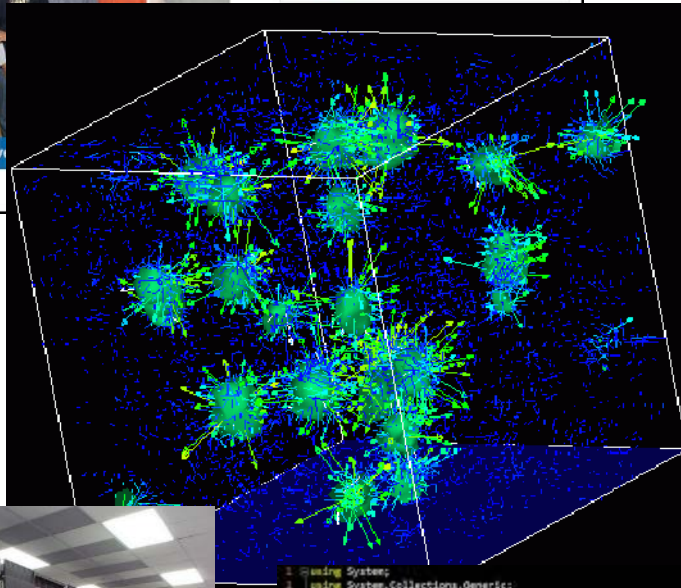




# Survey of Scientific Computing (SciComp 301)

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```
1 using System;
2 using System.Collections.Generic;
3 using System.ComponentModel;
4 using System.Data;
5 using System.Drawing;
6 using System.Linq;
7 using System.Text;
8 using System.Windows.Forms;
9
10 namespace SimpleEvents
11 {
12     public partial class Form1 : Form
13     {
14         Person person = new Person();
15
16         public Form1()
17         {
18             InitializeComponent();
19             person.FirstName = "Christian";
20             person.LastName = "Pano";
21         }
22
23         private void button1_Click(object sender, EventArgs e)
24         {
25             person.MainColor = textBox1.Text;
26         }
27     }
28 }
```

**Session 14**  
Cryptanalysis,  
Anagrams

# Session Goals

- Manage a C++ **string** as a **vector<char>**
  - Understand **ASCII** as an encoding mechanism
  - Read an ASCII **text file** stored on disk into a memory buffer
  - Generate a **histogram of character frequencies** within a file
- Encrypt and decrypt files using “**Caesar Shift**”
  - Perform **bigram analysis** on unreadable cipher text to determine the author’s native language
- Generate and discover simple and compound **anagrams**
  - Avoid combinatorial (exponential) explosion in search space

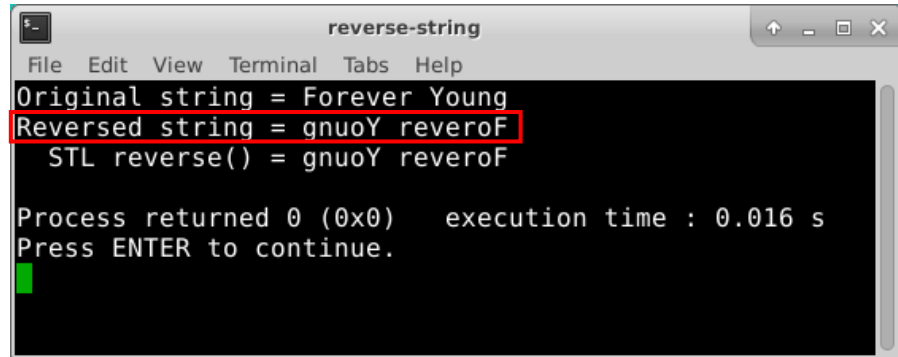
# C++ strings

- A C++ string is mostly equivalent to a **vector<char>**
  - A C++ **char** data type holds one “character”
  - There is a difference between the length of a string (the number of characters in the string) and the number of bytes required to store it in memory or on disk
  - The memory size (number of bits) of a character can vary by platform (Windows vs. Linux)
- A string has **.size()** or **.length()** methods to get the number of *characters* in the string
- We can access individual characters using the **.at()** method

# Reverse a String

i	s.at()
0	F
1	o
2	r
3	e
4	v
5	e
6	r
7	<i>(space)</i>
8	Y
9	o
10	u
11	n
12	g

**s.length()==13**



```
reverse-string
File Edit View Terminal Tabs Help
Original string = Forever Young
Reversed string = gnuoY reveroF
STL reverse() = gnuoY reveroF

Process returned 0 (0x0)    execution time : 0.016 s
Press ENTER to continue.
```

# Open Lab 1

## Reverse String

```
reverse-string.cpp ✕
1 // reverse-string.cpp
2
3 #include "stdafx.h"
4
5 using namespace std;
6
7 string ReverseString(string a)
8 {
9     string b;
10
11     [ ]
12
13
14     return b;
15 }
16
17 int main()
18 {
19     string s = "Forever Young";
20     string r = ReverseString(s);
21
22     cout << "Original string = "
23          << s << endl;
24
25     cout << "Reversed string = "
26          << r << endl;
27
28     reverse(s.begin(), s.end());
29
30     cout << " STL reverse() = "
31          << s << endl;
32
33     return 0;
34 }
35
```

Walk backwards through the given string **a**, while dynamically building string **b** one character at a time

# Edit Lab 1 – Reverse String

- Add code only to the **ReverseString()** function – don't modify any code in **main()**
  - A **string** is an vector – you can access individual elements (characters) using the **.at()** method
  - Use **.length()** to get the number of characters in the string
  - You can concatenate strings with the **+** operator
- On return, **b** should be the string **a** in reverse char order

```
7  string ReverseString(string a)
8  {
9      string b;
10
11      // Implement your algorithm here
12
13      return b;
14 }
```



## Edit Lab 1 – Reverse String

- Add code only to the **ReverseString()** function – don't modify any code in **main()**
  - A **string** is an vector – you can access individual elements (characters) using the **.at()** method
  - Use **.length()** to get the number of characters in the string
  - You can concatenate strings with the **+** operator
- On return, b should be the string a in reverse char order

```
7  string ReverseString(string a)
8  {
9      string b;
10
11     for(int i = a.length() - 1; i >= 0; --i)
12         b += a.at(i);
13
14     return b;
15 }
```

# Edit Lab 1

## Reverse String

```
reverse-string.cpp ✕
1 // reverse-string.cpp
2
3 #include "stdafx.h"
4
5 using namespace std;
6
7 string ReverseString(string a)
8 {
9     string b;
10
11     for(int i = a.length() - 1; i >= 0; --i)
12         b += a.at(i);
13
14     return b;
15 }
16
17 int main()
18 {
19     string s = "Forever Young";
20     string r = ReverseString(s);
21
22     cout << "Original string = "
23           << s << endl;
24
25     cout << "Reversed string = "
26           << r << endl;
27
28     reverse(s.begin(), s.end());
29
30     cout << " STL reverse() = "
31           << s << endl;
32
33     return 0;
34 }
35
```

Walk backwards through the given string a, while dynamically building string b one character at a time

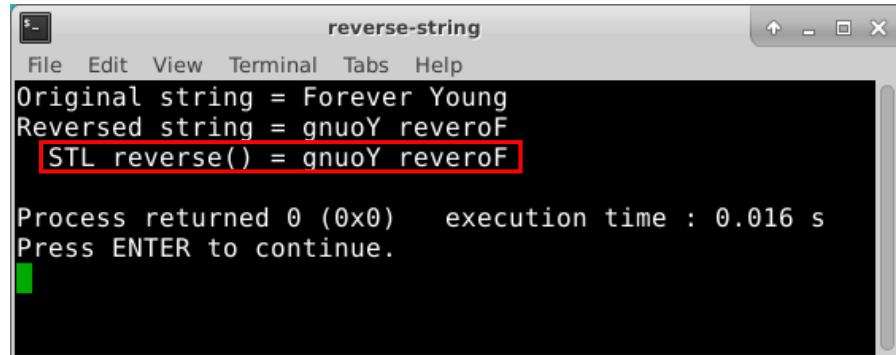
The C++ Standard Template Library (**STL**) has a built-in function to reverse the order of the elements in any vector



# Run Lab 1 – Reverse String

i	s.at()
0	F
1	o
2	r
3	e
4	v
5	e
6	r
7	(space)
8	Y
9	o
10	u
11	n
12	g

**s.length()==13**



```
reverse-string
File Edit View Terminal Tabs Help
Original string = Forever Young
Reversed string = gnuoY reveroF
STL reverse() = gnuoY reveroF
Process returned 0 (0x0)   execution time : 0.016 s
Press ENTER to continue.
```

**STL** = Standard Template Library

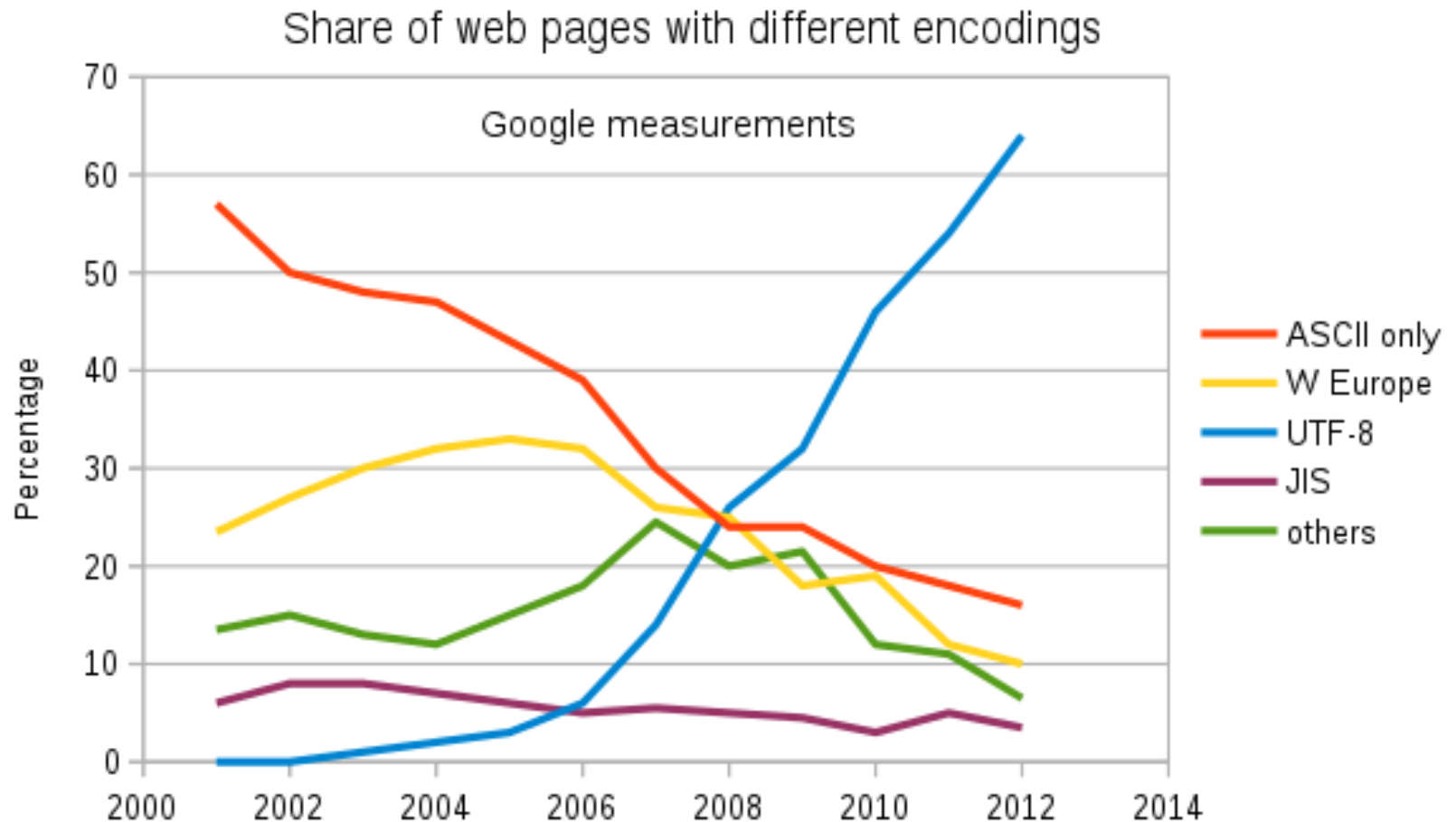
The STL is a set of free & open-source functions and classes to *reduce* the amount of code C++ programmers must write to solve common problems

# ASCII (“as-key”)

- **A**merican **S**tandard **C**ode for **I**nformation **I**nterchange
  - ASCII was the most common legacy International standard used across the Internet until 2007
  - Since 2008 ASCII has been surpassed by **UTF-8** (Universal Transformation Format), which includes ASCII as a subset
- ASCII is an 8-bit (**one byte**) character encoding scheme
  - ASCII maps most of the characters in the (Western) languages descending from Latin to a specific integer value
  - There is a 1:1 correspondence between a letter and a number. In ASCII, every character is **always** one byte long (in UTF-8 it is variable)
  - Inside a computer, **all** letters, punctuation marks, even numbers (when treated as strings) are encoded as either ASCII or UTF

# Learn about **UTF-8**

<https://en.wikipedia.org/wiki/UTF-8>



# ASCII range for common English characters

Dec	Char
32	(space)
33	!
34	"
35	#
36	\$
37	%
38	&
39	'
40	(
41	)
42	*
43	+
44	,
45	-
46	.
47	/
48	0
49	1
50	2

Dec	Char
51	3
52	4
53	5
54	6
55	7
56	8
57	9
58	:
59	;
60	<
61	=
62	>
63	?
64	@
65	A
66	B
67	C
68	D
69	E

Dec	Char
70	F
71	G
72	H
73	I
74	J
75	K
76	L
77	M
78	N
79	O
80	P
81	Q
82	R
83	S
84	T
85	U
86	V
87	W
88	X

Dec	Char
89	Y
90	Z
91	[
92	\
93	]
94	^
95	_
96	`
97	a
98	b
99	c
100	d
101	e
102	f
103	g
104	h
105	i
106	j
107	k

Dec	Char
108	l
109	m
110	n
111	o
112	p
113	q
114	r
115	s
116	t
117	u
118	v
119	w
120	x
121	y
122	z
123	{
124	
125	}
126	~

# ASCII Text Files – A “stream”

- A file on disk is essentially just a big **byte array**
  - A **byte** is an 8-bit *unsigned integer* between 0 and 255 (**uint8\_t**)
  - We can declare a byte array and load it with the contents of a file
  - A **stream** of file bytes in memory is called a **buffer**

