

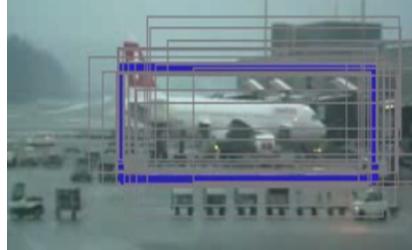
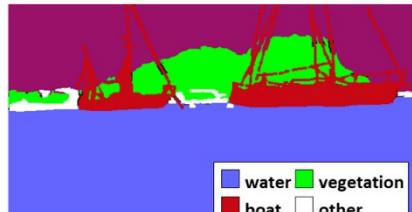
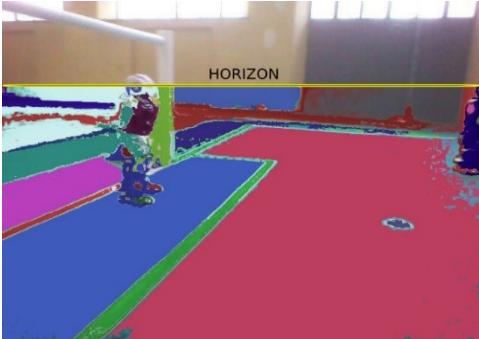
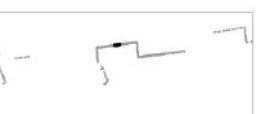
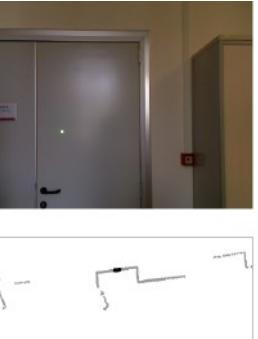


UNIVERSITÀ DEGLI STUDI DELLA BASILICATA

Corso di Sistemi Informativi
A.A. 2019/2020

Features

Aprile 2020



Riferimenti

- La maggior parte di queste slide sono adattate da Noah Snavely - CS5670: Computer Vision
["Lecture 4: Intro to local features and Harris corner detection"](#)
- Per le slide adattate da altri autori vengono fornite le relative citazioni
- I contenuti fanno riferimento al capitolo 4 del libro "Computer Vision: Algorithms and Applications" di Richard Szeliski, disponibile al seguente indirizzo
<http://szeliski.org/Book/>

Il corso

- Home page del corso
<http://web.unibas.it/bloisi/corsi/visione-e-percezione.html>
- Docente: Domenico Daniele Bloisi
- Periodo: Il semestre marzo 2020 – giugno 2020

Martedì 17:00-19:00 (Aula GUGLIELMINI)

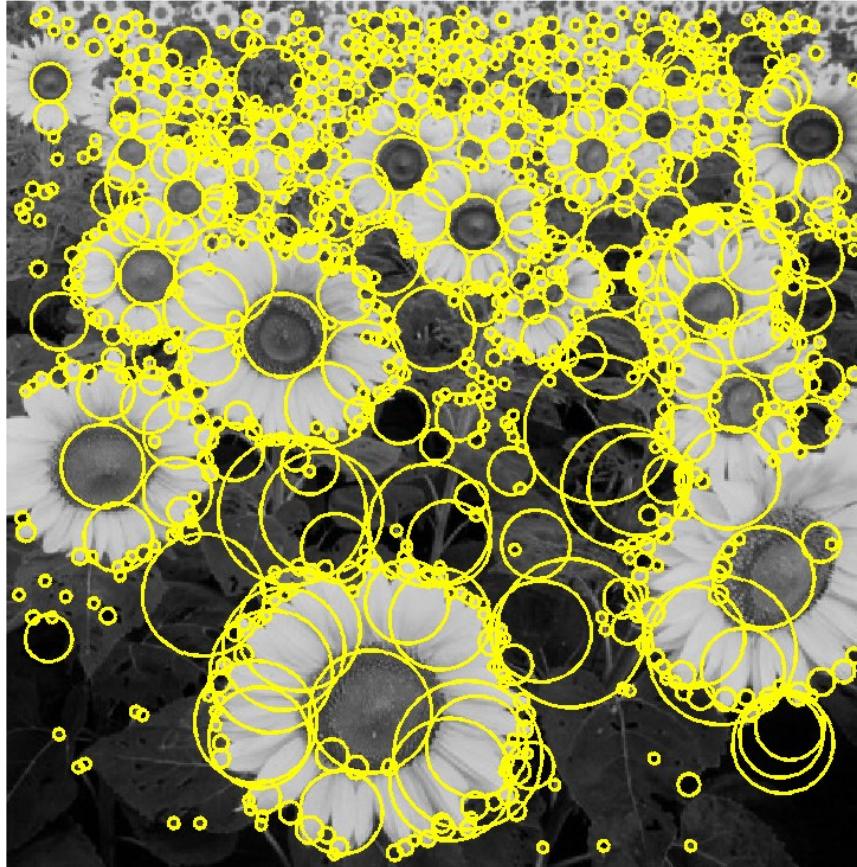
Mercoledì 8:30-10:30 (Aula GUGLIELMINI)

