

# Survey of Scientific Computing (SciComp 301)

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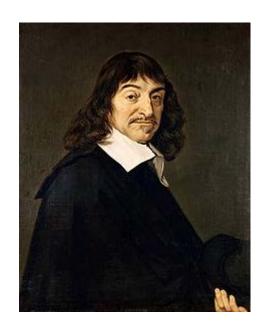
Session 05
2D Graphics,
Polar Coordinates

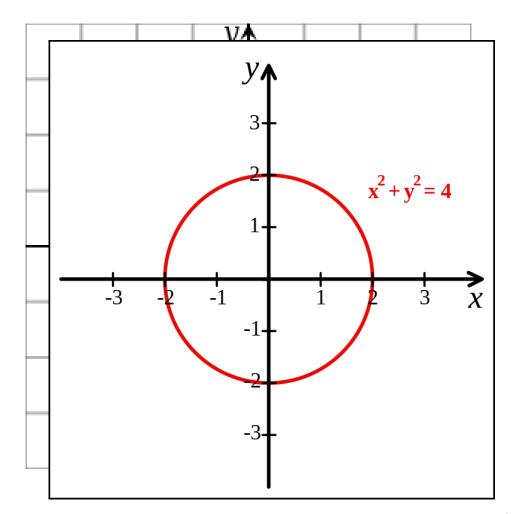
#### **Session Goals**

- Learn the SimpleScreen custom class to draw graphics
- Understand the World bounding rectangle
- Use Cartesian coordinates to draw 2D lines
- Use polar coordinates to draw 2D circles
- Approximate circles by dividing  $2\pi$  radians into intervals
- Use a delay count to watch each interval being drawn
- Appreciate the hidden geometry of the Olympic Rings
- Draw fancy curves using parametric equations

#### **Cartesian Coordinates**

Created by René Descartes in 1637



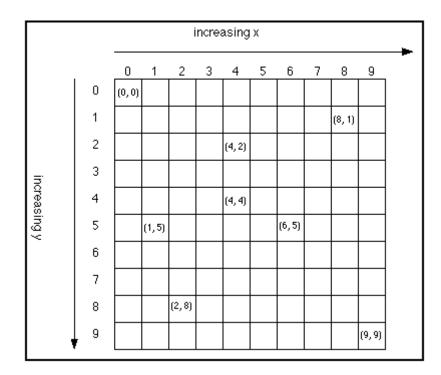


#### Screen Pixels

- A computer screen is divided into 2D array of small rectangles called pixels
- Every pixels has both an X and a Y coordinate
- Each pixel is set to a specific color
- The number of pixels in each dimension is the resolution
- Modern screens have resolutions greater than 1920 x 1080
- The top left screen pixel has coordinates (0,0) and there are no negative pixel coordinates
- Unfortunately there is an even greater **discrepancy** between Cartesian coordinates and pixel coordinates...

#### Screen Y vs. World Y Coordinates

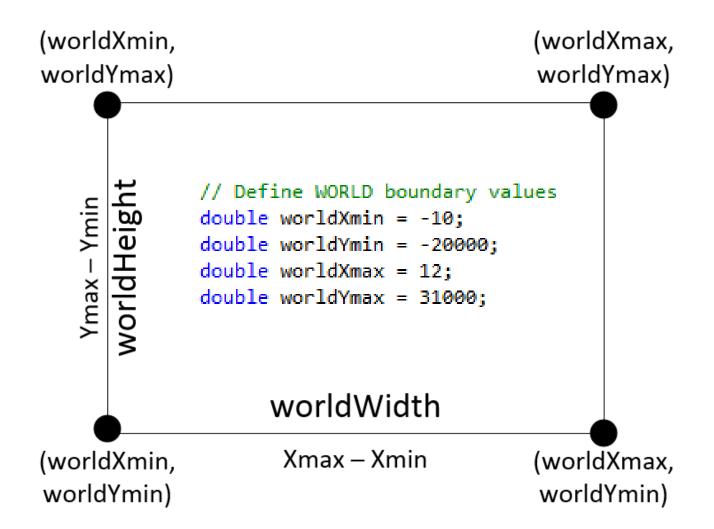
- In screen coordinates, as you move from the top of the screen towards the bottom, the Y coordinate increases!
- This is the <u>exact opposite</u> of world (Cartesian) coordinates
- Fortunately, the X axis behaves the as expected between the screen and world coordinate system
- This discrepancy will drive you nuts!