```
ifstream ifs("Encrypted.txt", ios::binary | ios::ate);
ifstream::pos_type pos = ifs.tellg();
vector<uint8_t> fileBytes(pos);
ifs.seekg(0, ios::beg);
ifs.read((char*)(fileBytes.data()), pos);
```

- We can then access any individual character within the disk file by using the normal **.at() method** on the vector **fileBytes** and specifying an **index value**

# Creating a Frequency Histogram








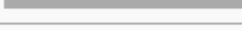





- Consider Lincoln's Gettysburg Address:

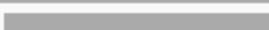












Four score and seven years ago our fathers brought forth on this continent a new nation, conceived in liberty, and dedicated to the proposition that all men are created equal.

Now we are engaged in a great civil war, testing whether that nation, or any nation so conceived and so dedicated, can long endure...

- We want to perform a **histogram analysis** of Lincoln's speech
  - What **letter** do you think occurs most frequently in **English**?
  - Spaces (**ASCII value 32**) usually occur most often because we use spaces as a word breaker

# Letter Frequencies in the English Language

Letter ↕	Relative frequency in the English language ↕	
a	8.167%	
b	1.492%	
c	2.782%	
d	4.253%	
e	12.702%	
f	2.228%	
g	2.015%	
h	6.094%	
i	6.966%	
j	0.153%	
k	0.772%	
l	4.025%	
m	2.406%	

Letter ↕	Relative frequency in the English language ↕	
n	6.749%	
o	7.507%	
p	1.929%	
q	0.095%	
r	5.987%	
s	6.327%	
t	9.056%	
u	2.758%	
v	0.978%	
w	2.361%	
x	0.150%	
y	1.974%	
z	0.074%	

```

int main()
{
    // Open file at the end so the "get" position will be file size
    ifstream ifs("The Gettysburg Address.txt", ios::binary | ios::ate);
    ifstream::pos_type pos = ifs.tellg();

    // Allocate a vector big enough to hold all the file bytes
    vector<uint8_t> fileBytes(pos);

    // Read in the file from the beginning straight into the vector
    ifs.seekg(0, ios::beg);
    ifs.read((char*)(fileBytes.data()), pos);

    // Create a new CERN ROOT app
    string title = "Frequency Analysis";
    TApplication* theApp = new TApplication(title.c_str(), nullptr, nullptr);

    TCanvas* c1 = new TCanvas(title.c_str());
    c1->SetTitle(title.c_str());

    // Create a ROOT one dimensional histogram of integers
    TH1I* h1 = new TH1I(nullptr, title.c_str(), 256, 0, 257);
    h1->SetStats(kFALSE);

    TAxis* ya = h1->GetYaxis();
    ya->SetTitle("Count");
    ya->CenterTitle();

    TAxis* xa = h1->GetXaxis();
    xa->SetTitle("ASCII Value");
    xa->CenterTitle();
    xa->SetTickSize(0);
}

```

## Open Lab 2

# Frequency Histogram



## View Lab 2 Frequency Histogram

```
// Fill the histogram using the bytes in the file
for (auto item : fileBytes)
    h1->Fill((int)item);

// Label any bin with the ASCII value
// if the bin count is > 6% of the file size,
// as these would be noteworthy occurrences
for (int i{}; i < xa->GetNbins();++i)
    if (h1->GetBinContent(i) > fileBytes.size() * 0.06)
        xa->SetBinLabel(i, to_string(i).c_str());

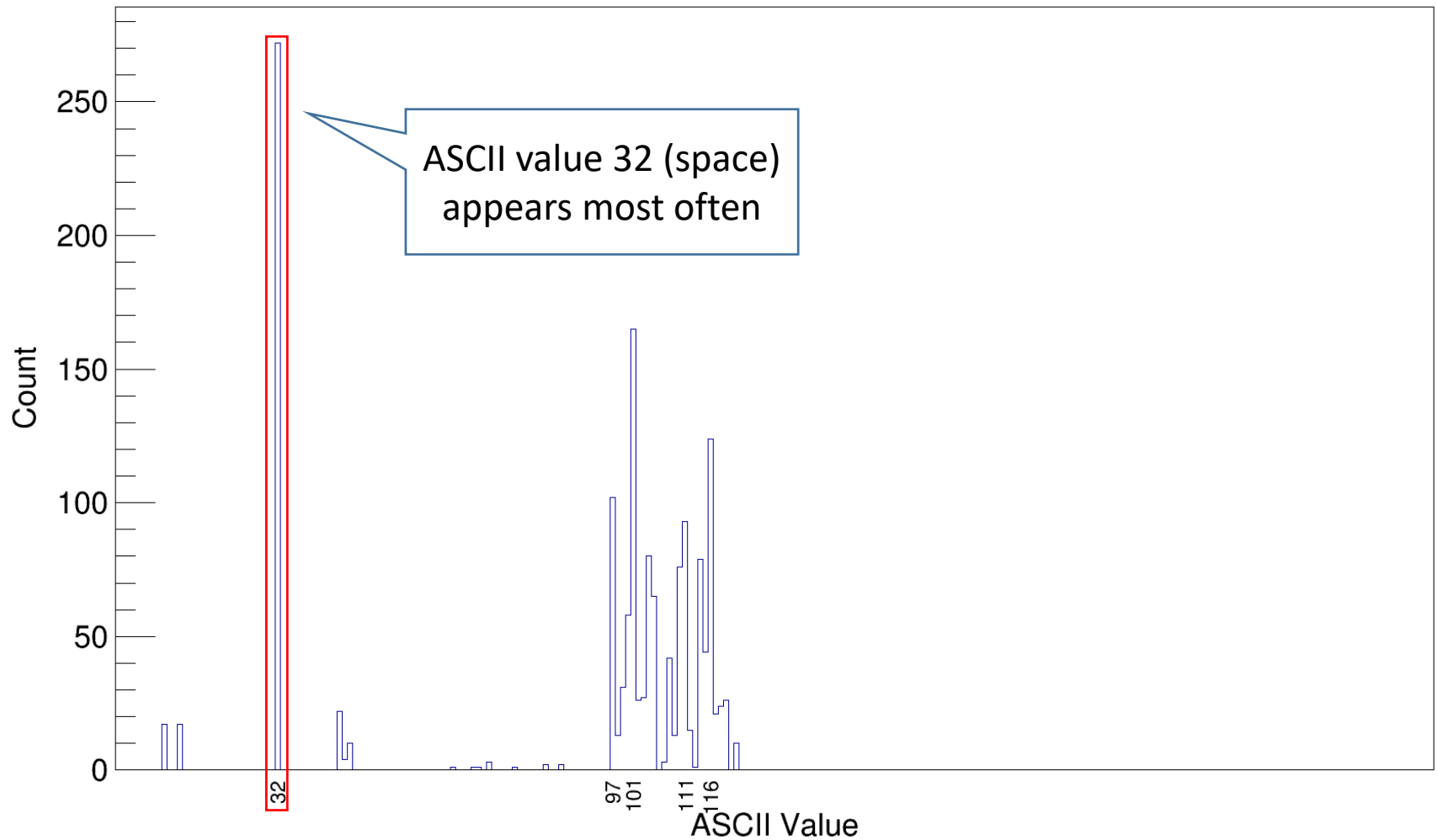
h1->Draw();