Feature extraction

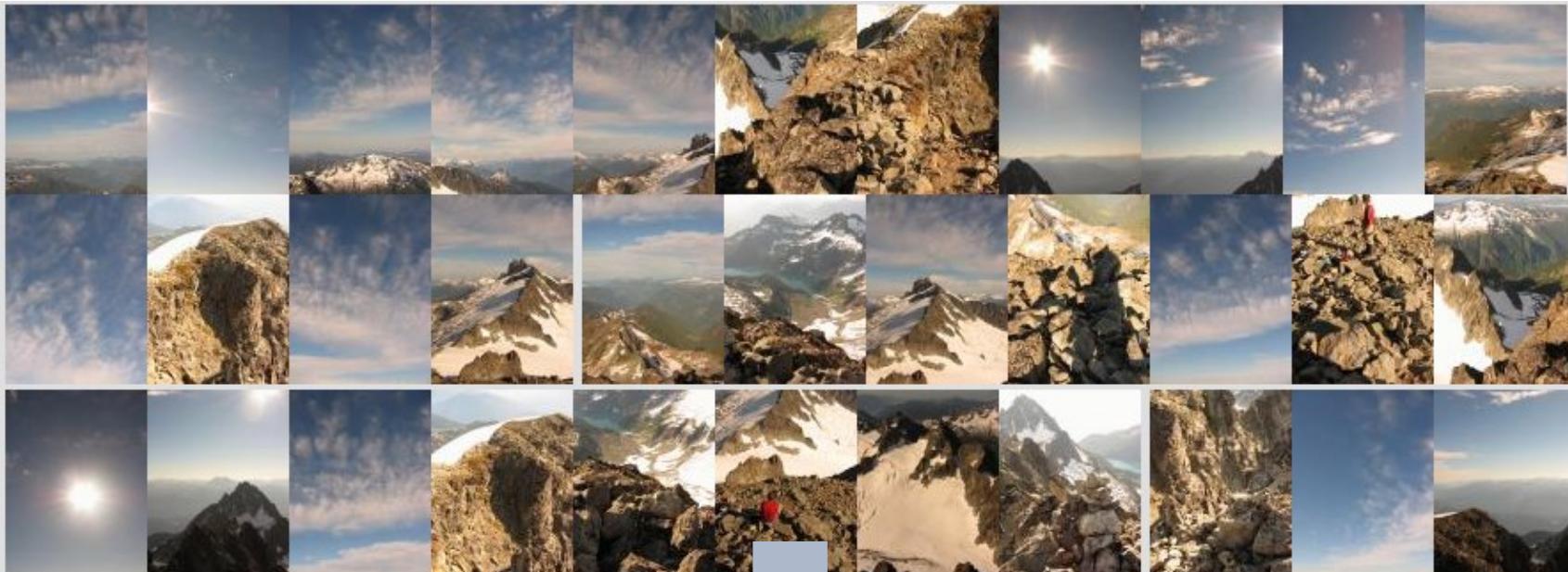
corners



blobs



Automatic panoramas



Credit: Matt Brown

Automatic panoramas



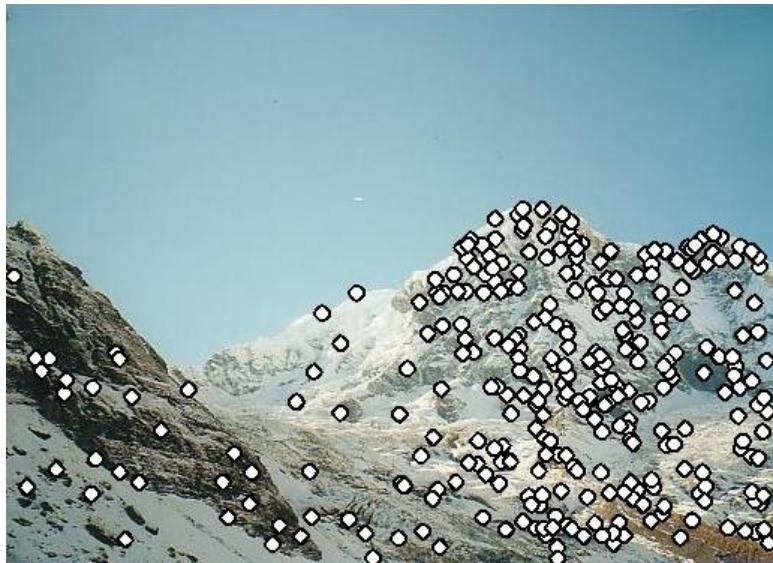
Feature matching

We have two images, how do we combine them?



Feature matching

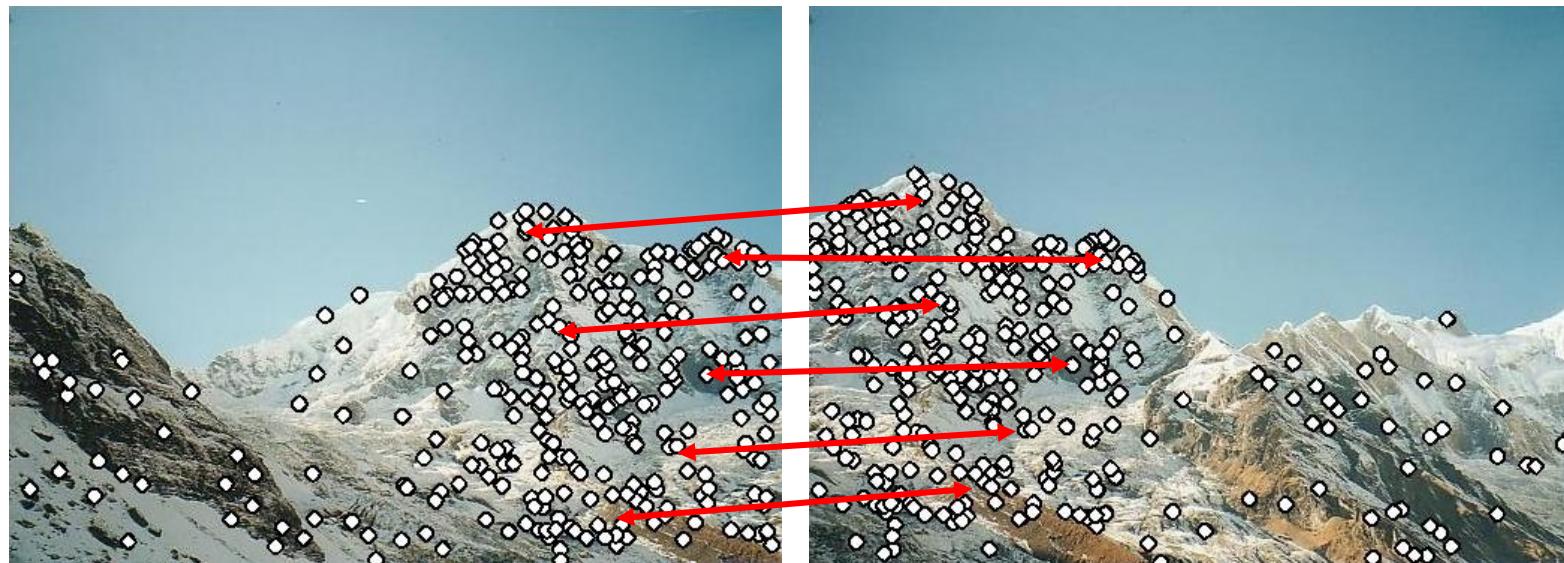
Step 1: extract features



Feature matching

Step 1: extract features

Step 2: match features



Feature matching

Step 1: extract features

Step 2: match features

Step 3: align images



Visual SLAM



<https://www.youtube.com/watch?v=DPLh6MoxPAk>

Image matching



by [Diva Sian](#)



by [swashford](#)

Harder case

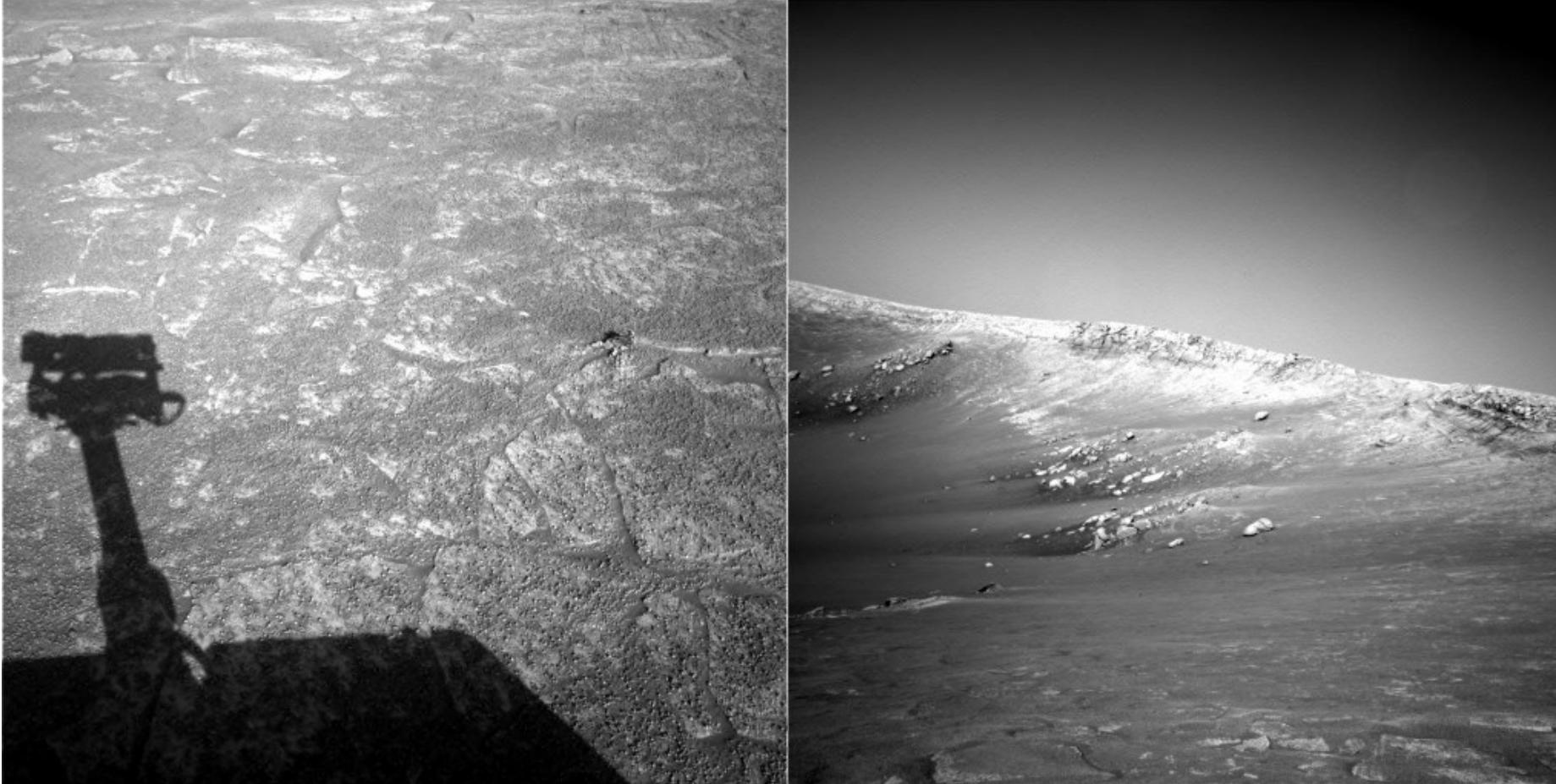


by [Diva Sian](#)

