## **Scientific Computing**

## Mean, Variance, and Standard Deviation Worksheet

Assume set X contains these numbers: {3, 9, 0, 2, 17, 8}

Question 1: How many elements are in set X?

$$n = 6$$

Question 2: What is the mean  $(\mu)$  of set X?

$$\mu = \frac{1}{n} \sum_{i=1}^{n} x_i$$

$$\mu = \frac{(3+9+0+2+17+8)}{6} = \frac{39}{6} = 6.5$$

Question 3: What is the <u>variance</u> ( $\sigma^2$ ) of set X?

$$\sigma^2 = \frac{1}{n} \sum_{i=1}^{n} (x_i - \mu)^2$$

$$\sigma^2 = \frac{(3 - 6.5)^2 + (9 - 6.5)^2 + (0 - 6.5)^2 + (2 - 6.5)^2 + (17 - 6.5)^2 + (8 - 6.5)^2}{6}$$

$$\sigma^2 = \frac{12.25 + 6.25 + 42.25 + 20.25 + 110.25 + 2.25}{6} = \frac{193.5}{6} = \mathbf{32.25}$$

Question 4: What is the standard deviation ( $\sigma$ ) of set X?

$$\sigma = \sqrt{\sigma^2}$$

$$\sigma = \sqrt{32.25} = 5.678908$$