theApp->Run();
return 0;
}
```

**Run Lab 2**

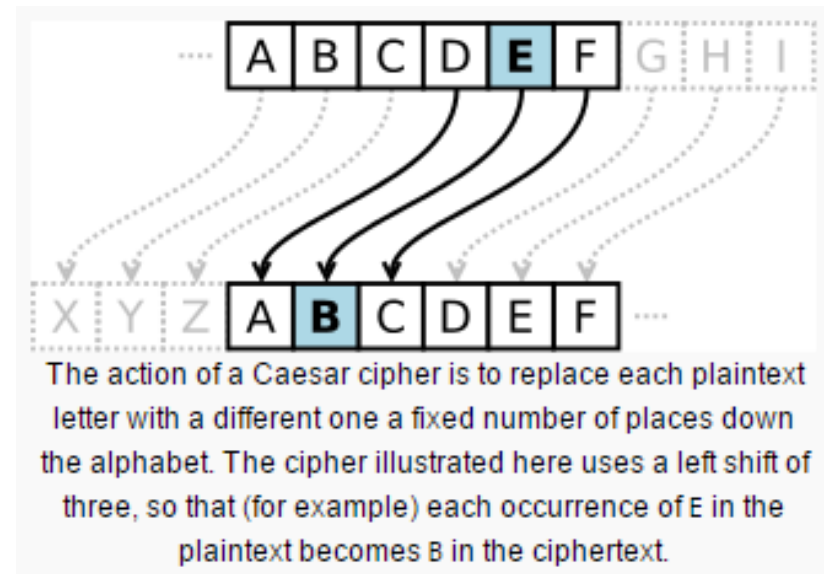
# Histogram of Lincoln's Gettysburg Address

## Frequency Analysis

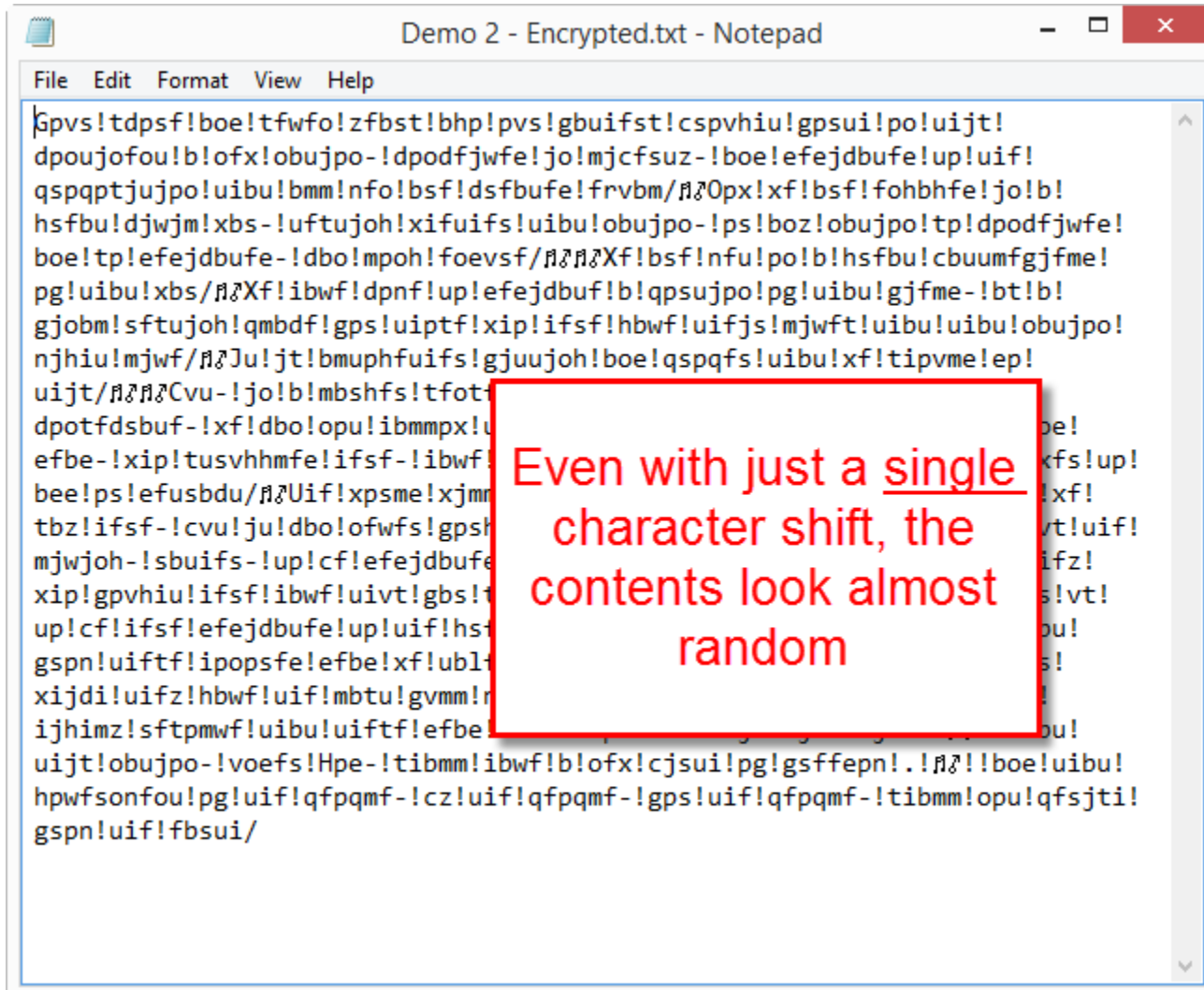


# The Caesar Shift Cipher

- Roman Emperor **Julius Caesar** used a simple (but effective for its time) encryption scheme for his private correspondence
- To create “**cipher text**” from “**plain text**” simply shift the original letters **forward** (*or backward*) a given number of letters in the alphabet
- To decrypt the message, simply **reverse the sign of the shift**



# The Caesar Shift Cipher



Demo 2 - Encrypted.txt - Notepad

File Edit Format View Help

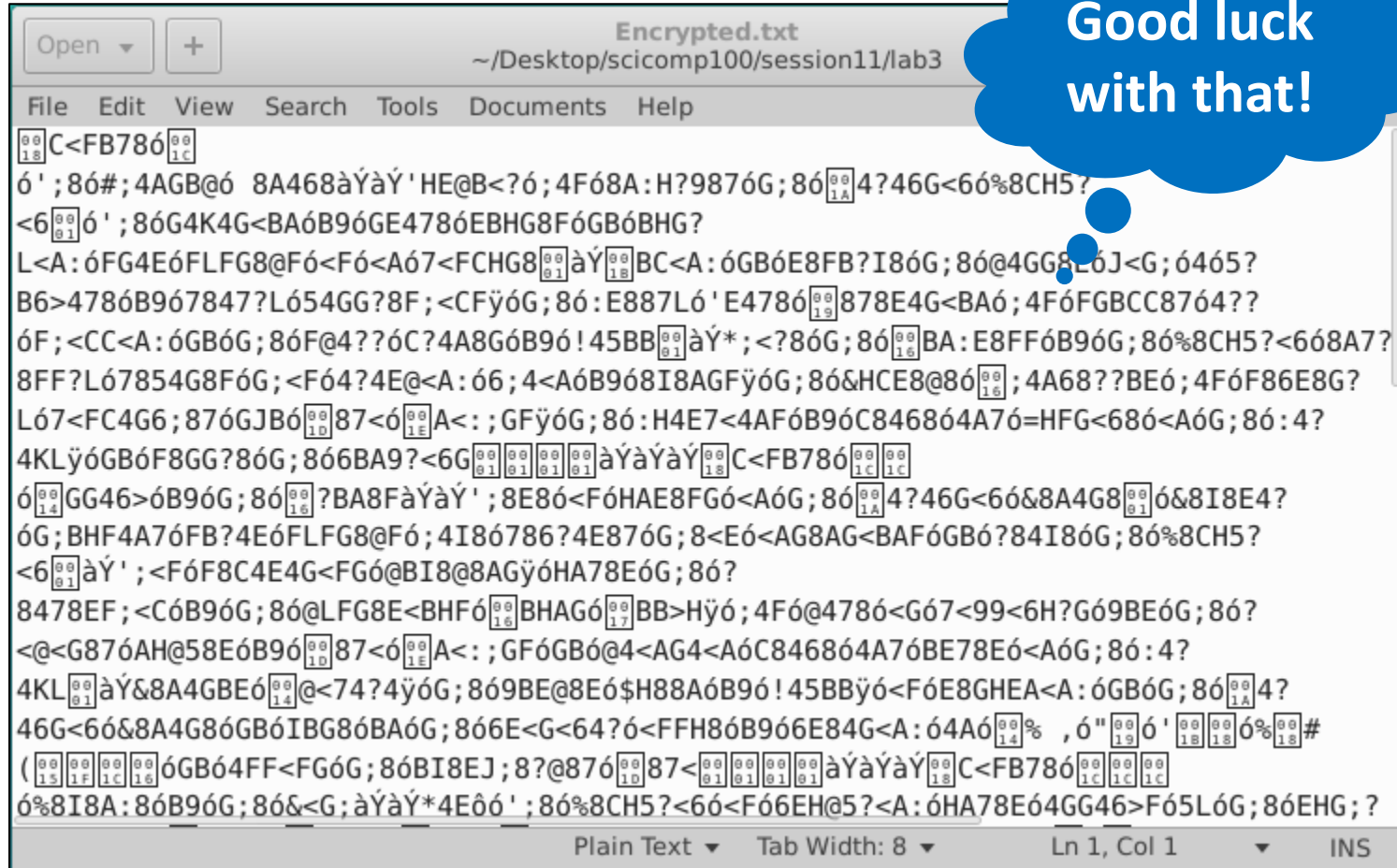
Spvs!tdpsf!boe!tfwfo!zfbst!bhp!pvs!gbuifst!cspvhiu!gpsui!po!uijt!  
dpoujofou!b!ofx!obujpo-!dpodfjwfe!jo!mjcfsuz-!boe!efejdbufe!up!uif!  
qspqptjujpo!uibu!bmm!nfo!bsf!dsfbufe!frvbm/!Xf!bsf!fohbhfe!jo!b!  
hsfbu!djwjm!xbs-!uftujoh!xifuijs!uibu!obujpo-!ps!boz!obujpo!tp!dpodfjwfe!  
boe!tp!efejdbufe-!dbo!mpoh!foevsf/!Xf!bsf!nfu!po!b!hsfbu!cbuumfgjme!  
pg!uibu!xbs/!Xf!ibwf!dpnf!up!efejdbuf!b!qpsujpo!pg!uibu!gjme-!bt!b!  
gjobm!sftujoh!qmbdf!gps!uiptf!xip!ifsf!hbwf!uifjs!mjwft!uibu!uibu!obujpo!  
njhiu!mjwf/!Ju!jt!bmuphfuijs!gjuujoh!boe!qspqfs!uibu!xf!tipvme!ep!  
uijt/!Cvu-!jo!b!mbshfs!tfot  
dpotfdsbuf-!xf!dbo!opu!ibmmpx!  
efbe-!xip!tusvhhmfe!ifsf-!ibwf  
bee!ps!efusbdu/!Uif!xpsme!xjmm  
tbz!ifsf-!cvu!ju!dbo!ofwfs!gps  
mjwjoh-!sbuifs-!up!cf!efejdbufe  
xip!gpvhiu!ifsf!ibwf!uivt!gbs!  
up!cf!ifsf!efejdbufe!up!uif!hs  
gspn!uiftf!ipopsfe!efbe!xf!ublt  
xijdi!uifz!hbwf!uif!mbtu!gvmm!  
ijhimz!sftpmwf!uibu!uiftf!efbe  
uijt!obujpo-!voefs!Hpe-!tibmm!ibwf!b!ofx!cjsui!pg!gsffepn!.!boe!uibu!  
hpwfonfou!pg!uif!qfpqmf-!cz!uif!qfpqmf-!gps!uif!qfpqmf-!tibmm!opu!qfsjti!  
gspn!uif!fbsui/

Even with just a single character shift, the contents look almost random

# The Caesar Shift Cipher

- The question becomes, if we are given a “Caesar Shift” encrypted file, which we believe was written in **English**, how can we figure out **what shift** was used?
- We could use “**brute force**” and try every possible value to see what shift produces legible prose
  - **We only need to try shifts between 1 and 255 – why?**
    - But it would still take a long time to sift through potentially 255 distinct files all filled with *gibberish* in order to break the cipher
- Can we glean any insight from analyzing the **character histogram** of the encrypted file?

# Open Lab 3 – Ciphertext.txt



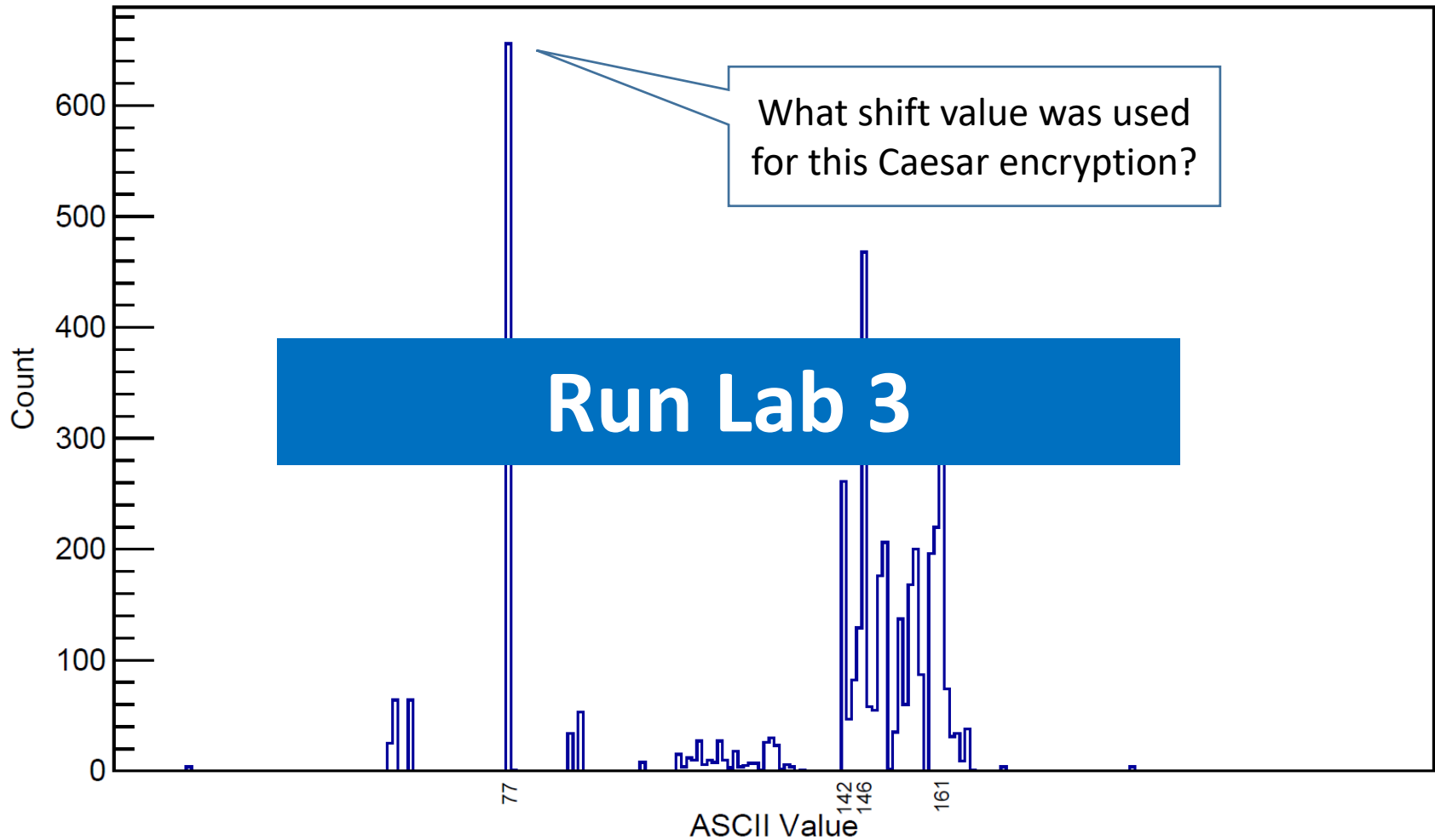
The screenshot shows a text editor window titled "Encrypted.txt" with the path "~/Desktop/scicomp100/session11/lab3". The editor contains a large block of text that has been encrypted using a Caesar cipher with a shift of 18. The text is displayed with each character followed by its hexadecimal ASCII value in a small box. A blue callout bubble with the text "Good luck with that!" points to the encrypted content. The status bar at the bottom indicates "Plain Text", "Tab Width: 8", "Ln 1, Col 1", and "INS".