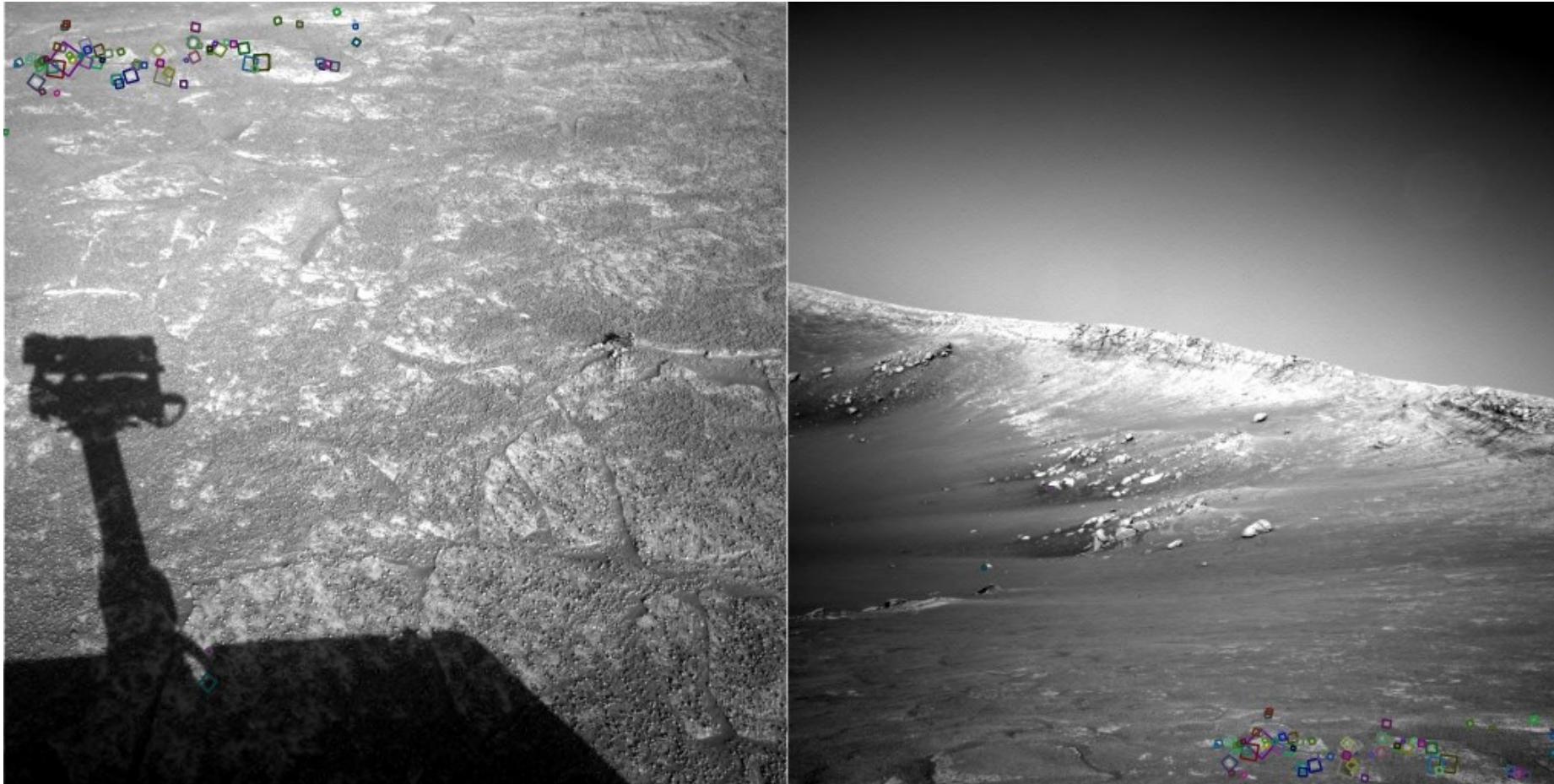


by [scgbt](#)

Harder still?

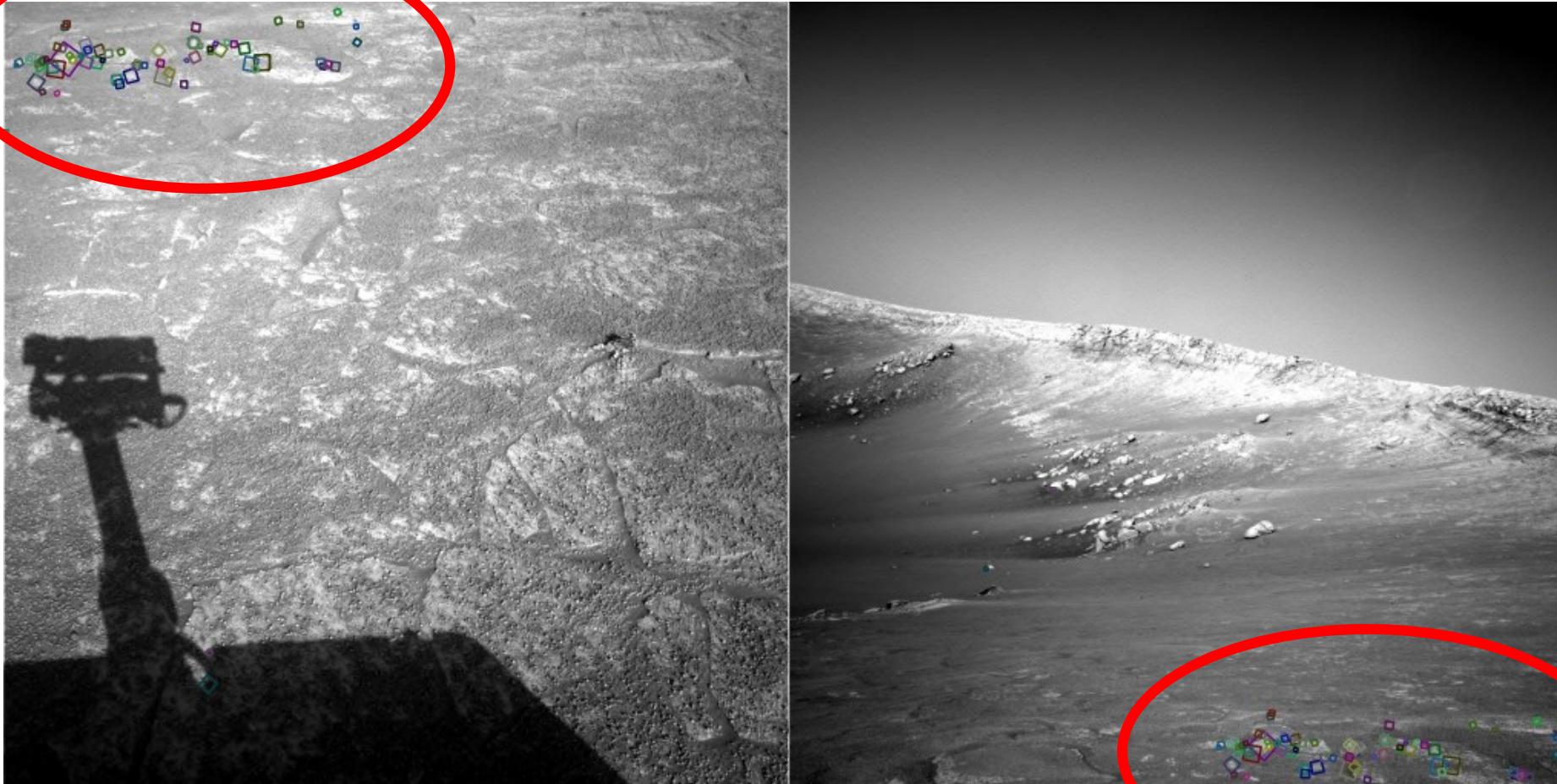


Harder still?