# World Bounding Rectangle

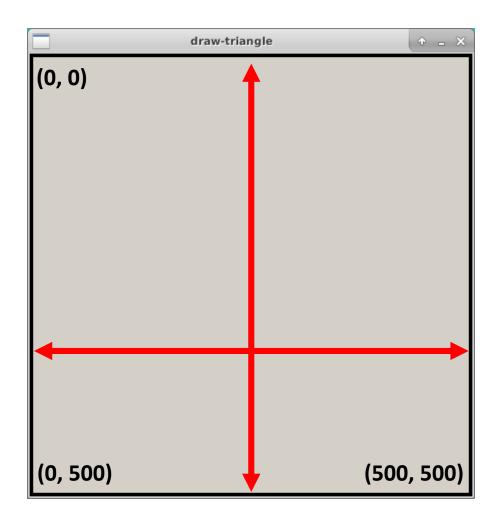
- World coordinates are what we use when doing pure math
- Screen coordinates are what we have to use when drawing
- We need a way to map World X,Y to Screen X,Y
- The world is framed by a "bounding rectangle" which is comprised of four variables of type double
  - worldYmin, worldYmin
  - worldYmax, worldYmax
- The values for all four World variables are our choice they can be as big or as small as we want them

# World Bounding Rectangle



# Screen Bounding Rectangle

- The Screen bounding rectangle is the size of the Allegro display bitmap
- Due to your smaller laptop screens, we set the size to be 501 x 501
- Remember Screen Y
   coordinates are inverted
   as (0,0) is in the top left

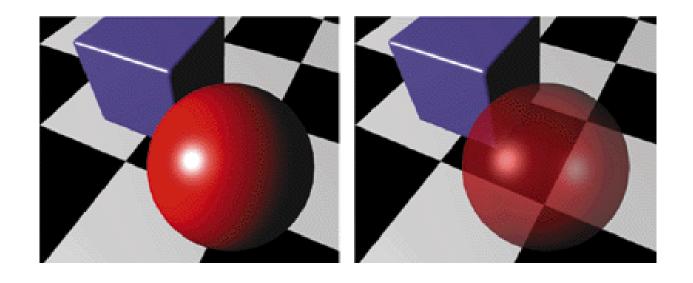


# **Argb Color Encoding**

#### 

```
ALLEGRO_COLOR clrRed = al_map_rgb(255, 0, 0); // Red ALLEGRO_COLOR clrGreen = al_map_rgb(0, 255, 0); // Green ALLEGRO_COLOR clrBlue = al_map_rgb(0, 0, 255); // Blue
```

# Alpha Blending = Opacity



Alpha = 0 means fully transparent (see through)

Alpha = 255 means fully opaque

We will be using Alpha = 255 in our code

#### Various Colors in **RGB** Values

94.28.13	241.148.108	97.119.171	90.103.39	164.131.196	140.253.153
11° 86% 37% 01 Dark Skin	18° 55% 95% 02 Light Skin	222° 43% 67% 03 Blue Sky	72° 62% 40% 04 Foliage	270° 33% 77% 05 Blue Flower	127° 46% 99% 06 Bluish Green
255.116.21	7.47.122	222.29.42	69.0.68	187.255.19	255.142.0
24° 92% 100% 07 Orange	219° 94% 48% 08 Purplish Blue	356° 87% 87% 09 Moderate Red	301° 100% 27% 10 Purple	77° 93% 100% 11 Yellow Green	33° 100% 100% 12 Orange Yellow
0.0.142	64.173.38	203.0.0	255.217.0	207.3.124	0.148.189
240° 100% 56% 13 Blue	108° 78% 68% 14 Green	0° 100% 80% 15 Red	51° 100% 100% 16 Yellow	324° 99% 81% 17 Magenta	193° 100% 74% 18 Cyan
255.255.255	249.249.249	180.180.180	117.117.117	53.53.53	0.0.0

# **Predefined Color "Names"**

AliceBlue	AntiqueWhite	Aqua	Aquamarine	Azure	Beige	Bisque
Black	BlanchedAlmond	Blue	BlueViolet	Brown	BurlyWood	CadetBlue
Chartreuse	Chocolate	Coral	CornflowerBlue	Cornsilk	Crimson	Cyan
DarkBlue	DarkCyan	DarkGoldenrod	DarkGray	DarkGreen	DarkKhaki	DarkMagenta
DarkOliveGreen	DarkOrange	DarkOrchid	DarkRed	DarkSalmon	DarkSeaGreen	DarkSlateBlue
DarkSlateGray	DarkTurquoise	DarkViolet	DeepPink	DeepSkyBlue	DimGray	DodgerBlue
Feldspar	Firebrick	FloralWhite	ForestGreen	Fuchsia	Gainsboro	GhostWhite
Gold	Goldenrod	Gray	Green	GreenYellow	Honeydew	HotPink
IndianRed	Indigo	lvory	Khaki	Lavender	LavenderBlush	LawnGreen
LemonChiffon	LightBlue	LightCoral	LightCyan	LightGoldenrodYellow	LightGray	LightGreen
LightPink	LightSalmon	LightSeaGreen	LightSkyBlue	LightSlateBlue	LightSlateGray	LightSteelBlue
LightYellow	Lime	LimeGreen	Linen	Magenta	Maroon	MediumAquamarine
MediumBlue	MediumOrchid	MediumPurple	MediumSeaGreen	MediumSlateBlue	MediumSpringGreen	MediumTurquoise
MediumVioletRed	MidnightBlue	MintCream	MistyRose	Moccasin	NavajoWhite	Navy
OldLace	Olive	OliveDrab	Orange	OrangeRed	Orchid	PaleGoldenrod
PaleGreen	PaleTurquoise	PaleVioletRed	PapayaWhip	PeachPuff	Peru	Pink
Plum	PowderBlue	Purple	Red	RosyBrown	RoyalBlue	SaddleBrown
Salmon	SandyBrown	SeaGreen	SeaShell	Sienna	Silver	SkyBlue
SlateBlue	SlateGray	Snow	SpringGreen	SteelBlue	Tan	Teal
Thistle	Tomato	Transparent	Turquoise	TVBlack	TVWhite	Violet
VioletRed	Wheat	White	WhiteSmoke	Yellow	YellowGreen	