```
Open ▾ +  
~/Desktop/scicomp100/session11/lab3  
File Edit View Search Tools Documents Help  
C<FB78ó  
ó';8ó#;4AGB@ó 8A468àÝàÝ'HE@B<?ó;4Fó8A:H?987óG;8ó4?46G<6ó%8CH5?  
<6ó';8óG4K4G<BAóB9óGE478óEBHG8FóGBóBHG?  
L<A:óFG4EóFLFG8@Fó<Fó<Aó7<FCHG8àÝBC<A:óGBóE8FB?I8óG;8ó@4GG8óJ<G;ó4ó5?  
B6>478óB9ó7847?Ló54GG?8F;<CFÿóG;8ó:E887Ló'E478ó878E4G<BAó;4FóFGBCC87ó4??  
óF;<CC<A:óGBóG;8óF@4??óC?4A8GóB9ó!45BBàÝ*;<?8óG;8óBA:E8FFóB9óG;8ó%8CH5?<6ó8A7?  
8FF?Ló7854G8FóG;<Fó4?4E@<A:ó6;4<AóB9ó8I8AGFÿóG;8ó&HCE8@8ó;4A68??BEó;4FóF86E8G?  
Ló7<FC4G6;87óGJBó87<óA<;GFÿóG;8ó:H4E7<4AFóB9óC8468ó4A7ó=HFG<68ó<AóG;8ó:4?  
4KLÿóGBóF8GG?8óG;8ó6BA9?<6GàÝàÝàÝC<FB78ó  
óGG46>óB9óG;8ó?BA8FàÝàÝ';8E8ó<FóHAE8FGó<AóG;8ó4?46G<6ó&8A4G8ó&8I8E4?  
óG;BHF4A7óFB?4EóFLFG8@Fó;4I8ó786?4E87óG;8<Eó<AG8AG<BAFóGBó?84I8óG;8ó%8CH5?  
<6àÝ';<FóF8C4E4G<FGó@BI8@8AGÿóHA78EóG;8ó?  
8478EF;<CóB9óG;8ó@LFG8E<BHFóBHAGóBB>Hÿó;4Fó@478ó<Gó7<99<6H?Gó9BEóG;8ó?  
<@<G87óAH@58EóB9ó87<óA<;GFóGBó@4<AG4<AóC8468ó4A7óBE78Eó<AóG;8ó:4?  
4KLàÝ&8A4GBEó@<74?4ÿóG;8ó9BE@8Eó$H88AóB9ó!45BBÿó<FóE8GHEA<A:óGBóG;8ó4?  
46G<6ó&8A4G8óGBóIBG8óBAóG;8ó6E<G<64?ó<FFH8óB9ó6E84G<A:ó4Aó% ,ó'ó'ó'ó'#  
(óGBó4FF<FGóG;8óBI8EJ;8?@87ó87<àÝàÝàÝC<FB78ó  
ó%8I8A:8óB9óG;8ó&<G;àÝàÝ*4Eóó';8ó%8CH5?<6ó<Fó6EH@5?<A:óHA78Eó4GG46>Fó5LóG;8óEHG;?
```

Plain Text ▾ Tab Width: 8 ▾ Ln 1, Col 1 ▾ INS

# Run Lab 3 – Histogram of Ciphertext

## Frequency Analysis



## Open Lab 4 – Caesar Decrypt

- **Your mission is to decrypt the Lab 3 ciphertext file**
- What if the survival of your country depended upon your ability to crack the encryption?



# Edit Lab 4 – Caesar Decrypt

```
caesar-decrypt.cpp ✕
1 // caesar-decrypt.cpp
2
3 #include "stdafx.h"
4
5 using namespace std;
6
7 int main()
8 {
9     ifstream ifs("Encrypted.txt", ios::binary | ios::ate);
10    ifstream::pos_type pos = ifs.tellg();
11
12    vector<uint8_t> fileBytes(pos);
13
14    ifs.seekg(0, ios::beg);
15    ifs.read((char*)(fileBytes.data()), pos);
16
17    int shift = 0;
18
19    for (auto b : fileBytes)
20        cout << (char)(b + shift);
21
22    cout << endl << endl;
23
24    return 0;
25 }
26
```

What shift value was used for the **Lab 3** Caesar encryption?

## Run Lab 4 – Caesar Decrypt

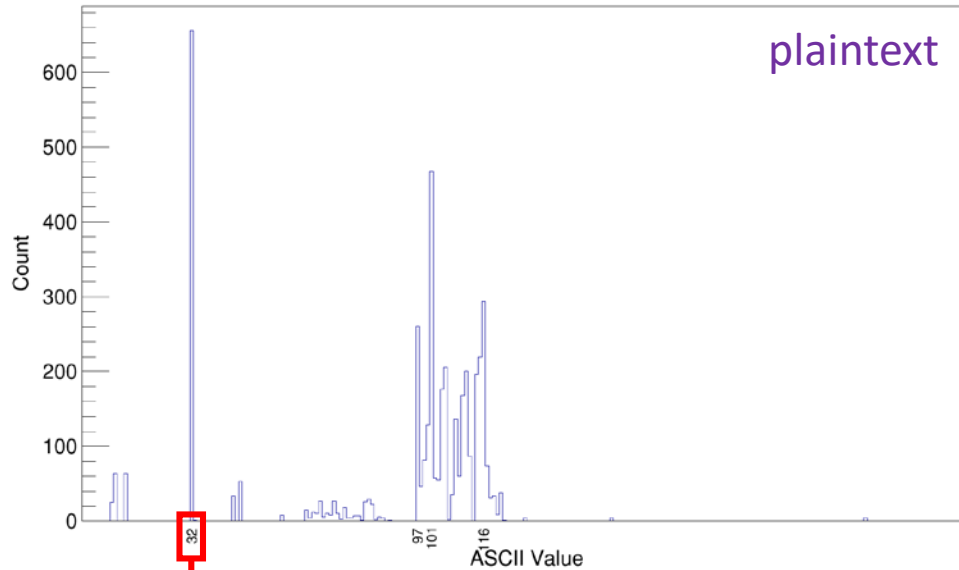
```