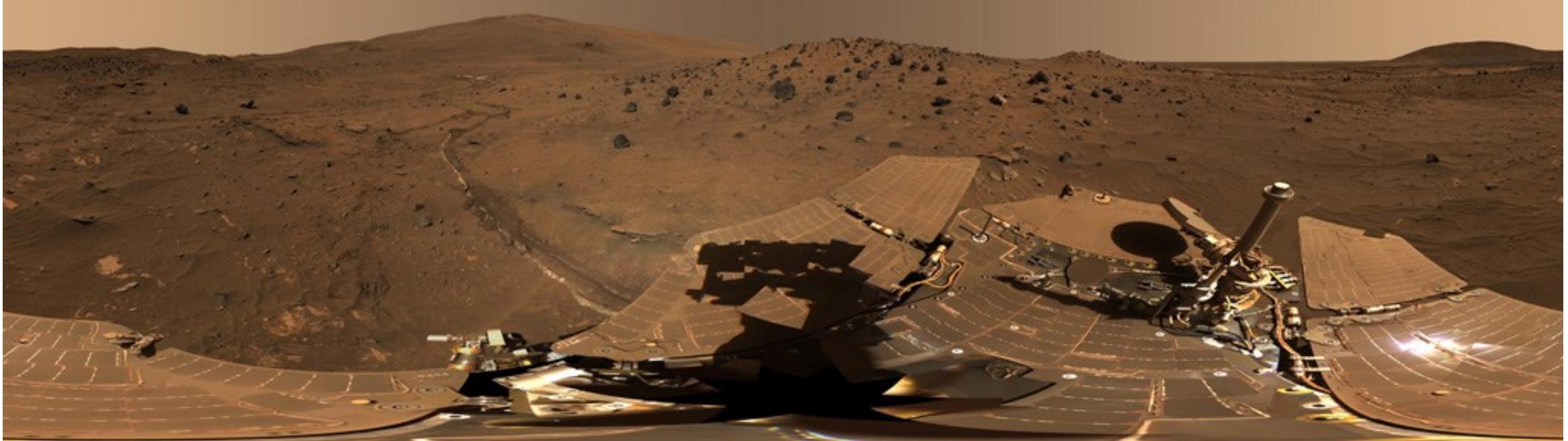
NASA Mars Rover images
with SIFT feature matches

Harder still?



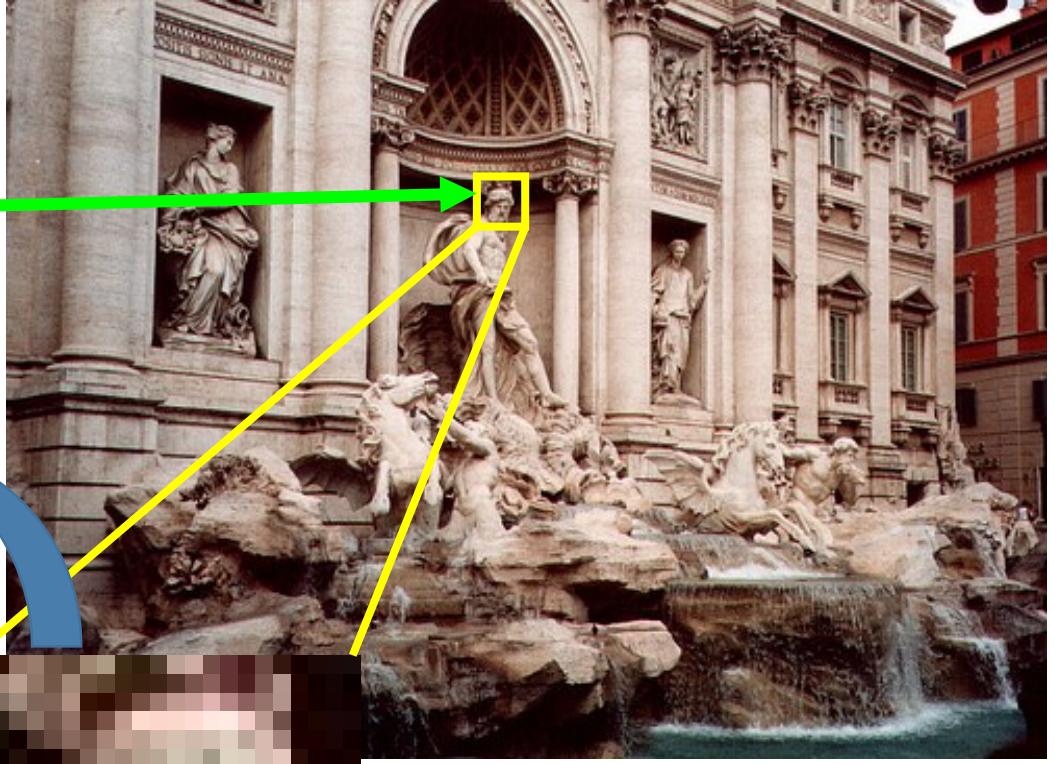
NASA Mars Rover images
with SIFT feature matches

