add(samples[i].x - 2, samples[i].y, samples[i].z);
        fSamples.add(&vSamples, { v0,v1,v2,v3 });
```

- IDW is a type of <u>deterministic</u> method for <u>multivariate</u> interpolation of a set of <u>scattered</u> points
- The value assigned to unknown points are calculated from a weighted average of the values at the known points
- The theory is the farther away a known point is from the unknown point, the less that known distant point can contribute to the unknown height
- Closer known points contribute more to the unknown height than known points that are farther away
- Your contribution is inverse to your distance



Sample Index

Distance (d) from Sample to **X** Sample Known Height

| 1  | 2  | 3  |  |  |  |
|----|----|----|--|--|--|
| 5  | 2  | 10 |  |  |  |
| 25 | 10 | 75 |  |  |  |

Weight = 1/d^p (set p = 1)
Sample Height • Weight

| 0.2 | 0.5 | 0.1 | 0.8  |
|-----|-----|-----|------|
| 5   | 5   | 7.5 | 17.5 |

$$\left(\frac{17.5}{0.8}\right)$$
 Height at X = 21.875

**Totals** 

A general form of finding an interpolated value u at a given point x based on samples  $u_i = u(x_i)$  for i=1,2,...,N using IDW is an interpolating function:

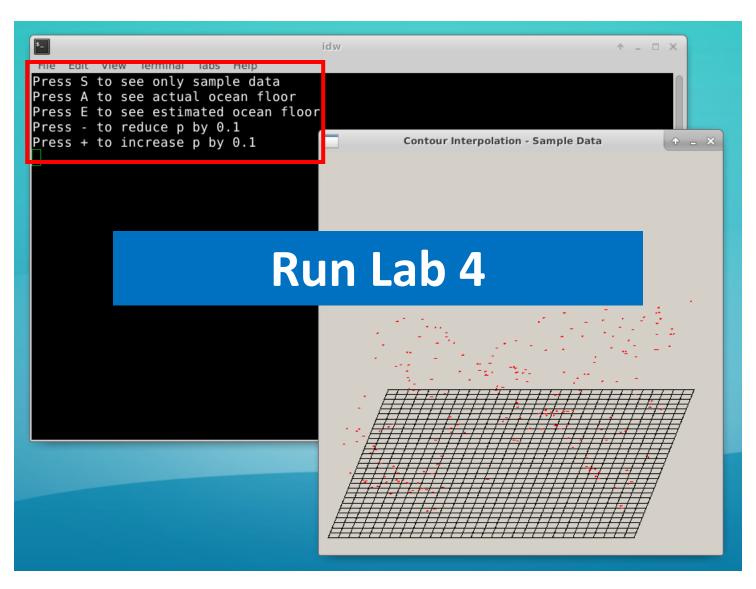
$$u(\mathbf{x}) = \begin{cases} \sum_{i=1}^{N} w_i(\mathbf{x}) u_i \\ \sum_{i=1}^{N} w_i(\mathbf{x}) \\ u_i, \end{cases} \text{ if } d(\mathbf{x}, \mathbf{x}_i) \neq 0 \text{ for all } i \end{cases}$$
where

$$w_i(\mathbf{x}) = \frac{1}{d(\mathbf{x}, \mathbf{x}_i)^p}$$