G;0G;8<E0I4?H45?80;BFG4:800GJB0087<009A<;GF0?84704078FC8E4G80@FF<BA0GB0E8F6H80G
0!8J0BC8000000G0<F040C8E<B70B906<I<?0J4E0%858?0FC468F;<CF00FGE<><A:09EB@040;<7
78A054F800;4I80JBA0G;8<E09<EFG0I<6GBEL04:4<AFG0G;808I<?09A?46G<600AC<E8000HE<A:
0G;8054GG?800E858?0FC<8F0@4A4:870GB0FG84?0F86E8G0C?4AF0GB0G;800AC<E80F0H?G<@4G80
J84CBA00G;8001111400&'003004A04E@BE870FC4680FG4G<BA0J<G;08ABH.;0CBJ8E0GB078FGEBL04A
08AG<E80C?4A8G000#HEFH8705L0G;800AC<E80F0F<A<FG8E04:8AGF00#E<A68FF0003<40E468F0;B
@8045B4E70;8E0FG4EF;<C006HFGB7<4A0B90G;80FGB?8A0C?4AF0G;4G064A0F4I80;8E0C8BC?804
0';800AC<E80&GE<>8F0096>000000G0<F04074E>0G<@809BE0G;80%858??<BA00014G;BH.;0G;80018
4G;0&G4E0;4F0588A078FGEBL870000C8E<4?0GEBBCF0;4I807E<I8A0G;80%858?09BE68F09EB@0G
;8<E0;<778A054F804A70CHEFH870G;8@046EBFF0G;80:4?4KL0000147<A:0G;807E8478700AC8E<
4?0&G4E9?88G0040:EBHC0B909E887B@09<;G8EF0?8705L00H>80&>LJ4?>8E0;4F08FG45?<F;870
40A8J0F86E8G054F80BA0G;80E8@BG80<680JBE?70B90BG;000';808I<?0?BE700EG;(0)478E00B5
F8FF870J<G;09<A7<A:0LBHA:0&>LJ4?>8E00;4F07<FC4G6;870G;BHF4A7F0B90E8@BG80CEB58F0<
0%8GHEA0B90G;80087<000000H>80&>LJ4?>8E0;4F0E8GHEA870GB0;<F0;B@80C?4A8G0B90'4GBB<A
80<A04A04GG8@CG0GB0E8F6H80;<F09E<8A709AA0&B?B09EB@0G;806?HG6;8F0B90G;80I<?80:4A:F
G8E0005540G;8GG0000GG?807B8F00H>80>ABJ0G;4G0G;80011111160011100#00000;4F0F86E8G?L058
:HA06BAFGEH6G<BA0BA040A8J04E@BE870FC4680FG4G<BA08I8A0@BE80CBJ8E9H?0G;4A0G;809<EF
G07E847870034G;0&G4E000*;8A06B@C?8G8700G;<F0H?G<@4G80J84CBA0J<??0FC8??068EG4<A07
BB@09BE0G;80F@4??054A70B90E858?F0FGEH::?<A:0GB0E8FGBE809E887B@0GB0G;80:4?4KL001111

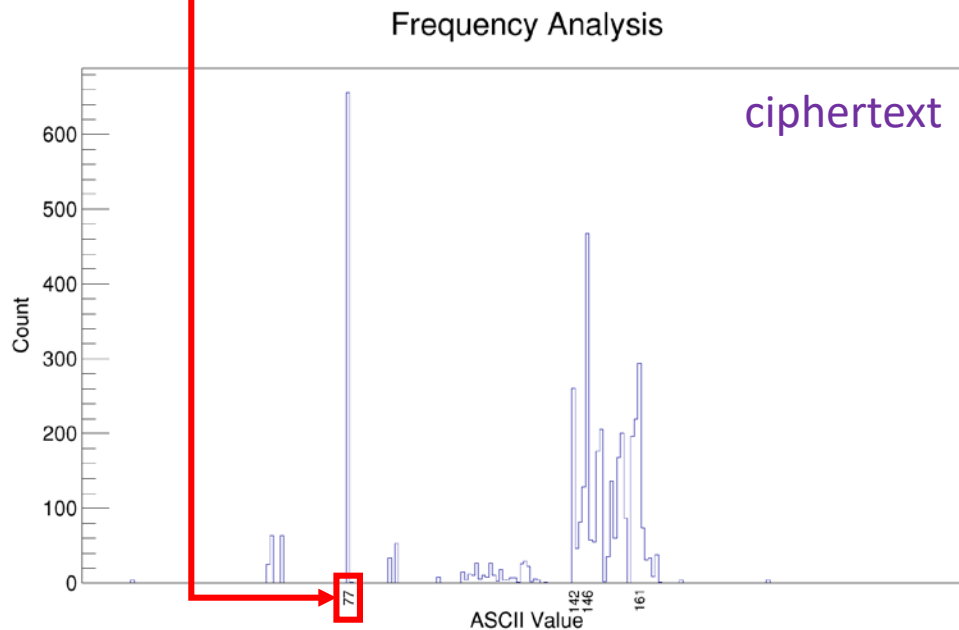
```

Process returned 0 (0x0)      execution time : 0.014 s  
Press ENTER to continue.

## Frequency Analysis



Notice the *relative* frequencies are the same before and after encryption



# The Caesar Shift Cipher

Because the **Caesar Shift** is a **monoalphabetic substitution cipher**, it is susceptible to **cryptanalysis** (breaking) by **frequency analysis**

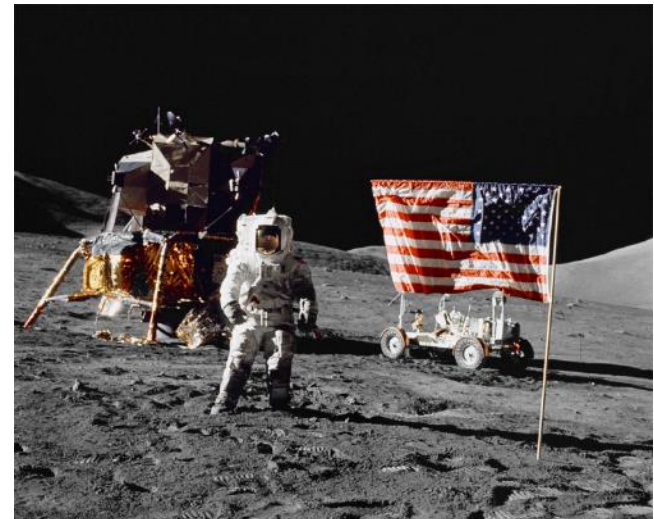


# Bigram Analysis

- Most Western (Latin influenced) languages have a unique fingerprint from their most frequent **bigrams** (two-letter pair)
  - In **English** the bigrams **TH** and **HE** occur most often, since “the” is the most frequent word in English
  - “The” also occurs very often in other languages, though each language spells it differently, and this helps establish the **distinct statistical profiles** of each language
- Linguists and statisticians have compiled lists of the most frequent **bigrams** *per* language
- We will analyze the bigrams in **President Kennedy’s Rice University Speech** - where he set the goal in 1962 for the USA to reach the moon before 1970!

# Kennedy's Moon Speech in 1962

“We choose to go to the moon in this decade and do the other things, not because they are easy, *but because they are hard*, because that goal will serve to organize and measure **the best of our energies and skills**, because that challenge is one that we are willing to accept, one we are unwilling to postpone, and one which we intend to win.”



# Bigram Analysis of Kennedy's Moon Speech (English)

```
freq-bigrams
File Edit View Terminal Tabs Help
Most recurring bigrams in file:
Kennedy Moon English.txt

ASCII      CHARS      FREQ
(65, 76)    AL         1.13
(65, 78)    AN         1.79
(65, 83)    AS         1.13
(65, 84)    AT         1.59
(69, 65)    EA         1.53
(69, 78)    EN         1.53
(69, 82)    ER         1.66
(69, 83)    ES         1.46
(69, 84)    ET         1.72
(72, 65)    HA         1.33
(72, 69)    HE         2.32
(73, 78)    IN         1.53
(76, 69)    LE         0.99
(76, 76)    LL         0.99
(78, 68)    ND         1.13
(78, 69)    NE         0.99
(78, 71)    NG         1.33
(78, 84)    NT         0.99
(79, 78)    ON         1.33
(82, 69)    RE         1.53
(83, 84)    ST         1.53
(84, 69)    TE         0.99
(84, 72)    TH         3.38
(84, 79)    TO         1.66

Process returned 0 (0x0)   execution time : 0.023 s
Press ENTER to continue.
```



# Kennedy's Moon Speech Translated

Nous choisissons d'aller sur la lune.  
Nous choisissons d'aller sur la lune  
dans cette décennie et de faire  
d'autres choses, non pas parce qu'ils  
sont faciles, mais parce qu'ils sont  
difficiles, parce que ce but servira à  
organiser et mesurer le meilleur de  
nos énergies et de compétences  
parce que ce défi est l'un  
sommes prêts à accepter,  
ne sommes pas disposés à  
et celui qui nous avons l'intention  
gagner.

Elegimos ir a la Luna. Elegimos ir a la  
Luna en esta década y hacer las  
otras cosas, no porque sean fáciles,  
sino porque son difíciles, porque esa  
meta servirá para organizar y medir  
lo mejor de nuestras energías y  
habilidades, porque ese desafío es  
una que estamos dispuestos a  
dispuestos  
hemos la

Wir wählen, um zum Mond zu fliegen. Wir  
wählen, um zum Mond in diesem  
Jahrzehnt zu gehen und die anderen  
Dinge, nicht weil sie leicht sind, sondern  
weil sie hart sind, denn das Ziel wird dazu  
dienen, zu organisieren und zu messen,  
das Beste aus unserer Energien und  
Fähigkeiten, denn das ist eine  
Herausforderung dass wir bereit sind zu  
akzeptieren, das wir nicht bereit sind, zu  
verschieben, und eine, die wir  
beabsichtigen, zu gewinnen.



# Bigram Statistics by Language

## Bigrams - Kennedy Speech

= Unique Indicators (for each language)  
 = Relative Indicator (see German)

English		Speech
TH	2.71	3.38
HE	2.33	2.32
IN	2.03	1.53
ER	1.78	1.66
AN	1.61	1.79
RE	1.41	
ES	1.32	
ON	1.32	
ST	1.25	
NT	1.17	
EN	1.13	
AT	1.12	

Top 5: 10.46 10.68

Spanish		Speech
DE	2.57	2.41
ES	2.31	2.84
EN	2.27	1.75
EL	2.01	1.57
LA	1.80	1.69
OS	1.79	
ON	1.61	
AS	1.56	
ER	1.52	
RA	1.47	
AD	1.43	
AR	1.43	

Top 5: 10.96 10.26

French		Speech
ES	2.91	2.17
LE	2.08	2.17
DE	2.02	2.11
EN	1.97	1.61
ON	1.70	2.00
NT	1.69	
RE	1.62	
AN	1.28	
LA	1.25	
ER	1.21	
TE	1.19	
EL	1.15	

Top 5: 10.68 10.06

German		Speech
ER	3.90	3.29
EN	3.61	4.44
CH	2.36	1.67
DE	2.31	1.90
EI	1.98	1.73
TE	1.98	
IN	1.71	
ND	1.68	
IE	1.48	
GE	1.45	
ST	1.21	
NE	1.19	

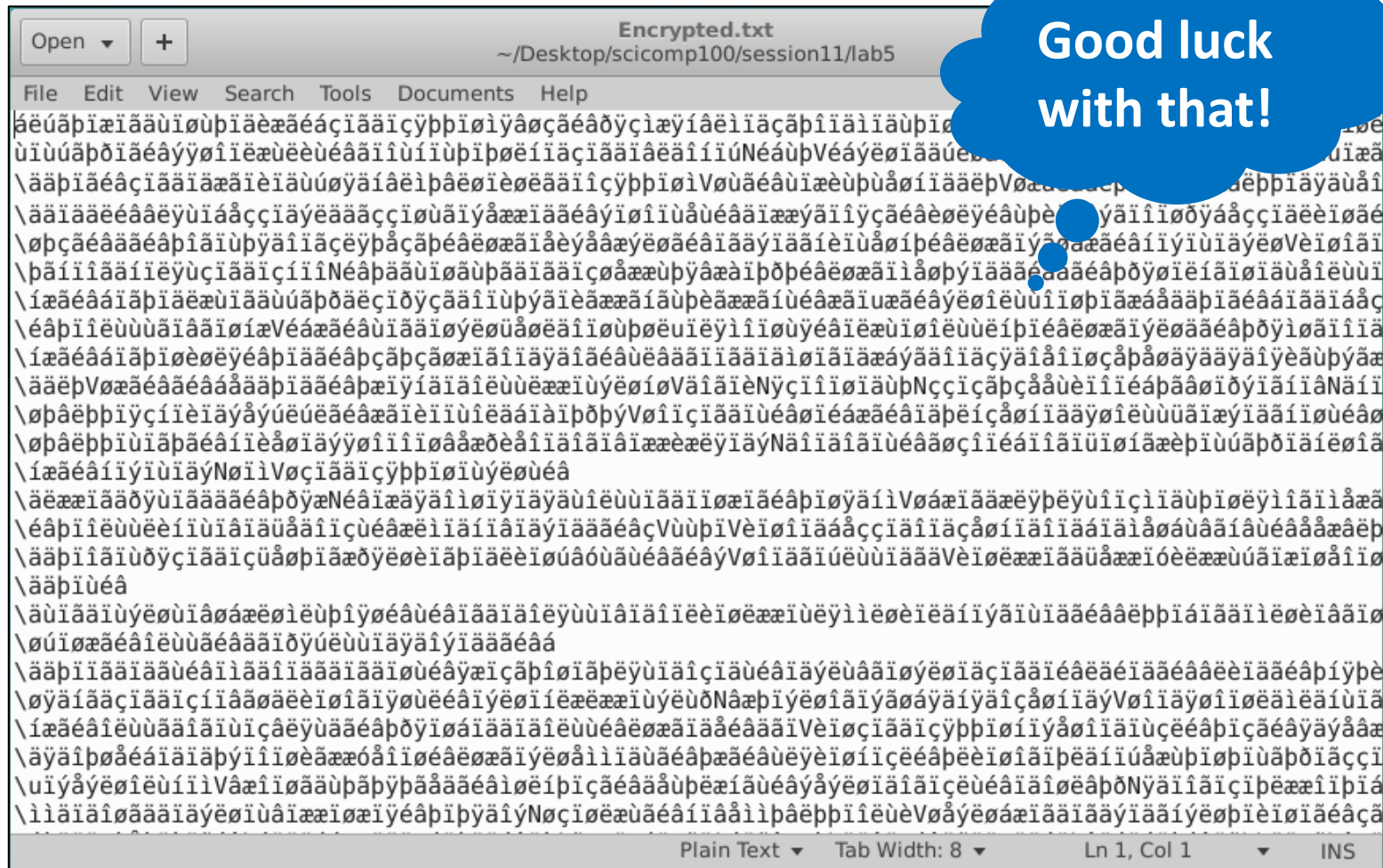
Top 5: 14.16 13.03

German is the most consistent language for bigrams

# Bigram Analysis

- You have been given **another** encrypted message!
- It **is** encrypted with a **monoalphabetic substitution cipher**, **but** single letter frequency analysis **does not** show any consistent Caesar shifting – it appears to be a **different shift for each plaintext letter**
- Even if you are **unable** to break the encryption, **can you tell what language was used** to author the plaintext?
  - Q: **Are you serious?** How can you possibly discern the author language if you **cannot even read the contents** in the first place?
  - A: Enigma was also **unbreakable**

# Open Lab 5 – Ciphertext.txt



# Run Lab 5 – Bigram Analysis