Spirit Mars Rover Panorama



<https://mars.nasa.gov/mer/multimedia/panoramas/spirit/>

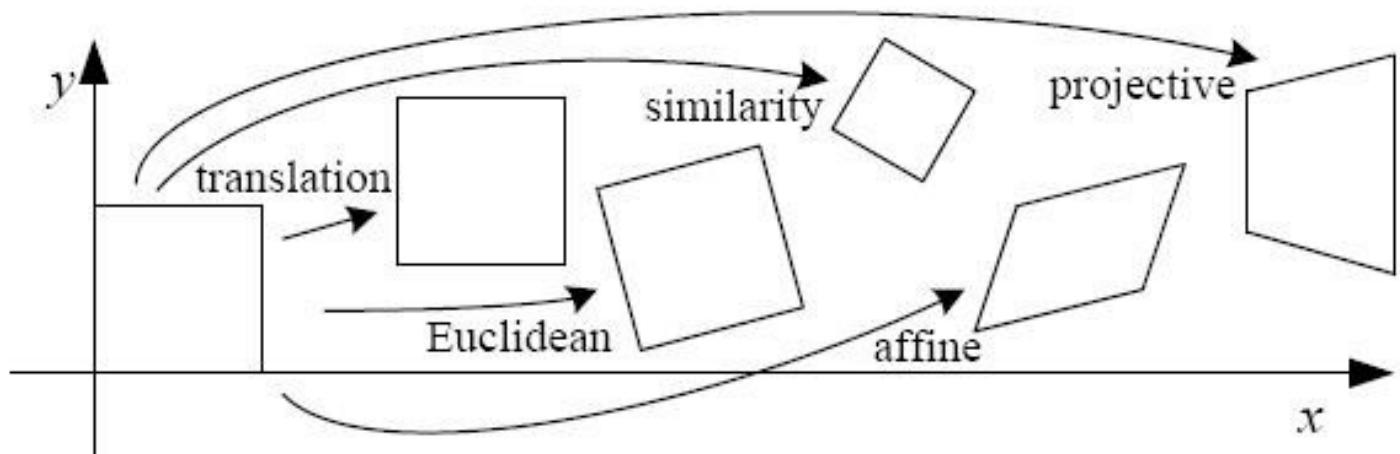
Feature matching



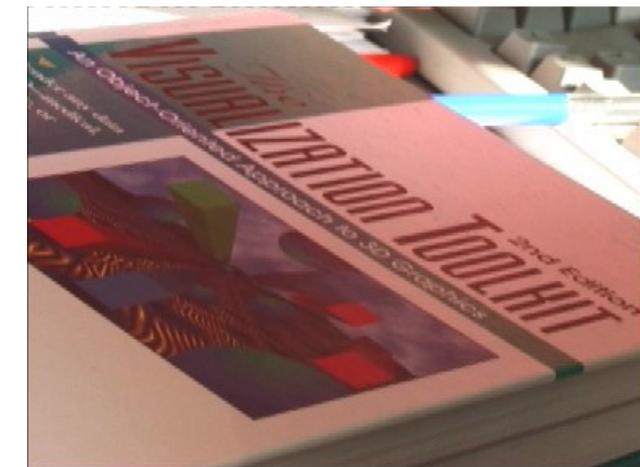
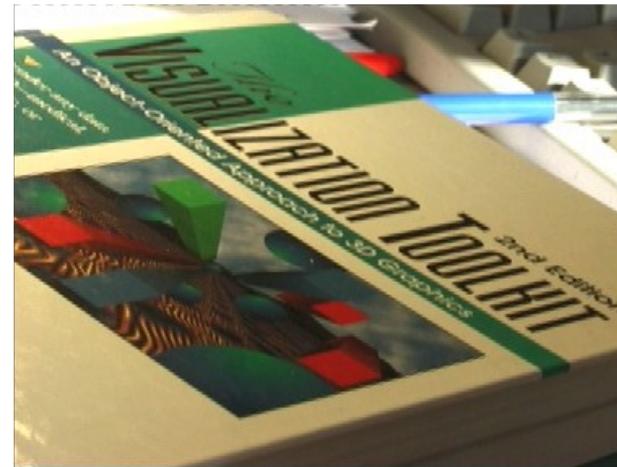
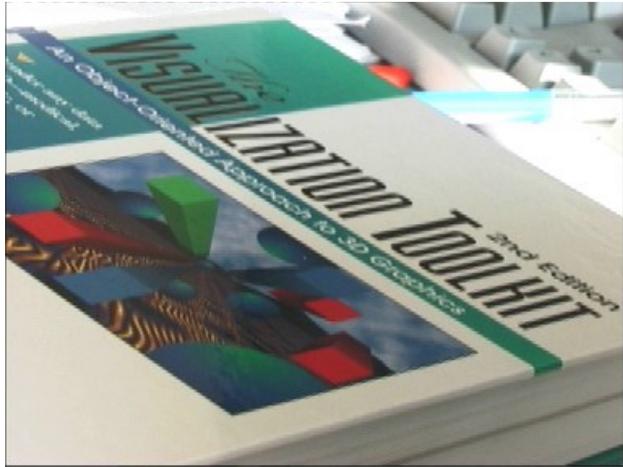
Geometric transformations

- Translation
- Euclidean (translation + rotation)
- Similarity (translation + rotation + scale)
- Affine transformations
- Projective transformations

Only holds
for planar patches



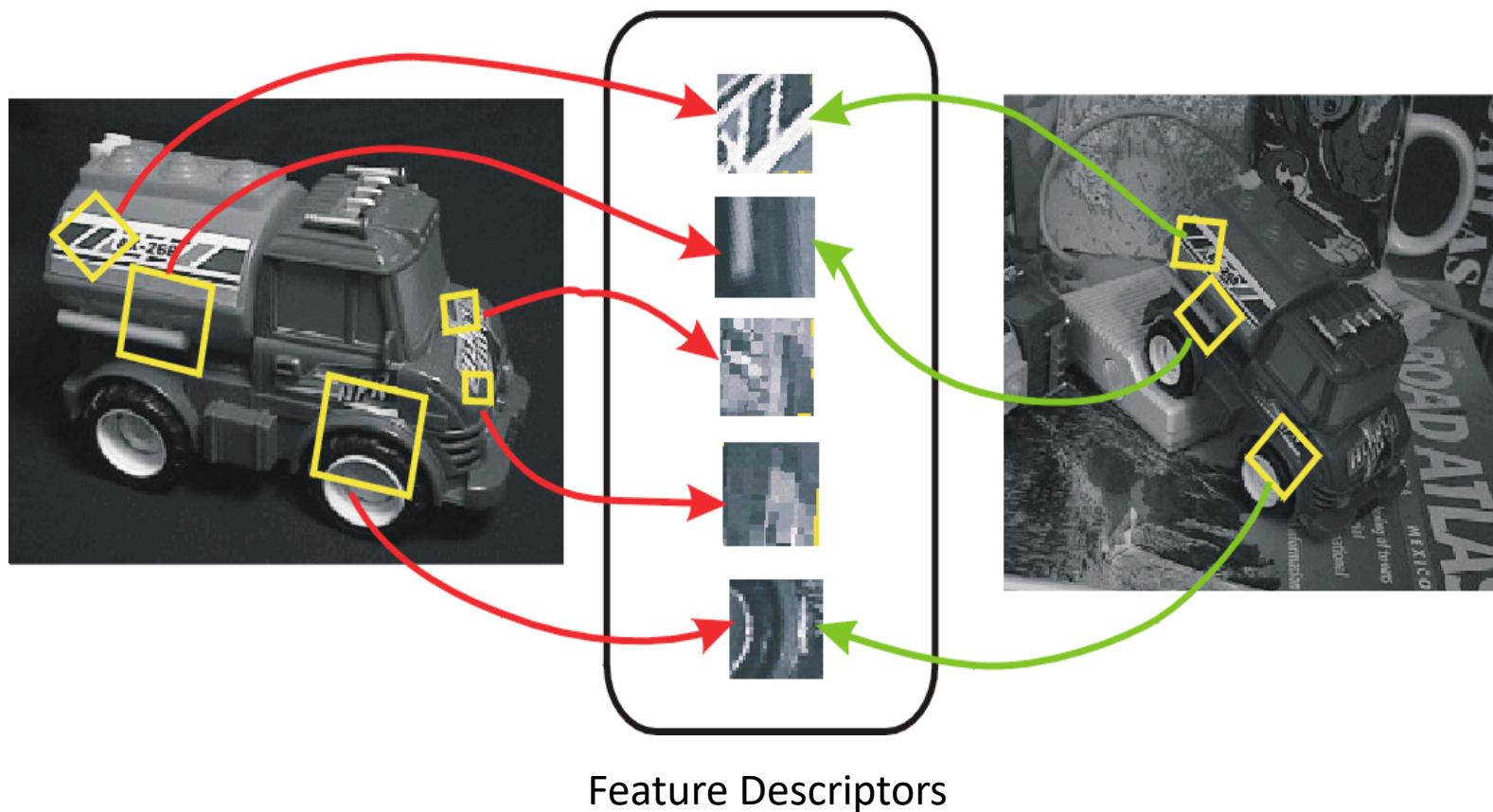
Photometric transformations



Invariant Local Features

Find features that are invariant to transformations

- geometric invariance: translation, rotation, scale
- photometric invariance: brightness, exposure, ...



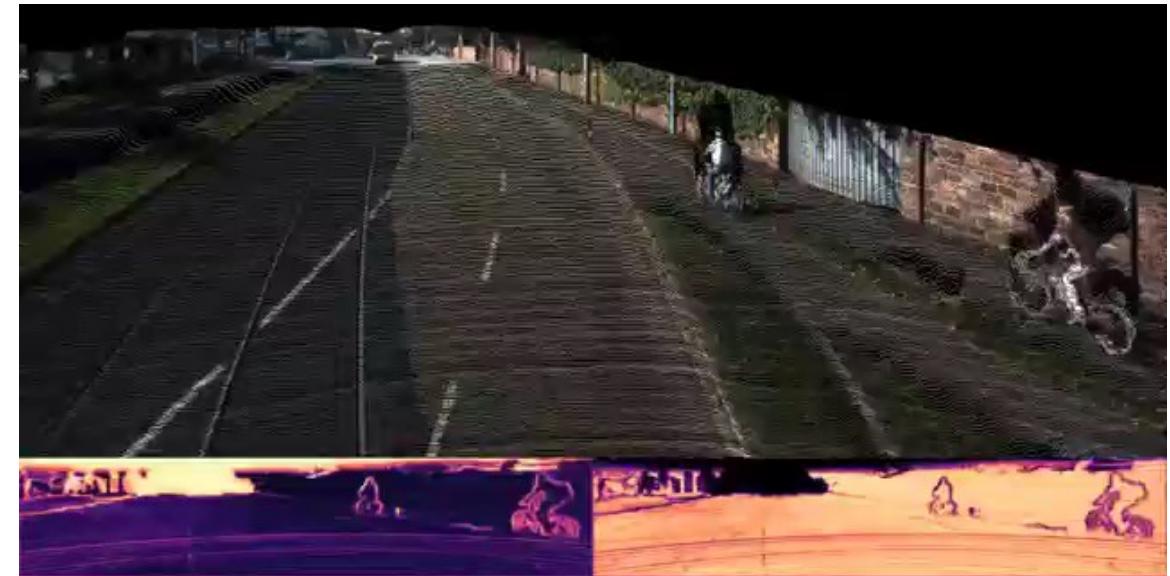
Advantages of local features

- **Locality**
 - features are local, so robust to occlusion and clutter
- **Quantity**
 - hundreds or thousands in a single image
- **Distinctiveness**
 - can differentiate a large database of objects
- **Efficiency**
 - real-time performance achievable

More motivations...