# Allegro Graphics Library

http://liballeg.org



#### A game programming library

#### Allegro

About

Git repository

License

Language bindings

#### Downloads

Latest version

Older versions

Extra addons

#### Documentation

Latest version

All versions

Tutorials

Books

Wiki

#### Support

Forums Mailing lists

Bug tracker

IRC

Community

Allegro.cc

#### Welcome to Allegro!

Allegro is a cross-platform library mainly aimed at video game and multimedia programming. It handles common, low-level tasks such as creating windows, accepting user input, loading data, drawing images, playing sounds, etc. and generally abstracting away the underlying platform. However, Allegro is *not* a game engine: you are free to design and structure your program as you like.

Allegro 5 has the following additional features:

- . Supported on Windows, Linux, Mac OSX, iPhone and Android
- . User-friendly, intuitive C API usable from C++ and many other languages
- Hardware accelerated bitmap and graphical primitive drawing support (via OpenGL or Direct3D)
- Audio recording support
- · Font loading and drawing
- Video playback
- · Abstractions over shaders and low-level polygon drawing
- And more!

#### News

```
// SimpleScreen
class SimpleScreen
public:
    SimpleScreen(void(*draw)(SimpleScreen& ss) = nullptr,
        void(*eventHandler)(SimpleScreen& ss, ALLEGRO EVENT& ev)= nullptr);
    ~SimpleScreen();
    void SetWorldRect(double xMin, double yMin,
        double xMax, double yMax);
    void GetWorldRect();
    void SetProjection(double degrees = 45, double correction = 1);
    void SetCameraLocation(double x, double y, double z);
    void SetZoomFrame(string clr, double width = 2);
    void LockDisplay();
    void UnlockDisplay();
    void Clear();
    void Update();
    void Redraw();
    void Exit();
    void HandleEvents();
    bool Contains(double x, double y);
    void DrawAxes(string clr = "black", float width = 1);
    void DrawLine(Point2D &a, Point2D &b,
        string clr = "black", float width = 1);
   void DrawLines(PointSet* ps, string clr, float width = 1,
        bool close = true, bool fill = false, long delay = 0);
    void DrawLines(FacetSet* facets, string clr, float width = 1,
        bool fill = false, long delay = 0);
```