```
freq-bigrams
File Edit View Terminal Tabs Help
Most recurring bigrams in file:
Encrypted.txt

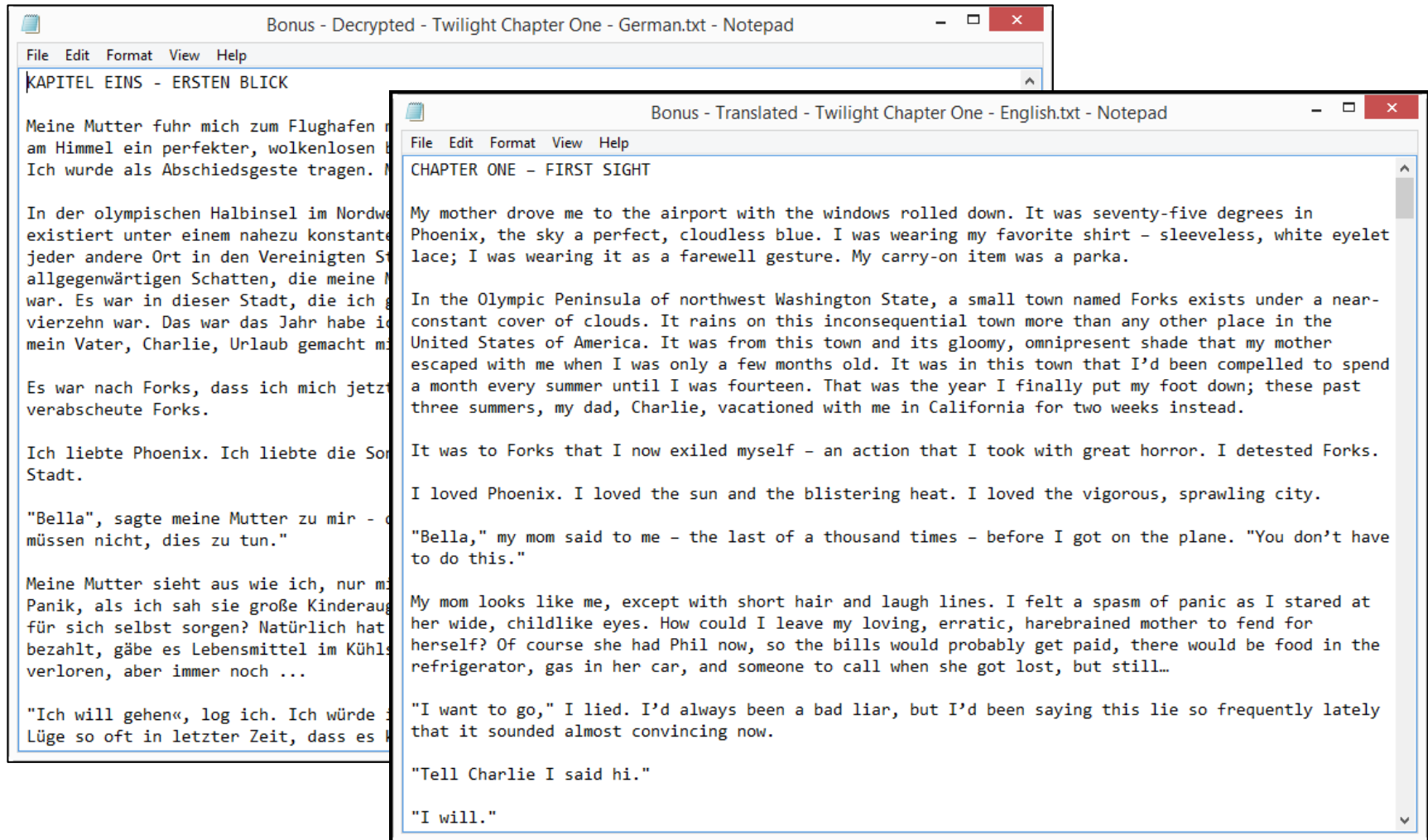
ASCII      CHARS      FREQ
(227, 228)  00        2.29
(227, 233)  00        2.10
(227, 239)  00        1.84
(228, 238)  00        1.60
(228, 239)  00        1.60
(233, 226)  00        3.64
(237, 239)  00        1.44
(238, 239)  00        1.71
(239, 227)  00        2.49
(239, 228)  00        3.88
(239, 248)  00        2.98
(239, 249)  00        1.44
(254, 239)  00        2.03

Process returned 0 (0x0)    execution time : 0.028 s
Press ENTER to continue.
```

Consider the frequencies of the **most recurring bigrams** in the cipher text.

**What language has this level of bigram consistency?**

# Lab 5 – Bigram Analysis

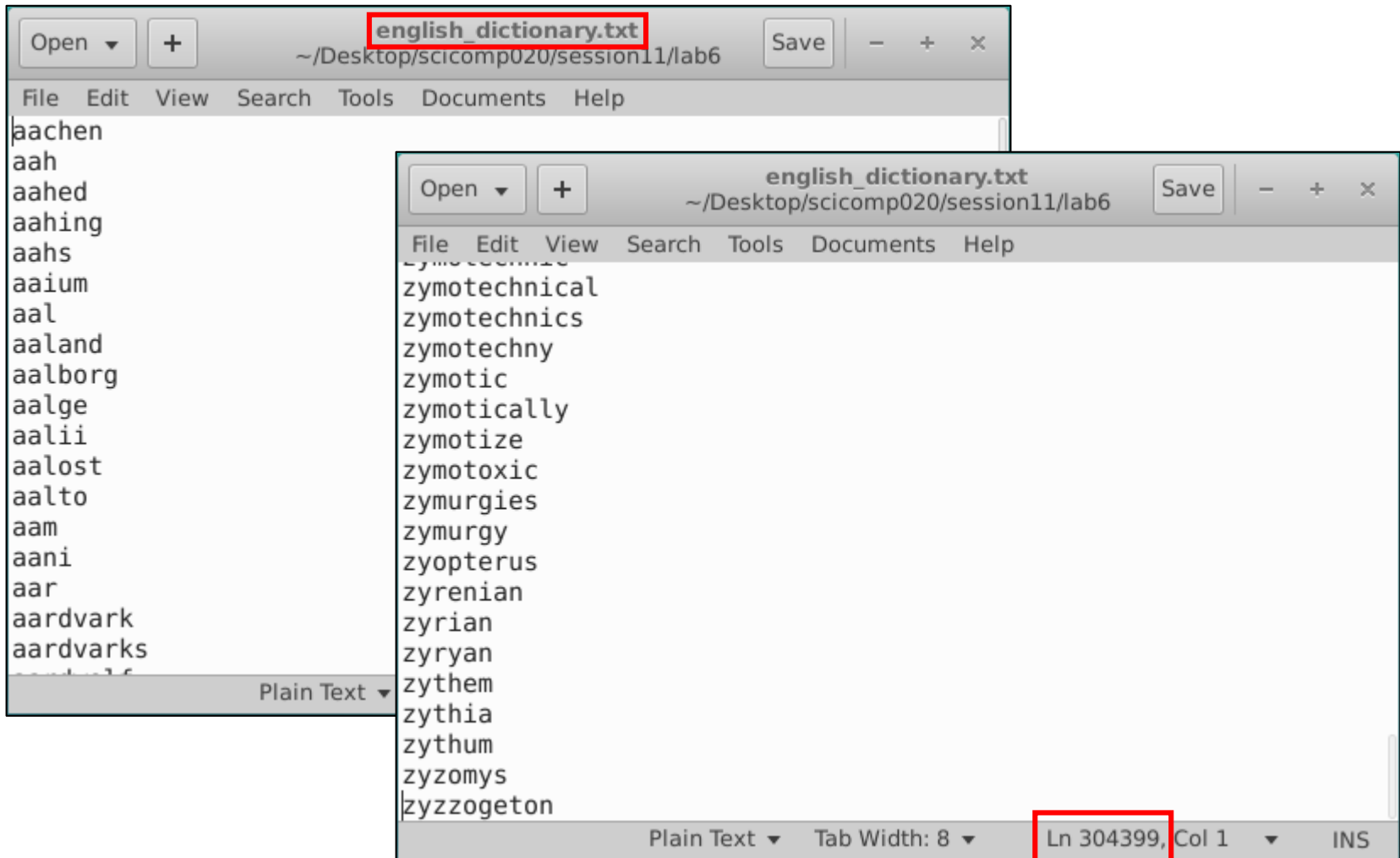


# Anagrams

- Different words all spelled with the same set of letters are called **anagrams**
- Given an **English dictionary**, how could you **find all** the anagrams of a word?
- What algorithm would you use? **Trial and error?**

Word	Letters	Anagrams	Permutations
STOP	4	6	24
LEAST	5	10	120
TRACES	6	9	720
PLAYERS	7	7	5,040
RESTRAIN	8	6	40,320
MASTERING	9	4	362,880
SUPERSONIC	10	3	3,628,800

# Anagrams



# Anagrams

- stop = post, pots, spot, tops
- least = slate, stale, steal, tales
- traces = carets, caster, caters, crates, reacts, recast
- players = parsley, parleys, replays, sparely
- restrain = retrains, strainer, terrains, trainers
- mastering = ???
- supersonic = ???

**Naive Approach** = Try every possible permutation of all given letters, checking in dictionary file to see if that permutation it is a valid English word



# Open Lab 6 – Slow Anagrams