The p value indicates the "power" of the distance penalty

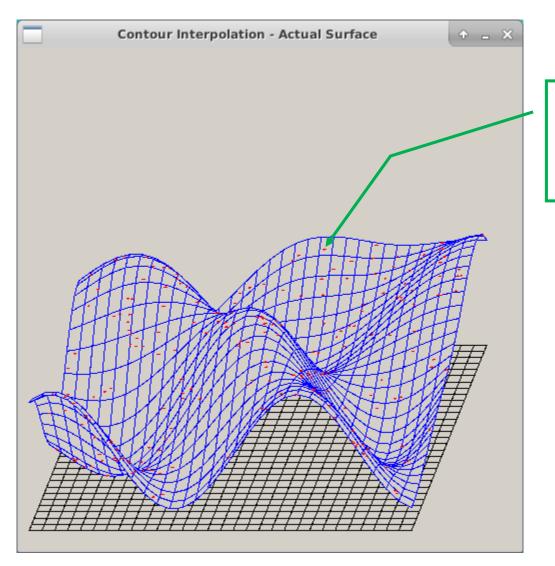
```
u(\mathbf{x}) = \begin{cases} \sum_{i=1}^{N} w_i(\mathbf{x}) u_i \\ \sum_{i=1}^{N} w_i(\mathbf{x}) \\ u_i, \end{cases} & \text{if } d(\mathbf{x}, \mathbf{x}_i) \neq 0 \text{ for all } i \end{cases} \\ v_i(\mathbf{x}) = \frac{1}{d(\mathbf{x}, \mathbf{x}_i)^p} \\ w_i(\mathbf{x}) = \frac{1}{d(\mathbf{x}, \mathbf{x}_i)^p} \\ v_i(\mathbf{x}) = \frac{1}{d(\mathbf{x},
```

#### Inverse Distance Weighting



#### **Actual Ocean Floor**

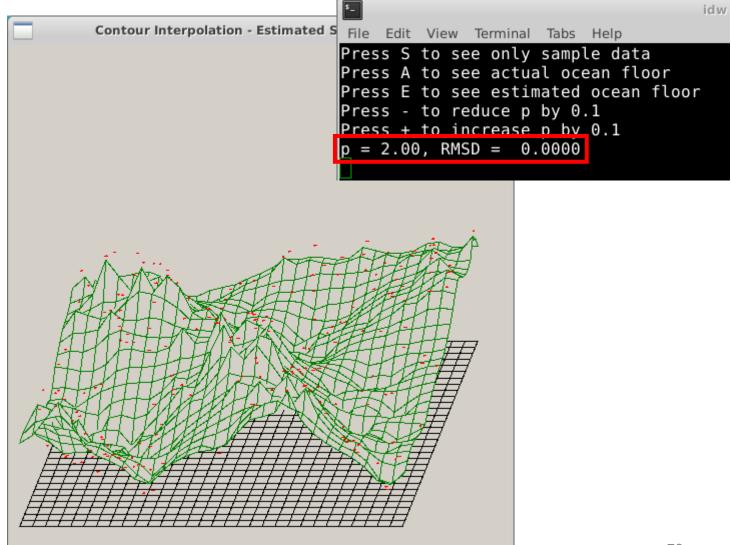
Press the **A**key to see
the <u>actual</u>
ocean floor



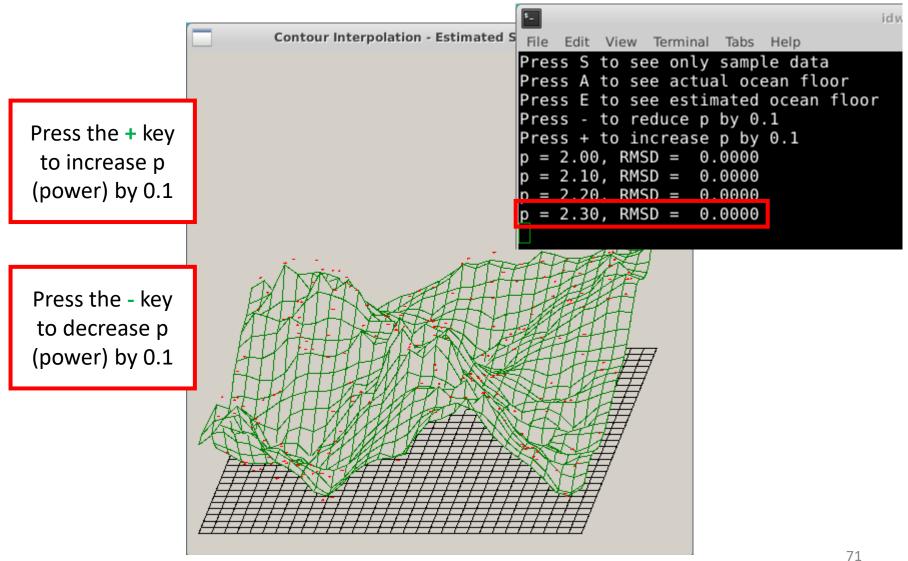
The **red** "dots" are the sample data points

#### **Estimated Ocean Floor**

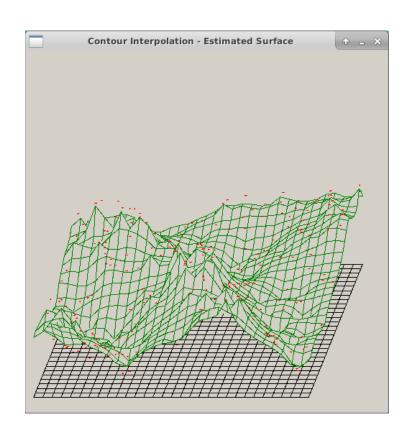