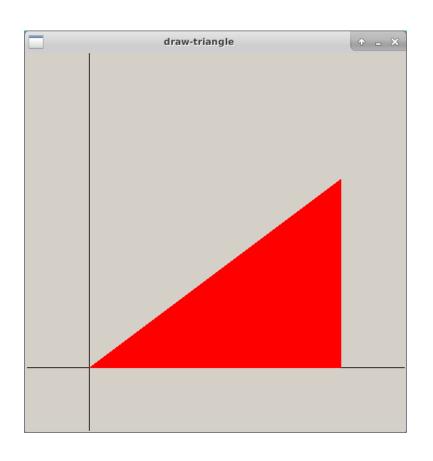
# The SimpleScreen Class



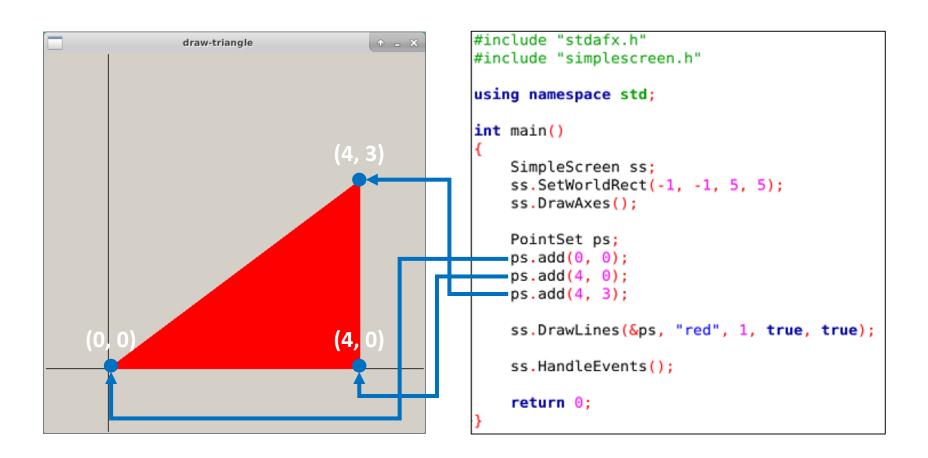
#### The **PointSet** Class

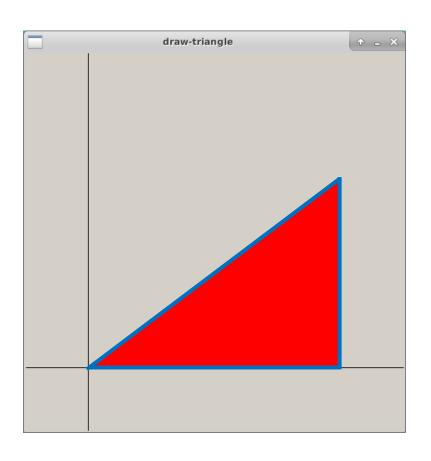
```
// PointSet
class PointSet
{
public:
    PointSet();
    ~PointSet();
    Point2D* at(size_t i);
    void clear();
    void add(double x, double y);
    size_t size();
private:
    vector<Point2D*>* points;
};
```

- No coding required just follow along main()
- Draw a 3-4-5 right triangle in the *first* quadrant
- Paint the entire triangle RED including the interior
- Set the correct world rectangle dimensions

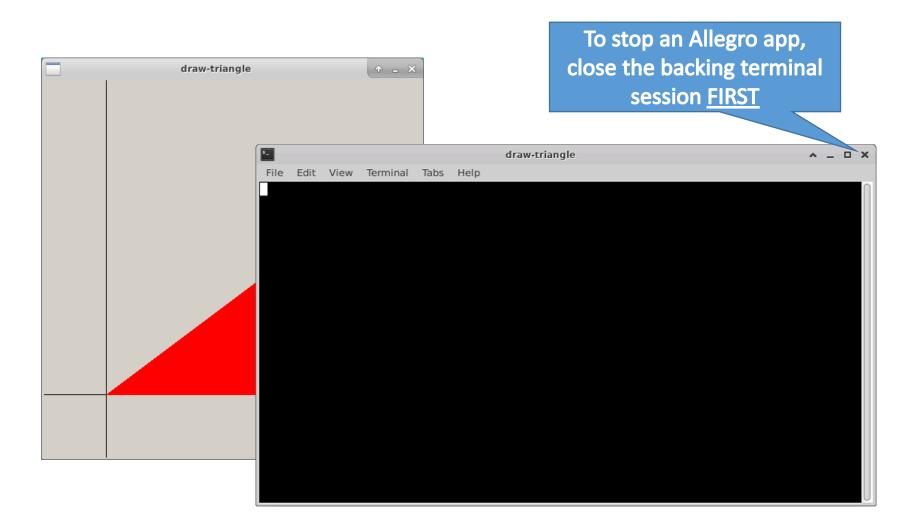


```
#include "stdafx.h"
#include "simplescreen.h"
using namespace std;
int main()
   SimpleScreen ss:
   ss.SetWorldRect(-1, -1, 5, 5);
    ss.DrawAxes();
    PointSet ps;
    ps.add(0, 0);
    ps.add(4, 0);
    ps.add(4, 3);
    ss.DrawLines(&ps, "red", 1, true, true);
    ss.HandleEvents();
    return 0;
```





```
#include "stdafx.h"
#include "simplescreen.h"
using namespace std;
int main()
    SimpleScreen ss;
    ss.SetWorldRect(-1, -1, 5, 5);
    ss.DrawAxes():
    PointSet ps;
    ps.add(0, 0);
    ps.add(4, 0);
    ps.add(4, 3);
    ss.DrawLines(&ps, "red", 1, true, true);
    ss.HandleEvents();
    return 0;
```



# Open Lab 2 – Draw Rectangle

- Draw a violet rectangle in the first quadrant
- The dimensions are: Area = 210 and Perimeter = 62
- Assume the world coordinates are (-30,-30) to (30,30)

```
int main()
{
    SimpleScreen ss;
    ss.SetWorldRect(-30, -30, 30, 30);
    ss.DrawAxes();

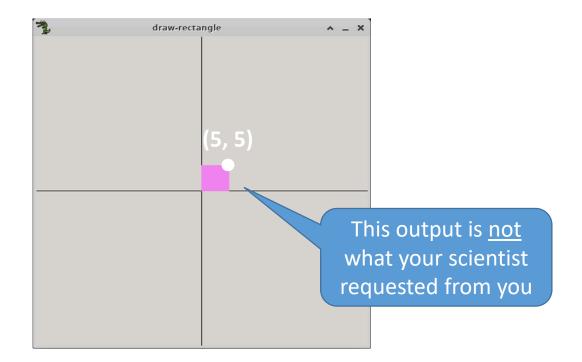
    PointSet ps;
    ps.add(0, 0);
    ps.add(5, 0);
    ps.add(5, 5);
    ps.add(0, 5);

    ss.DrawLines(&ps, "violet", 1, true, true);
    ss.HandleEvents();

    return 0;
}
```