```
anagrams-slow.cpp ✕  
1 // anagrams-slow.cpp  
2  
3 #include "stdafx.h"  
4  
5 using namespace std;  
6  
7 vector<string> phrases {  
8     "Stop", "Least", "Traces", "Players", "Restrained"  
9 };  
10  
11 vector  
12 vector  
13  
46 int main()  
47 {  
48     // Read in the dictionary file  
49     ifstream inputFile("english_dictionary.txt");  
50     string line;  
51     while (getline(inputFile, line)) {  
52         boost::trim(line);  
53         if (line.length() > 0)  
54             dictionary.push_back(line);  
55     }  
56  
57     // Start a timer  
58     boost::timer timer;  
59
```

## View Lab 6

### Slow Anagrams

```
// Find any anagrams for every requested phrase
for (auto& phrase : phrases) {

    // Convert phrase to all lowercase
    boost::to_lower(phrase);

    // Create vector of individual characters
    vector<char> letters;
    for (auto s : phrase)
        letters.push_back(s);

    // Add all permutations of letters to words vector
    words.clear();
    Permute<char>(&letters, letters.size());

    // Remove redundant permutations caused
    // by a phrase having duplicated letters
    sort(words.begin(), words.end());
    auto last = unique(words.begin(), words.end());
    words.erase(last, words.end());

    // Display only words that are found in the dictionary
    for (const auto& word : words)
        if (binary_search(dictionary.begin(),
                           dictionary.end(), word))
            cout << word << endl;

    cout << endl;
}
```

# View Lab 6

## Slow Anagrams

```
template <typename T>
string Concat(vector<T>* set)
{
    string c{};
    for (const auto& item : *set)
        c += item;
    return c;
}

template <typename T>
void Swap(vector<T>* set, int a, int b)
{
    T tmp = set->at(a);
    set->at(a) = set->at(b);
    set->at(b) = tmp;
}

template <typename T>
void Permute(vector<T>* set, int level)
{
    // Heap's Algorithm
    if (level == 0) {
        // At this point, set contains a new permutation
        words.push_back(Concat(set));
    } else {
        for (int i{ 0 }; i < level; ++i) {
            Permute(set, level - 1);
            Swap(set, level % 2 == 1 ? 0 : i, level - 1);
        }
    }
}
```

# Lab 6 – Slow Anagrams

## Permutations by interchanges

By B. R. Heap

Methods for obtaining all possible permutations of a number of objects, in which each permutation differs from its predecessor only by the interchange of two of the objects, are discussed. Details of two programs which produce these permutations are given, one allowing a specified position to be filled by each of the objects in a predetermined order, the other needing the minimum of storage space in a computer.

In programs of a combinatorial nature, it is often required to produce all possible permutations of  $N$  objects. Many methods can be used for this purpose and a general review of them has been given by D. H. Lehmer in *Proceedings of Symposia in Applied Mathematics* (American Mathematical Society), Vol. 10, p. 179. In this note we shall describe methods for obtaining the permutations in which each permutation is obtained from its predecessor by means of the interchange of two of the objects. Thus  $(N - 2)$  of the  $N$  objects are undisturbed in going from one permutation to the next.

We shall consider values of  $N$  up to  $N = 12$ , since the

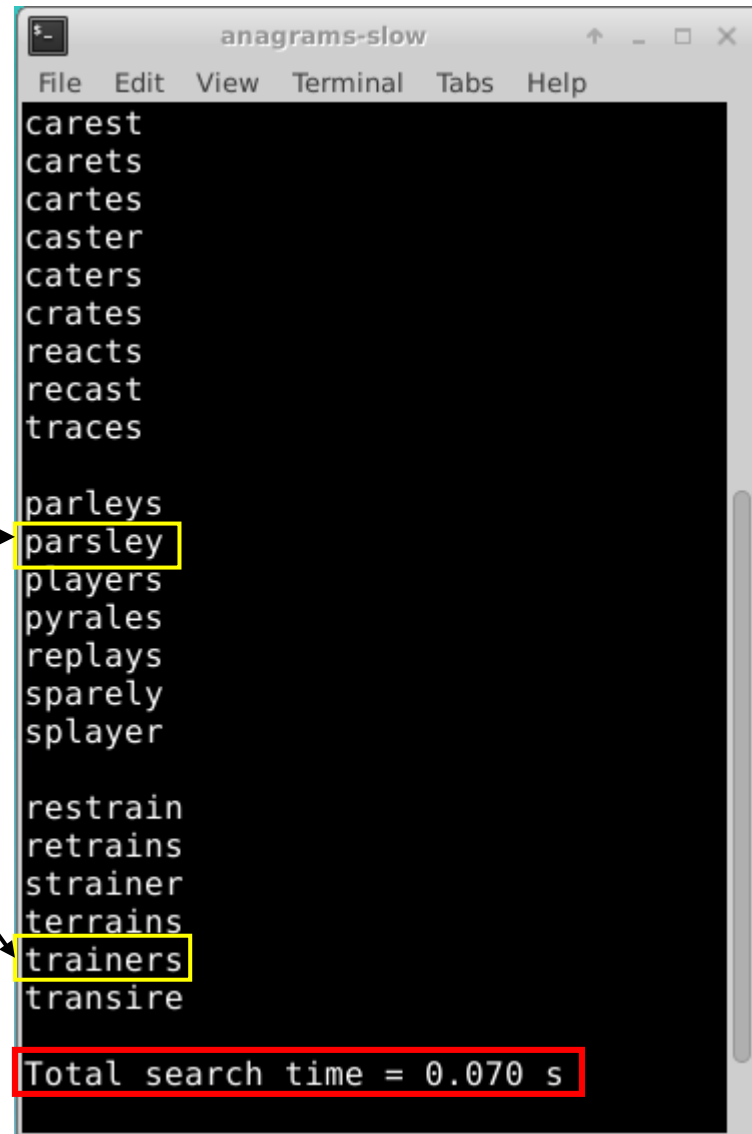
of the first  $(n - 1)$  objects and again permute the first  $(n - 1)$  objects. Again interchange the  $n$ th object with one of the first  $(n - 1)$  objects, making sure that this object has not previously occupied the  $n$ th cell. Now repeat the process until each of the objects has filled the  $n$ th position while the other  $(n - 1)$  have been permuted, and clearly all  $n!$  permutations have been found. Finally, it is clear that two objects can be permuted by a simple interchange, and so  $N$  objects can be so permuted. To achieve this one only needs to specify a total of

$$1 + 2 + 3 + \dots + (N - 1) = \frac{1}{2} N(N - 1)$$

1963

## Run Lab 6 – Slow Anagrams

- Stop
- Least
- Traces
- Players
- Restrain



```
anagrams-slow
File Edit View Terminal Tabs Help
carest
carets
cartes
caster
caters
crates
reacts
recast
traces

parleys
parsley
players
pyrales
replays
sparely
splayer

restrain
retrains
strainer
terrains
trainers
transire

Total search time = 0.070 s
```

# Anagrams

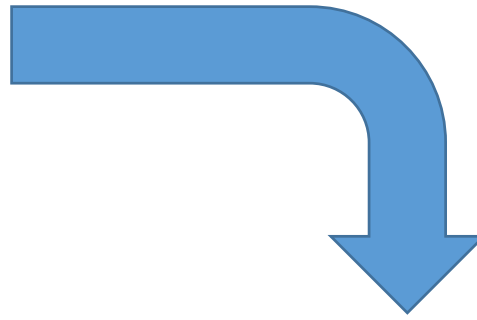
- stop = post, pots, spot, tops
  - least = slate, stale, steal, tales
  - traces = carets, caster, caters, crates, reacts, recast
  - players = parsley, parleys, replays, sparely
  - restrain = retrains, strainer, terrains, trainers
- mastering = ???
  - supersonic = ???

**Novel Approach** - Thinking in reverse! First, SORT the given dictionary file **by word letter order**, then SEARCH for equal first columns (e.g. "OPST") to find all anagrams in the dictionary

A way of finding anagrams that much  
faster than by trying every permutation!

POSSUM	M	O	P	S	S	U		MOPSSU
POST	O	P	S	T				OPST
POSTAGE	A	E	G	O	P	S	T	AEGOPST
POTION	I	N	O	O	P	T		INOOPT
POTS	O	P	S	T				OPST
POUCH	C	H	O	P	U			CHOPU
SPOT	O	P	S	T				OPST
SPOUSE	E	O	P	S	S	U		EOPSSU
STOP	O	P	S	T				OPST
TOPICS	C	I	O	P	S	T		CIOPT
TOPS	O	P	S	T				OPST
TORCH	C	H	O	R	T			CHORT

MOPSSU	POSSUM
OPST	POST
AEGOPST	POSTAGE
INOOPT	POTION
OPST	POTS
CHOPU	POUCH
OPST	SPOT
EOPSSU	SPOUSE
OPST	STOP
CIOPST	TOPICS
OPST	TOPS
CHORT	TORCH



AEGOPST	POSTAGE
CHOPU	POUCH
CHORT	TORCH
CIOPST	TOPICS
EOPSSU	SPOUSE
INOOPT	POTION
MOPSSU	POSSUM
OPST	POST
OPST	POTS
OPST	SPOT
OPST	STOP
OPST	TOPS



# Open Lab 7

## Fast Anagrams

anagrams-fast.cpp ✕

```
1 // anagrams-fast.cpp
2
3 #include "stdafx.h"
4
5 using namespace std;
6
7 class Anagram
8 {
9 public:
10     Anagram(string word);
11     string word;
12     string letters;
13 };
14
15 Anagram::Anagram(string word)
16 {
17     boost::to_lower(word);
18     this->word = word;
19     sort(word.begin(), word.end());
20     this->letters = word;
21 }
22
23 auto compare_lambda = []
24 (const Anagram& a, const Anagram& b) -> bool {
25     return a.letters < b.letters;
26 };
27
28 vector<string> phrases {
29     "Stop", "Least", "Traces", "Players", "Restrain",
30     "Mastering", "Supersonic"
31 };
32
33 vector<Anagram> anagrams;
```

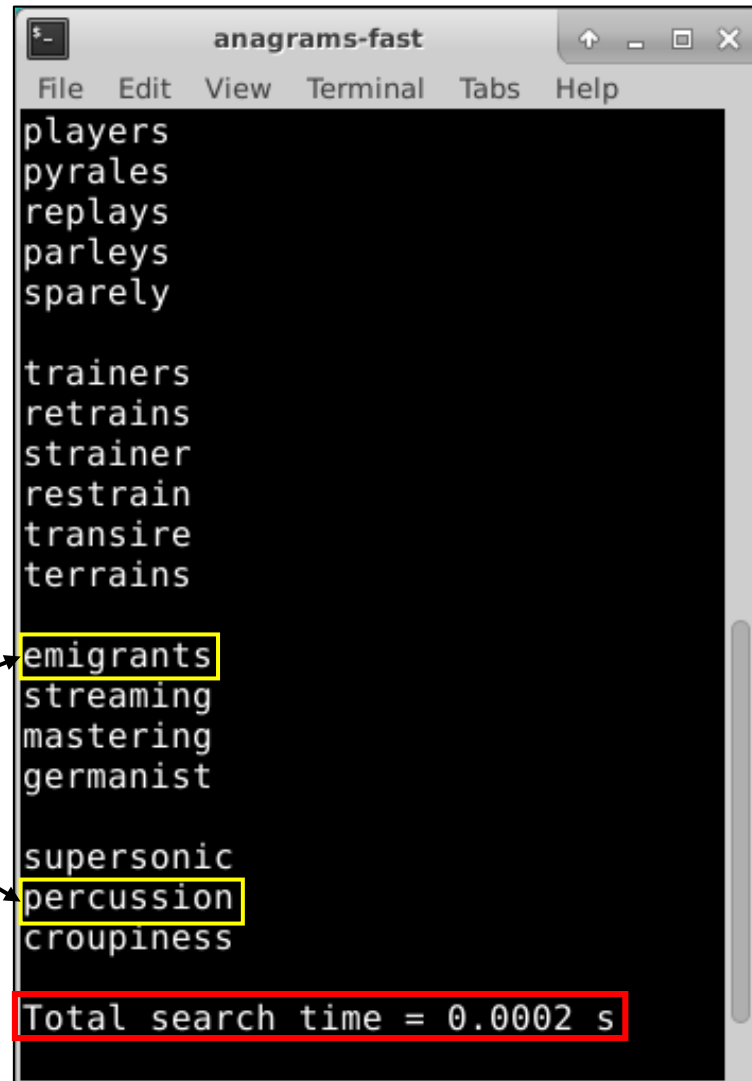
# View Lab 7

## Fast Anagrams