Press the **E**key to see the
estimated
ocean floor

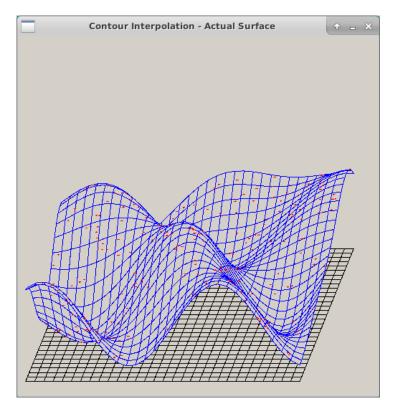


#### **Estimated Ocean Floor**



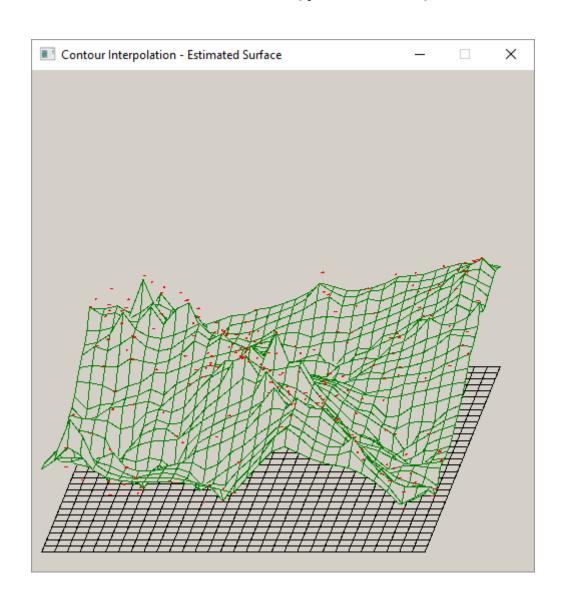
## Estimated vs Actual (p = 2.0)



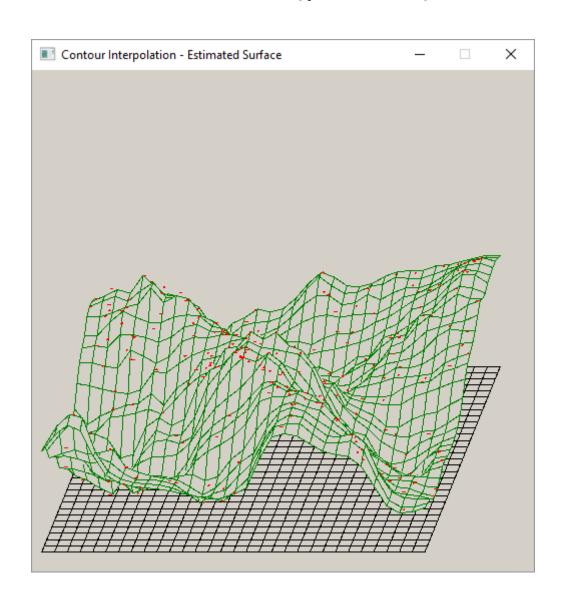


A first order approximation having only 24% of the world sampled (220 of 900 actual points)

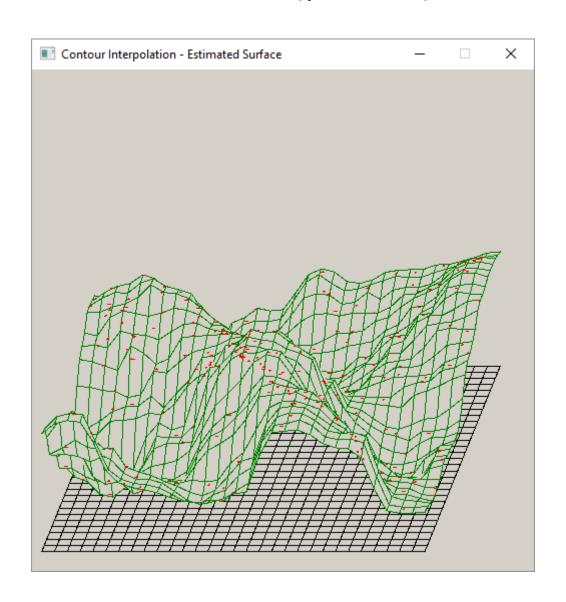
# Estimate (p = 2.0)



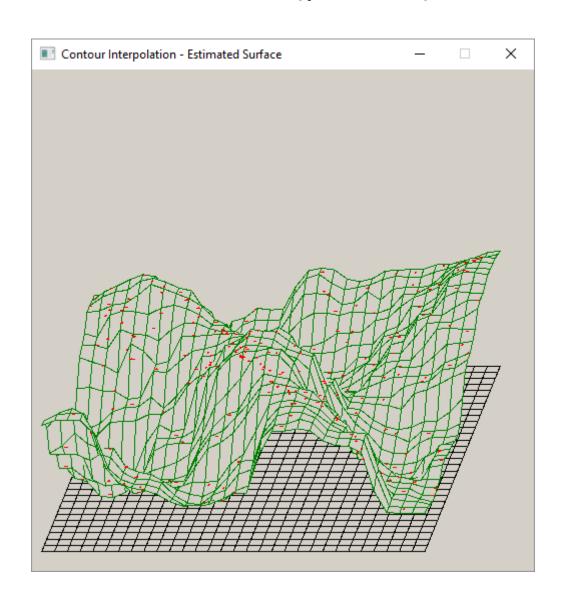
# Estimate (p = 3.0)



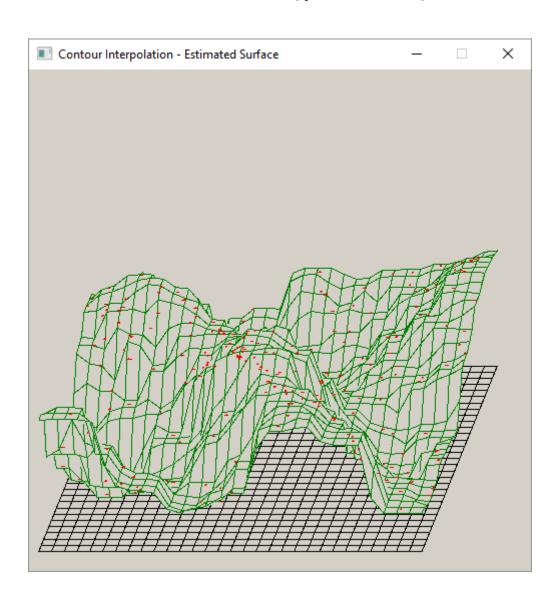
# Estimate (p = 4.0)



# Estimate (p = 5.0)



# Estimate (p = 9.0)



### Root Mean Square Deviation

- As we increase the **power** term **p**, is our model getting better or worse at predicting reality?