### Run Lab 2 – Draw Rectangle

- Draw a violet rectangle in the first quadrant
- The dimensions are: Area = 210 and Perimeter = 62
- Assume the world coordinates are (-30,-30) to (30,30)

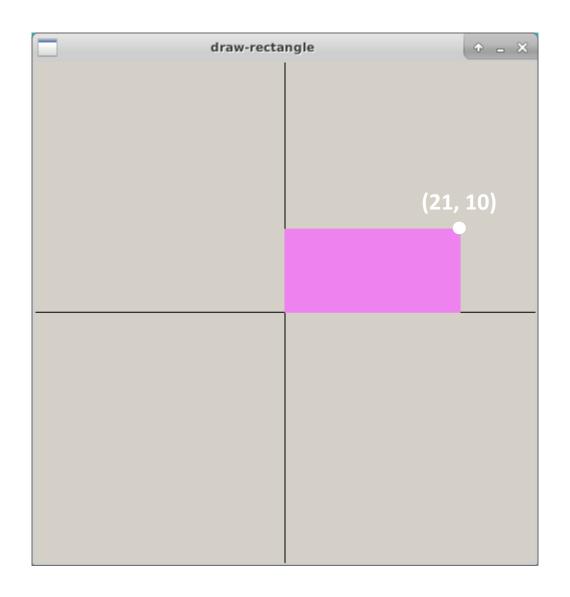


### Edit Lab 2 – Draw Rectangle

- Draw a violet rectangle in the first quadrant
- The dimensions are: Area = 210 and Perimeter = 62
- Assume the world coordinates are (-30,-30) to (30,30)
- Edit the coordinates of the three remaining corner points with the correct values

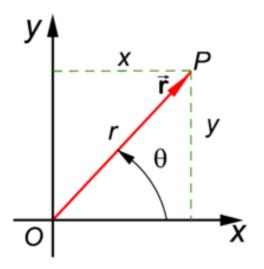
```
PointSet ps;
ps.add(0, 0);
ps.add(5, 0);
ps.add(5, 5);
ps.add(0, 5);
Fix these
last 3 points
```