```
35 int main()
36 {
37     // Load dictionary into the anagrams vector
38     string line;
39     ifstream inputFile("english_dictionary.txt");
40     while (getline(inputFile, line)) {
41         boost::trim(line);
42         if (line.length() > 0 )
43             anagrams.push_back(Anagram(line));
44     }
45
46     // Sort the anagrams by their sorted letters
47     sort(anagrams.begin(), anagrams.end(), compare_lambda);
48
49     // Start a timer
50     boost::timer timer;
51
52     for (const auto& phrase : phrases) {
53         Anagram input{ phrase };
54
55         // Find *first* word in dictionary that has sorted letters
56         // matching the current phrase also sorted by letters
57         auto lower = lower_bound(anagrams.begin(),
58                                 anagrams.end(), input, compare_lambda);
59
60         // Find *last* word in dictionary that has sorted letters
61         // matching the current phrase also sorted by letters
62         auto upper = upper_bound(lower, anagrams.end(),
63                                 input, compare_lambda);
64
65         // Display all dictionary words matching the phrase's anagram
66         for(auto& a{lower}; a< upper; ++a)
67             cout << a->word << endl;
68
69         cout << endl;
70     }
71
72     cout << "Total search time = "
73         << fixed << setprecision(4)
74         << timer.elapsed() << " s" << endl;
75
76     return 0;
77 }
78
```

## Run Lab 7 – Fast Anagrams

- Stop
- Least
- Traces
- Players
- Restrain
- Mastering
- Supersonic



```
anagrams-fast
File Edit View Terminal Tabs Help

players
pyrales
replays
parleys
sparely

trainers
retrains
strainer
restrain
transire
terrains

emigrants
streaming
mastering
germanist

supersonic
percussion
croupiness

Total search time = 0.0002 s
```

# Slow vs. Fast Anagrams

- Slow Anagram approach took **700 ms** while the Fast Anagram approach took **2ms** – that is a **350X speedup** despite including **3 additional (longer) phrases!**
  - Even **binary searching** (as used in Lab 6) cannot overcome the penalty of enumerating over permutations which **could never be valid English words** – this is the inherent problem with the Slow Anagram approach
- The **dictionary** defines the **search space** – don't expand the search space by testing **unconstrained permutations** – this leads to **combinational explosion**
  - Supersonic has 3M letter permutations, but only **3 anagrams**
  - Elvis = Lives . . . **Listen = Silent**

# Open Lab 8

## Compound Anagrams

What **two** smaller words can be made out of the letters in the word **dormitory**?

```
class Anagram2
{
public:
    Anagram2(string word);
    Anagram2(string word1, string word2);
    string word1;
    string word2;
    string letters;
};

Anagram2::Anagram2(string word)
{
    sort(word.begin(), word.end());
    this->letters = word;
}

Anagram2::Anagram2(string word1, string word2)
{
    this->word1 = word1;
    this->word2 = word2;
    string word = word1 + word2;
    sort(word.begin(), word.end());
    this->letters = word;
}

auto compare_lambda = [](const Anagram2& a, const Anagram2& b) ->bool {
    return a.letters < b.letters; };

bool contained(string a, string b)
{
    // Is a fully & uniquely contined in b?
    if (a.length() > b.length())
        return false;

    for (size_t i{}; i < a.length(); i++)
    {
        auto pos = b.find(a[i], i);
        if (pos == string::npos)
            return false;
        b[pos] = ' ';
    }

    return true;
}
```

room (moor)  $\approx$  dormitory (dimoorrrty)

# View Lab 8

## Compound Anagrams

```
// Read in the dictionary file
ifstream inputFile("english_dictionary.txt");
string line;
while (getline(inputFile, line)) {
    boost::trim(line);
    if (line.length() > 0) {
        Anagram2 word(line);
        // Only add words from dictionary that could
        // possibly be in the anagram of the given phrase
        if (contained(word.letters, input.letters))
            dictionary.push_back(line);
    }
}

// Create compound anagram from every
// successive two words in the dictionary
for (size_t i{}; i < dictionary.size() - 1; i++)
    for (size_t j{ i + 1 }; j < dictionary.size(); j++)
        anagrams.push_back(
            Anagram2(dictionary.at(i),
                dictionary.at(j)));

// Sort the anagrams by their sorted letters
sort(anagrams.begin(), anagrams.end(), compare_lambda);

// Find *first* word in dictionary that has sorted letters
// matching the current phrase also sorted by letters
auto lower = lower_bound(anagrams.begin(), anagrams.end(),
    input, compare_lambda);

// Find *last* word in dictionary that has sorted letters
// matching the current phrase also sorted by letters
auto upper = upper_bound(lower, anagrams.end(),
    input, compare_lambda);

// Create a vector concatenating both words of each anagram
vector<string> phrases;
for (auto& a = lower; a < upper; a++)
    phrases.push_back(a->word1 + " " + a->word2);

// Sort & display the vector of the compound anagrams
sort(phrases.begin(), phrases.end());
for (auto& s : phrases)
    cout << s << endl;
```

dormitory (dimoorrtty) =  
dirty room (dimoorrtty)

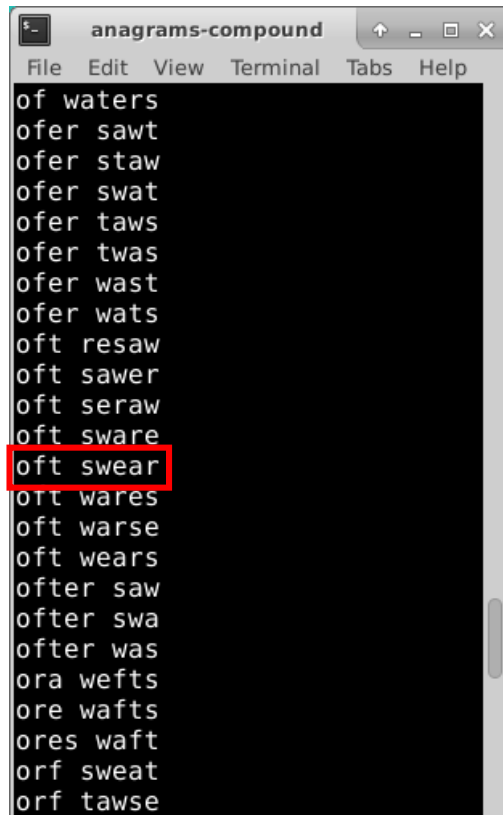
## Edit Lab 8 - Compound Anagrams

Enable the other phrases to reveal  
lurking compound anagrams.. 😊

```
52  vector<string> dictionary;  
53  vector<Anagram2> anagrams;  
54  
55  int main()  
56  {  
57      string phrase{ "Dormitory" };  
58      //string phrase{ "Software" };  
59      //string phrase{ "Mother-In-Law" };  
60  }
```

# Run Lab 8 - Compound Anagrams

```
int main()
{
    //string phrase{ "Dormitory" };
    string phrase{ "Software" };
    //string phrase{ "Mother-In-Law" };
```

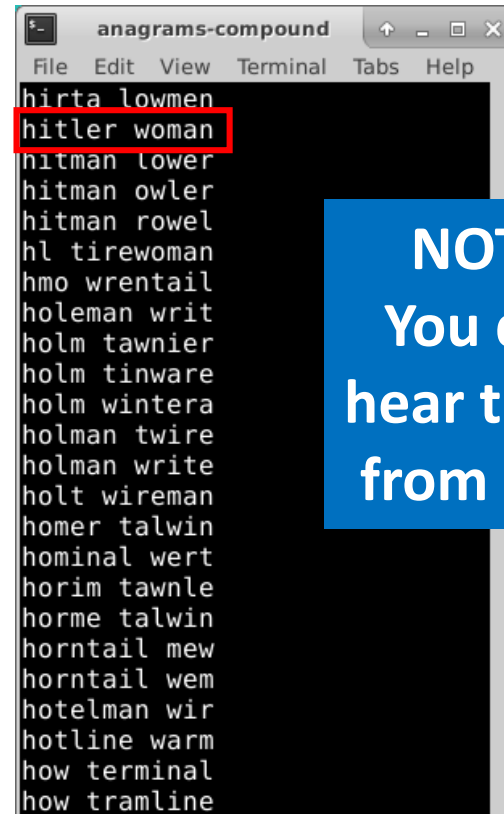


anagrams-compound

File Edit View Terminal Tabs Help

of waters  
ofer sawt  
ofer staw  
ofer swat  
ofer taws  
ofer twas  
ofer wast  
ofer wats  
oft resaw  
oft sawer  
oft seraw  
oft sware  
**oft swear**  
ort wares  
oft warse  
oft wears  
offer saw  
offer swa  
offer was  
ora wefts  
ore wafts  
ores waft  
orf sweat  
orf tawse

```
int main()
{
    //string phrase{ "Dormitory" };
    //string phrase{ "Software" };
    string phrase{ "Mother-In-Law" };
```



anagrams-compound

File Edit View Terminal Tabs Help

hirta lowmen  
**hitler woman**  
hitman lower  
hitman owler  
hitman rowel  
hl tirewoman  
hmo wrentail  
holeman writ  
holm tawnier  
holm tinware  
holm wintera  
holman twire  
holman write  
holt wireman  
homer talwin  
hominal wert  
horim tawnle  
horme talwin  
horntail mew  
horntail wem  
hotelman wir  
hotline warm  
how terminal  
how tramline

**NOTICE:**  
You didn't  
hear this one  
from me! 😊



# Who knew?

**The Morse Code = Here come dots**  
**The meaning of life = The fine game of nil**  
**Statue of Liberty = Built to stay free**

# Now you know...

- C++ **strings** are essentially a vector of type **char**
  - **ASCII** is an international standard for encoding most Western language characters into a single byte
- Character histograms enable **frequency analysis**
  - Caesar-Shift ciphers are not very secure
  - All **monoalphabetic substitution ciphers** can be broken with **bigram analysis**
  - Using “brute force” to crack a cipher is often **intractable** – get statistics on your side to help you out!
- **Heap’s Algorithm** will generate all **permutations** of a set
- Consider problems *backwards*: don’t expand search spaces