- The root-mean-square deviation (RMSD) is a statistic to measure the differences between values predicted by a model and the values actually observed

$$RMSD = \sqrt{\frac{\sum_{t=1}^{n} (\hat{y}_t - y)^2}{n}}.$$

• By averaging the errors  $(actual - estimated)^2$  across all sample points, we calculate a comparative statistic that can help empirically determine the optimal p value because it will minimize the overall error of the model

#### Edit Lab 4 - Calculate the RMSD

```
main.cpp 🗷
  77
  78
          double CalcRMSD()
  79
        □ {
              double rmsd = 0;
  80
  81
              double sumErrors = 0;
              for (int iz\{ intervals - 1 \}; iz >= 0; --iz )
  82
  83
                  for (int ix{}; ix < intervals; ++ix)</pre>
  84
  85
  86
                       double x = ix * delta:
  87
                       double z = -iz * delta;
                       double act = GetActHeight(x, z);
  88
  89
                       double est = GetEstHeight(x, z);
                      sumErrors += 0;
  90
  91
  92
  93
              rmsd = 0;
  94
              return rmsd;
  95
```



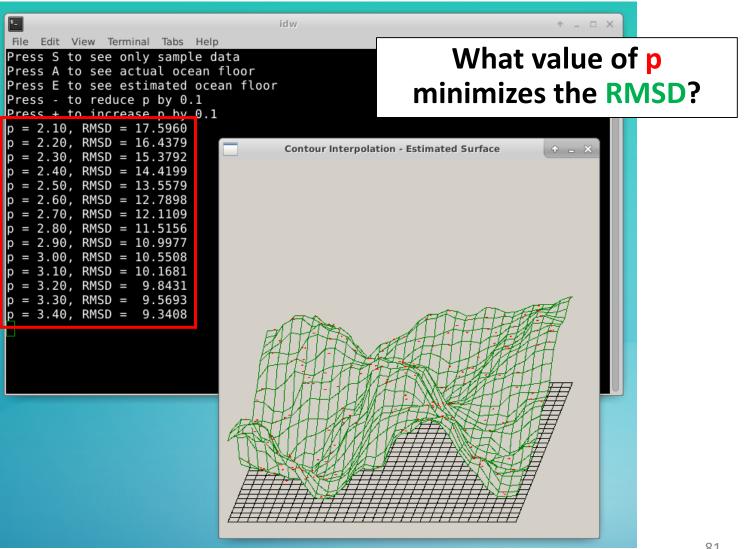
Fix the code to calculate sumErrors and rmsd

#### Edit Lab 4 - Calculate the RMSD

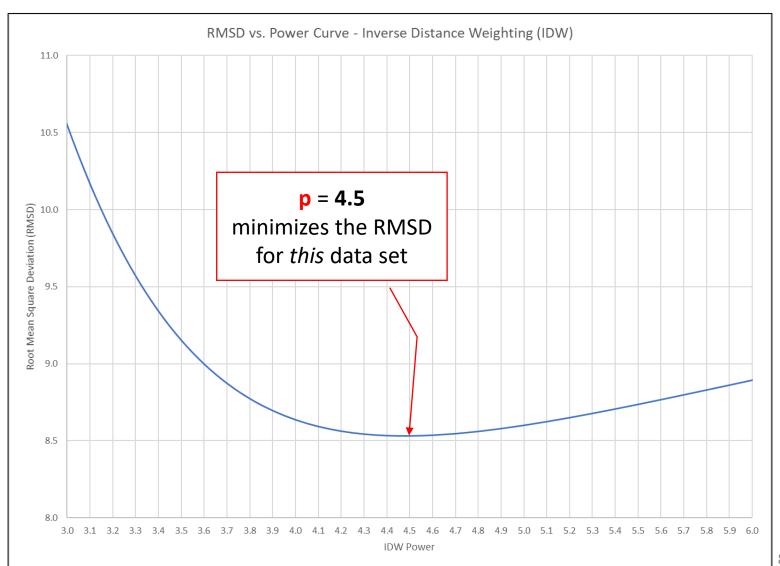
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  83
                  for (int ix{}; ix < intervals; ++ix)</pre>
  84
  85
                      double x = ix * delta;
  86
  87
                      double z = -iz * delta;
  88
                      double act = GetActHeight(x, z);
                      double est = GetEstHeight(x, z);
  89
  90
                      sumErrors += pow(act - est, 2)
  91
  92
  93
              rmsd = sgrt(sumErrors / (intervals * intervals));
  94
              return rmsd;
  95
```

What value of p minimizes the RMSD?

#### **Check** Lab 4 - Calculate the RMSD



### Graphing the **RMSD**



### Now you know...

- Identifying repeated sequences in DNA can lead to new understandings of genetic structure and purpose
  - Suffix sort is a very clever way to find the longest repeating substring (LRSS)
  - Sequence alignment tools (BLAST, etc.) look for which two sequences share a similar subsequence
  - Alternatively, LRSS looks inside a <u>single</u> sequence, to see what patterns might repeat <u>within it</u>
- There could be biological significance of a very long substring that appears only a <u>few</u> times within the entire sequence

### Now you know...

- The Inverse Distance Weighting (IDW) method can interpolate multi-dimensional data taken from random sample locations
  - How to convert non-uniformly measured spatial data into a regular conforming mesh
  - How to use RMSD as one metric to characterize the "goodness of fit" for predicted interpolated data points
- Scientists rarely enjoy the luxury of having too many data samples and must often <u>interpolate</u> to fill in the missing gaps