# Check Lab 2 – Draw Rectangle

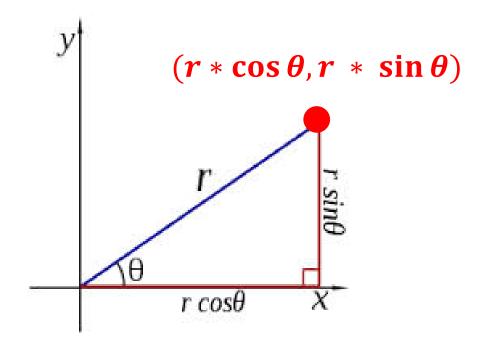




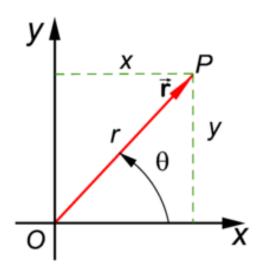
#### **Polar Coordinates**

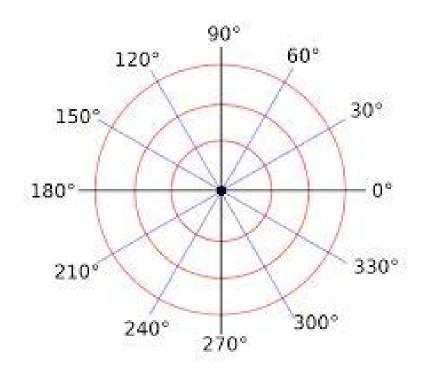


A radius and an angle (theta) make a 2D polar coordinate

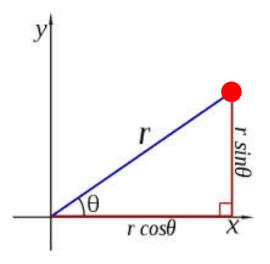


#### **Polar Coordinates**

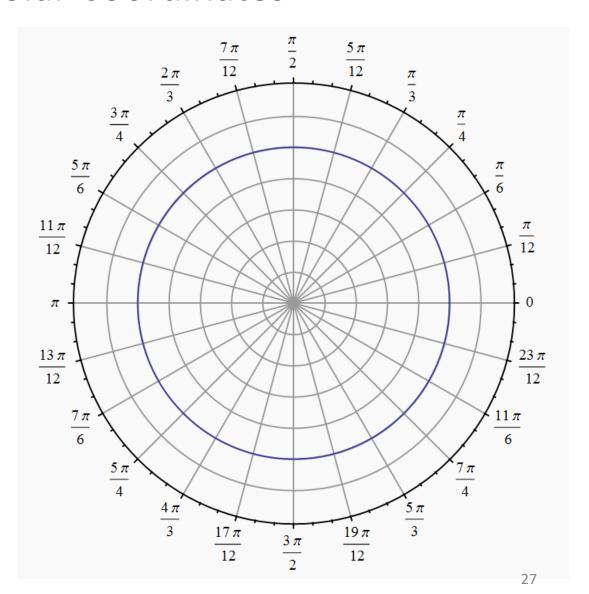




#### **Polar Coordinates**

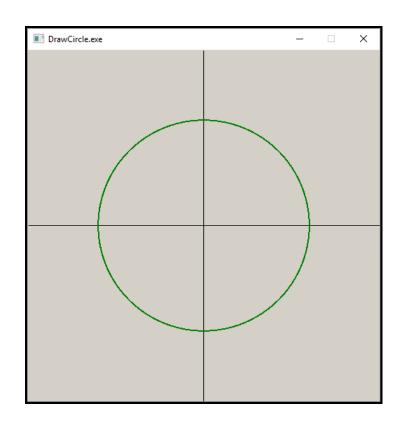


Angles are measured in radians  $(0 \le \theta \le 2\pi)$ 



# Open Lab 3 – Draw Circle

```
void draw(SimpleScreen& ss) {
    ss.DrawAxes();
    double radius{ 3 };
    int intervals{ 97 };
    double deltaTheta{ 2.0 * M PI / intervals };
    PointSet psCircle;
    for (int i{}; i < intervals; ++i) {</pre>
        double theta = deltaTheta * i:
        double x = radius * cos(theta);
        double y = radius * sin(theta);
        psCircle.add(x, y);
    ss.DrawLines(&psCircle, "green", 2);
int main()
   SimpleScreen ss(draw);
    ss.SetWorldRect(-5, -5, 5, 5);
   ss.HandleEvents();
    return 0;
```



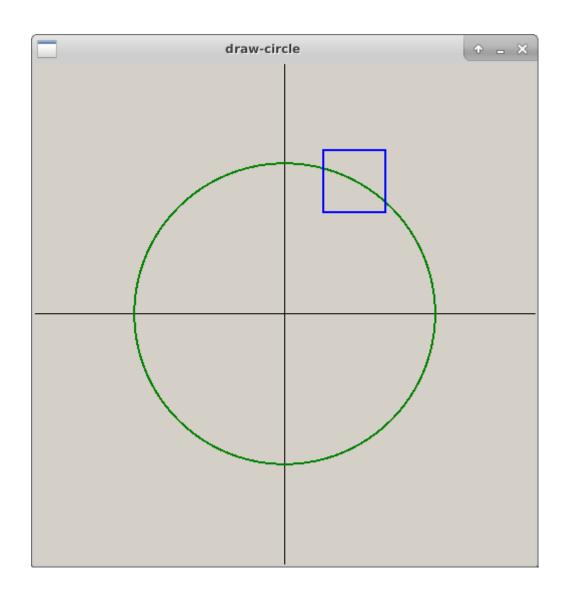
draw() is a "callback function"

It is your custom drawing

code that is called by the

SimpleScreen object

#### Run Lab 3 – Draw Circle



By using the callback pattern, the framework can call your custom **draw()** function whenever it needs to repaint the screen. This enables features like **zooming** 

You can left click and drag on the canvas to outline a zoom frame. When you release the left mouse button it will set the new world rectangle to the coordinates of the zoom frame and redraw the image

A **single right click** will restore each of the prior zoom levels

#### Edit Lab 3 – Draw Circle

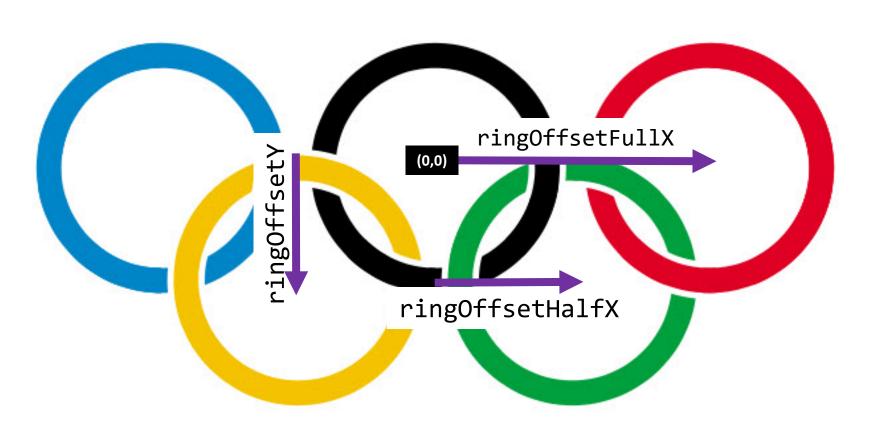
- First, change intervals to 8, run the app, then leave it at 8 for the next steps what shape do you see?
- Then change call to ss.DrawLines() as follows, and run the app each time after making these individual changes:

```
ss.DrawLines(psCircle, "blue", 2, false);
ss.DrawLines(psCircle, "red", 2, true, true);
```

```
void DrawLines(PointSet* ps, string clr, float width = 1,
bool close = true, bool fill = false, long delay = 0);
```