Feature points are used for:

- Image alignment (e.g., mosaics)
- 3D reconstruction
- Motion tracking (e.g. for AR)
- Object recognition
- Image retrieval
- Robot/car navigation
- ... other



<https://www.youtube.com/watch?v=Kr0W7io5rHw>

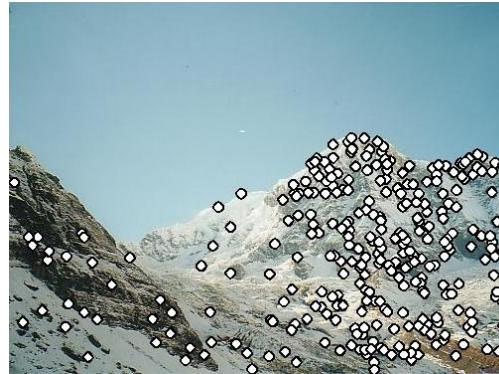
Approach

- 1. Feature detection:** find it
- 2. Feature descriptor:** represent it
- 3. Feature matching:** match it

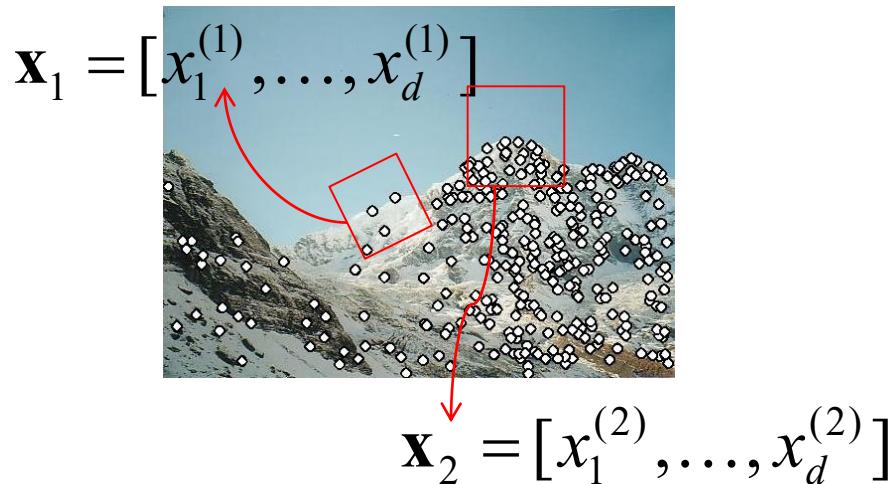
Feature tracking: track it, when motion

Local features: main components

- 1) Detection: Identify the interest points



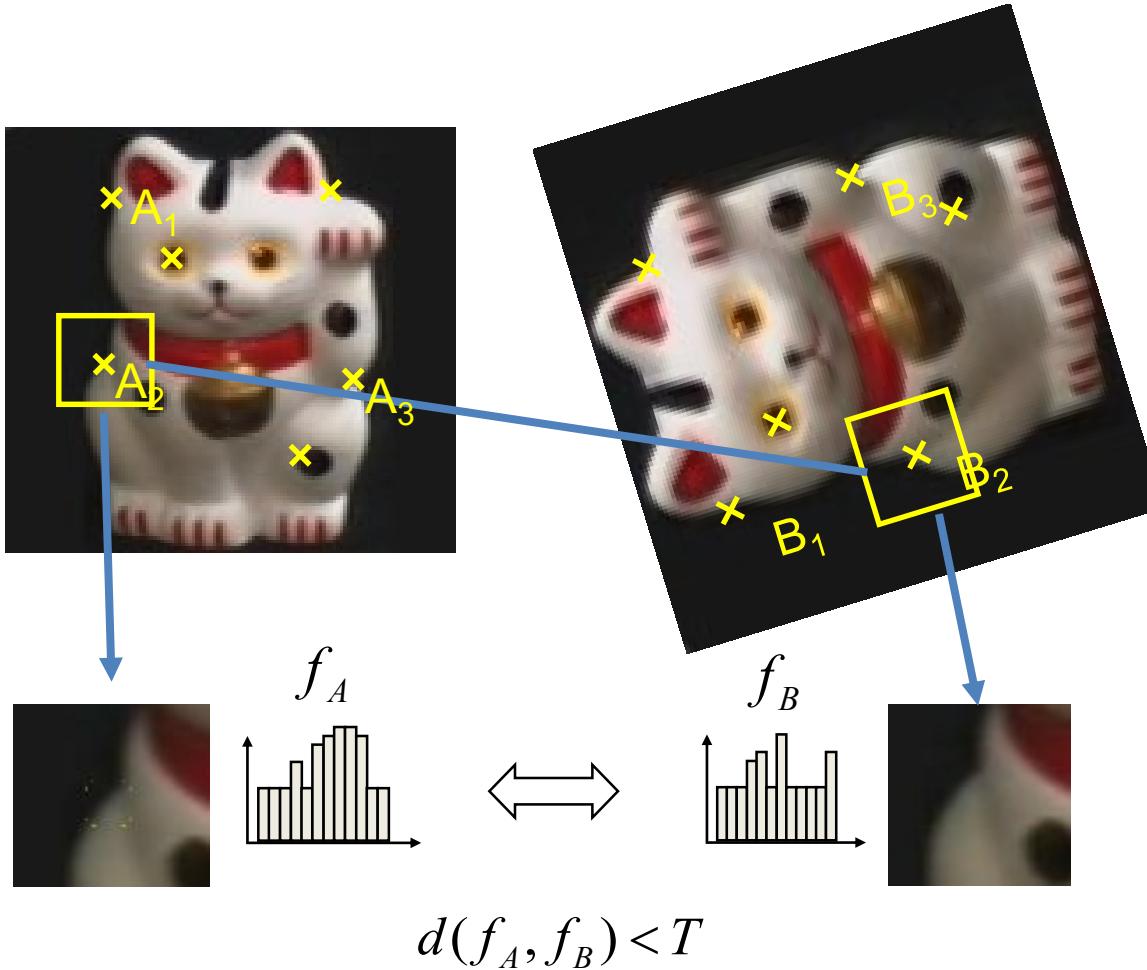
- 2) Description: Extract vector feature descriptor surrounding each interest point



- 3) Matching: Determine correspondence between descriptors in two views



Overview of Keypoint Matching



1. Find a set of distinctive keypoints
2. Define a region around each keypoint
3. Extract and normalize the region content
4. Compute a local descriptor from the normalized region
5. Match local descriptors

What points to choose?



Source: Derek Hoiem

Low-texture region?



Gradients have small magnitude

Edge?



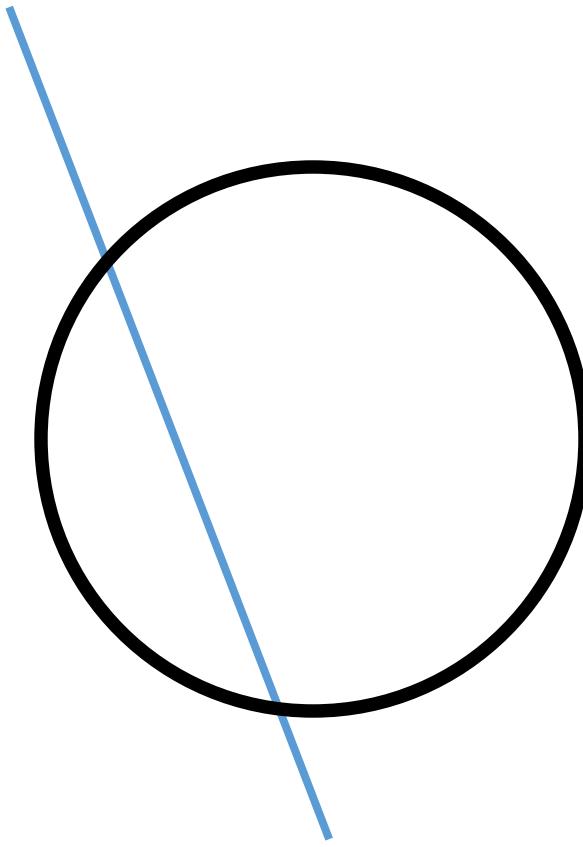
Gradients very large or very small

High-texture region?