## Creating a New **Primitive**

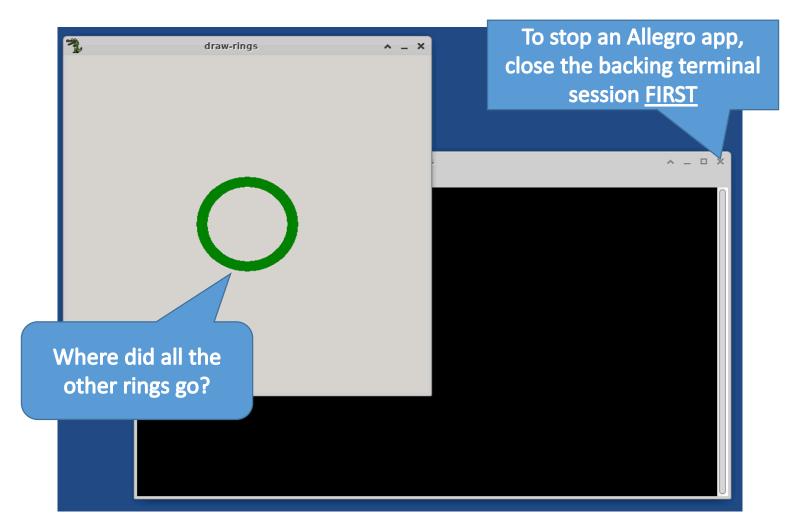
# Drawing the Olympic Rings



### Open Lab 4 – Draw the Olympic Rings

```
void draw(SimpleScreen& ss)
   double radius{ 5 };
    int width{ 15 };
   // You must determine proper offsets
   double ringOffsetFullX{};
   double ringOffsetHalfX{};
   double ringOffsetY{};
   ss.DrawCircle(0, 0, radius, "black", width);
   ss.DrawCircle(-ringOffsetFullX, 0, radius, "blue", width);
   ss.DrawCircle(ringOffsetFullX, 0, radius, "red", width);
   ss.DrawCircle(-ringOffsetHalfX, ringOffsetY, radius, "yellow", width);
   ss.DrawCircle(ringOffsetHalfX, ringOffsetY, radius, "green", width);
int main()
   SimpleScreen ss(draw);
   ss.SetWorldRect(-20, -20, 20, 20);
    ss.HandleEvents();
    return 0;
```

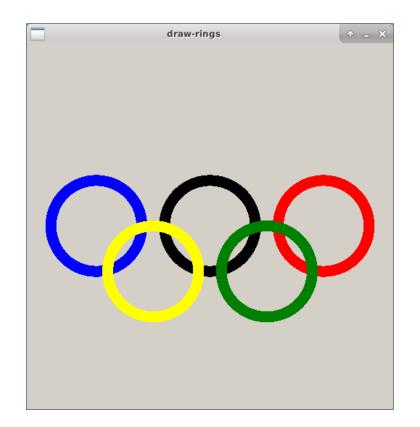
# Run Lab 4 – Draw the Olympic Rings



#### **Edit** Lab 4 – Draw the Olympic Rings

```
void draw(SimpleScreen& ss)
   double radius{ 5 };
    int width{ 15 };
    // You must determine proper offsets
   double ringOffsetFullX{};
   double ringOffsetHalfX{};
    double ringOffsetY{};
    ss.DrawCircle(0, 0, radius, "black", width);
    ss.DrawCircle(-ringOffsetFullX, 0, radius, "blue", width);
    ss.DrawCircle(ringOffsetFullX, 0, radius, "red", width);
    ss.DrawCircle(-ringOffsetHalfX, -ringOffsetY, radius, "yellow", width);
    ss.DrawCircle(ringOffsetHalfX, -ringOffsetY, radius, "green", width);
int main()
   SimpleScreen ss(draw);
    ss.SetWorldRect(-20, -20, 20, 20);
    ss.HandleEvents():
    return 0;
```