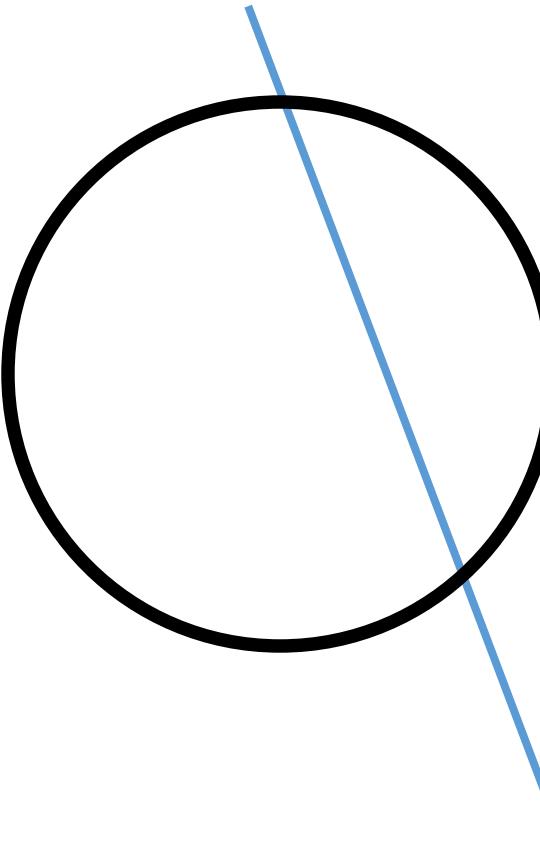


Gradients are different, large magnitudes

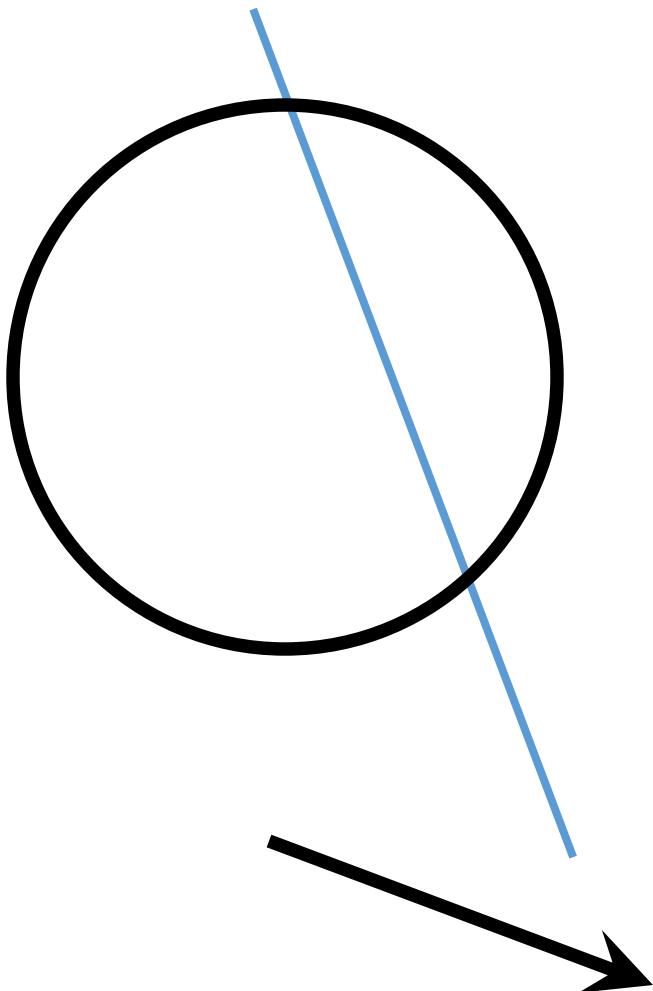
The aperture problem



The aperture problem



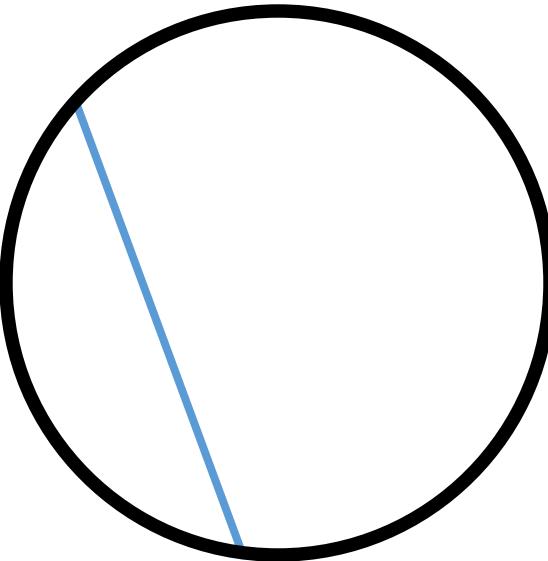
The aperture problem



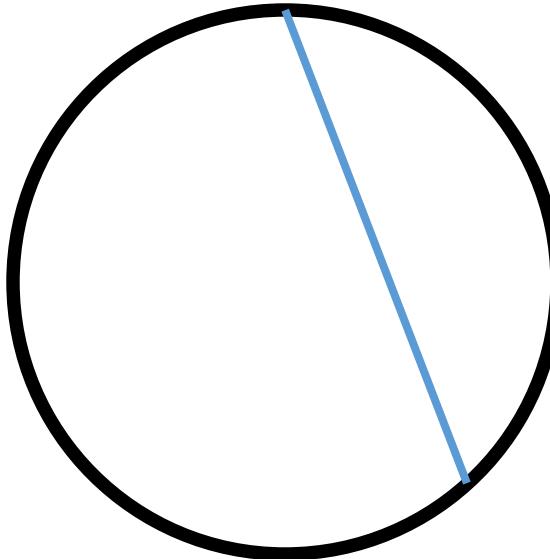
Actual motion

Source: Derek Hoiem

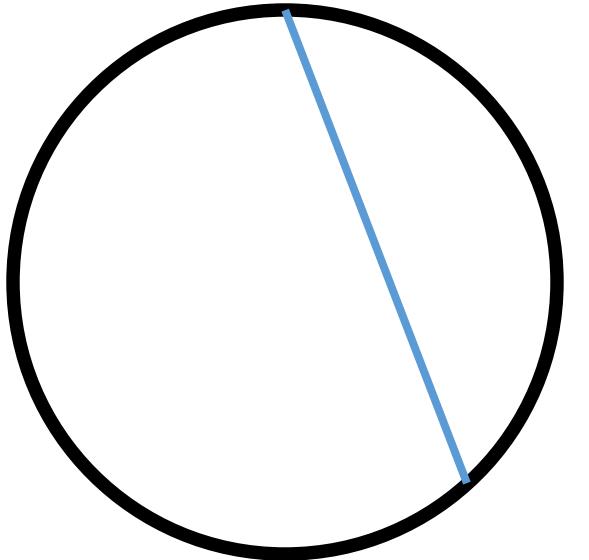
The aperture problem



The aperture problem



The aperture problem



Perceived motion

The barber pole illusion



http://www.opticalillusion.net/wp-content/uploads/2013/07/WedBarb4BB_F8_HQ.mp4?_=1

So, what makes a good feature?