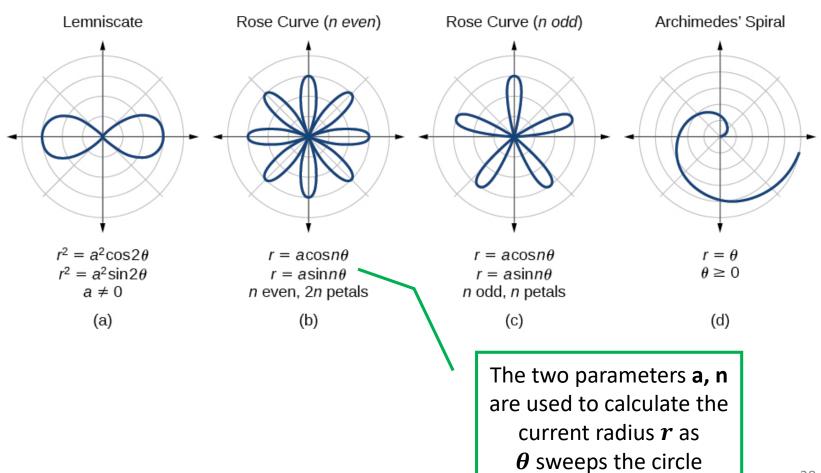
# Check Lab 4 – Draw the Olympic Rings



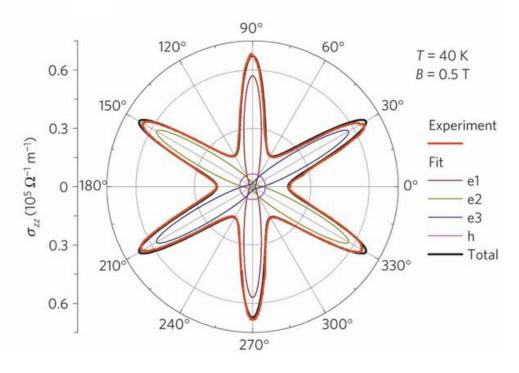


```
// You must determine proper offsets
double ringOffsetFullX{radius * 5. / 2};
double ringOffsetHalfX{radius * 5. / 4};
double ringOffsetY{-radius};
```



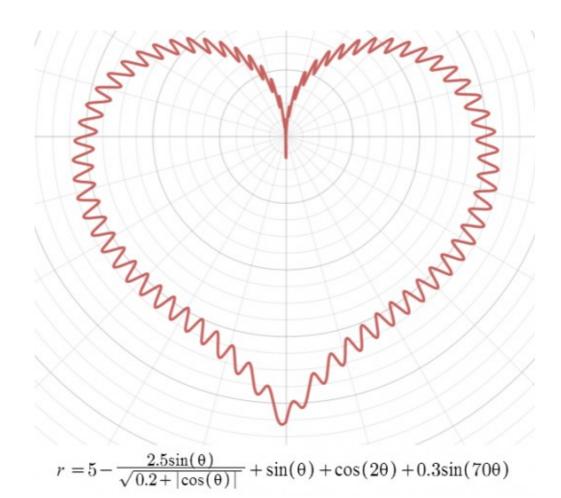


#### Field Induced Polarization of Dirac Valleys in Bismuth\*



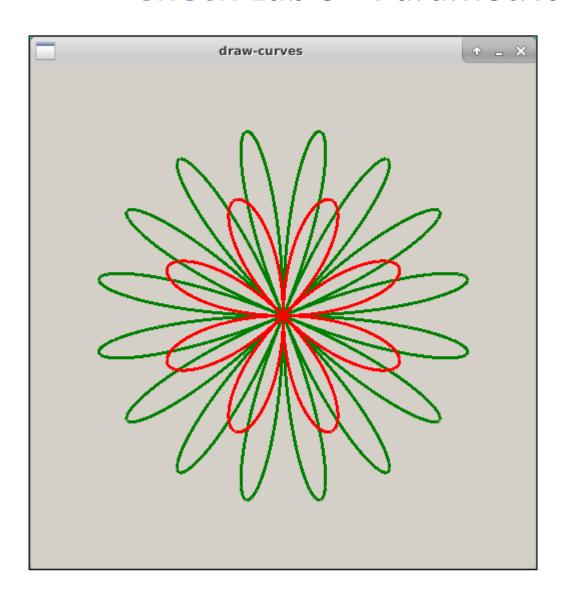
$$r = \sin^2\left(\frac{6}{5}\right) + \cos^2\left(\frac{6}{1}\right)$$

<sup>\*</sup>Bismuth is the element with the highest atomic mass that is stable



```
void CalcPolarCurve(PointSet& ps,
    double loops, double radius)
    int intervals( 997 );
                                          These two parameters
                                           are used to calculate
    double deltaTheta{ 2/0 * M_PI / i
                                          the current radius r as
                                            \boldsymbol{\theta} sweeps the circle
    for (int i{}; i <= intervals; i++</pre>
         double theta{/ i * deltaTheta };
         double r{ radius * sin(loops *
                                           theta)
         double x{ r * cos(theta)
         Open and run Lab 5
```

#### **Check** Lab 5 - Parametric Curves



#### The key points are:

- The radius is changing while  $\theta$  is changing
- The shape of the curve depends on two parameters

#### Now you know...

- Allegro is a free, open source, cross platform library for rendering 2D graphics
- A "bounding rectangle" is used to scale world (virtual) coordinates to screen (physical) coordinates
- How to create and populate elements of a PointSet
- How to "connect the dots" using SimpleScreen.DrawLines()
- How to use polar coordinates to draw 2D circles
- We approximate circles by drawing small intervals
- We can draw fancy curves by using parametric equations