Want uniqueness

Look for image regions that are unusual

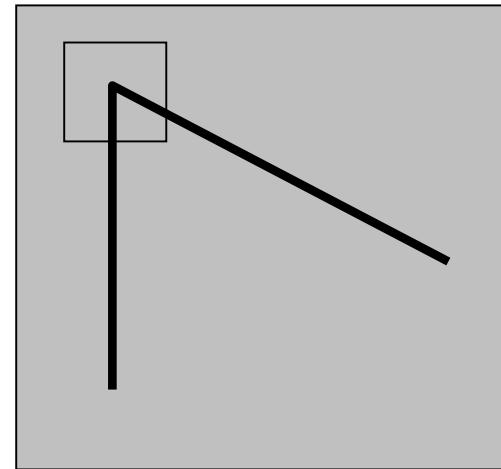
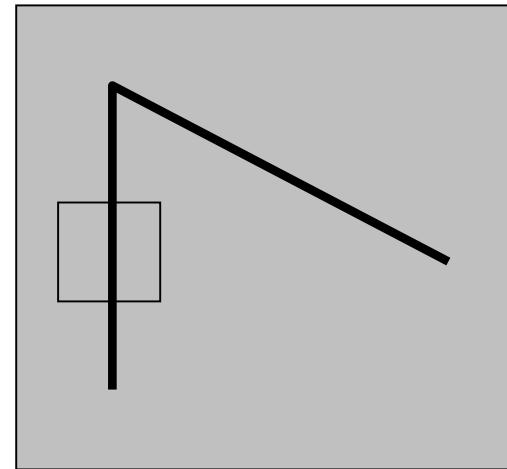
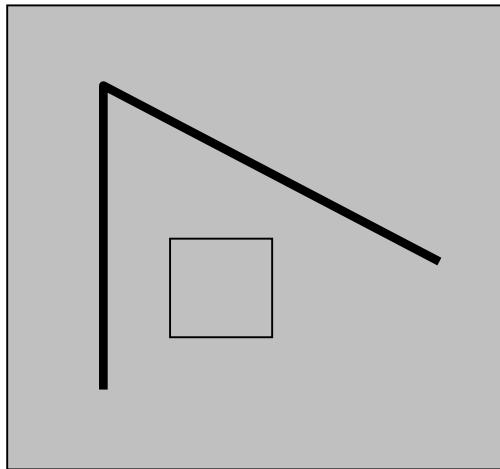
- Lead to unambiguous matches in other images

How to define “unusual”?

Want uniqueness

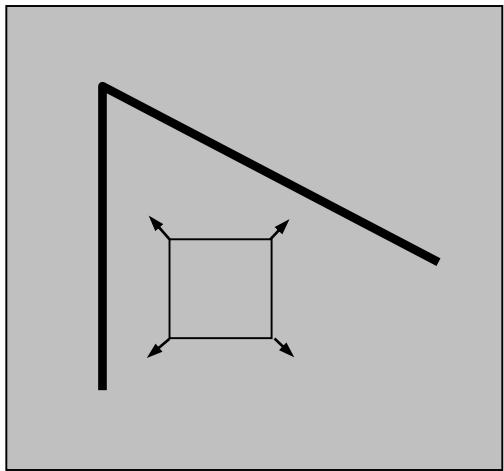
Suppose we only consider a small window of pixels

- What defines whether a feature is a good or bad candidate?

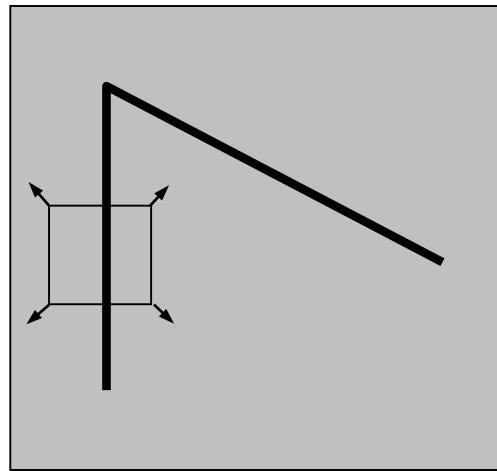


Want uniqueness

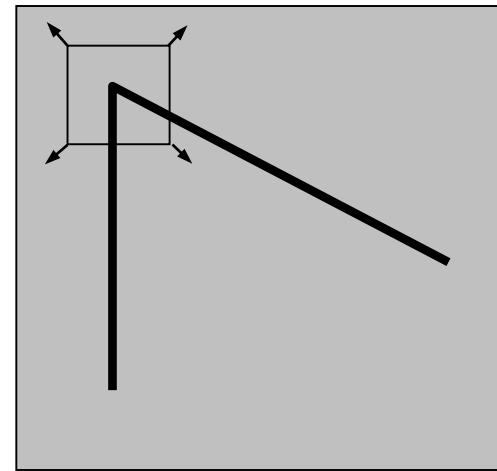
- How does the window change when you shift it?
- Shifting the window in any direction causes a big change



“flat” region:
no change in all
directions



“edge”:
no change along the
edge direction

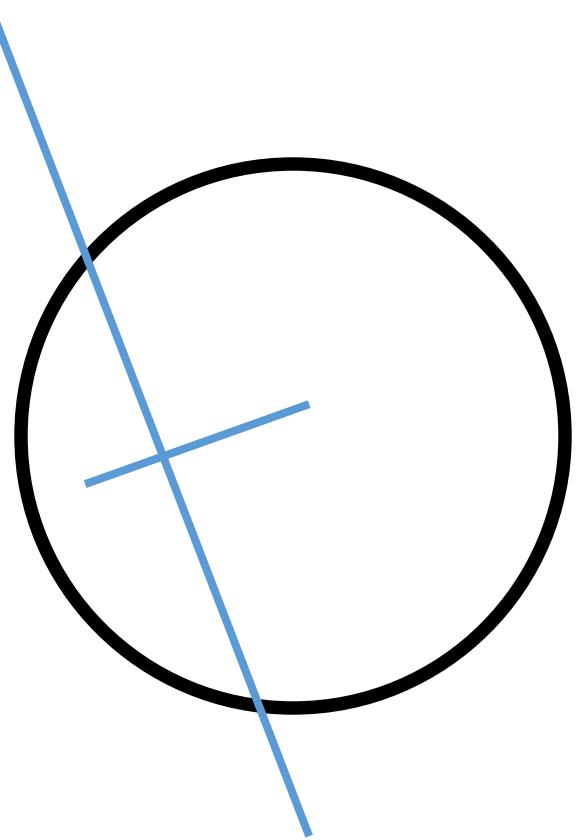


“corner”:
significant change in
all directions

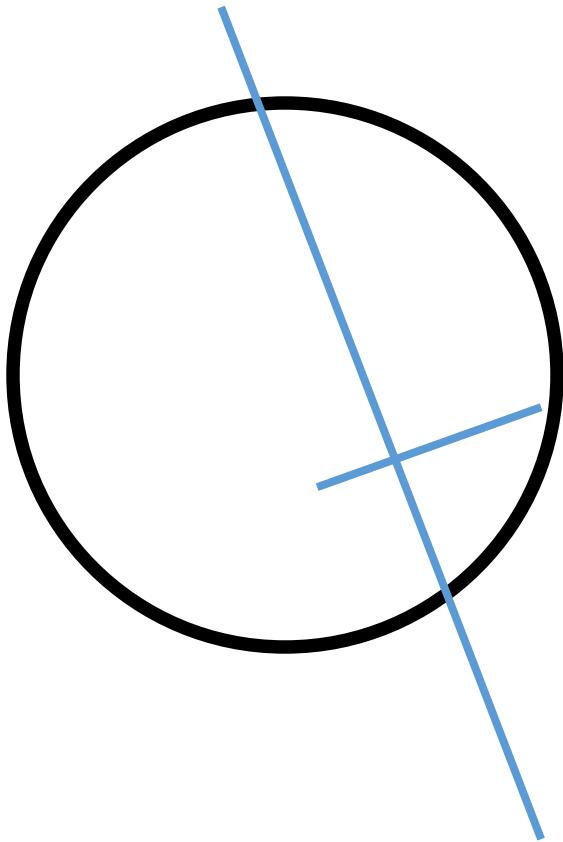
Corners

- Textureless patches are nearly impossible to localize
- Patches with large contrast changes (gradients) are easier to localize
- But straight line segments at a single orientation suffer from the aperture problem, i.e., it is only possible to align the patches along the direction normal to the edge direction
- Gradients in at least two (significantly) different orientations are the easiest, e.g., **corners**

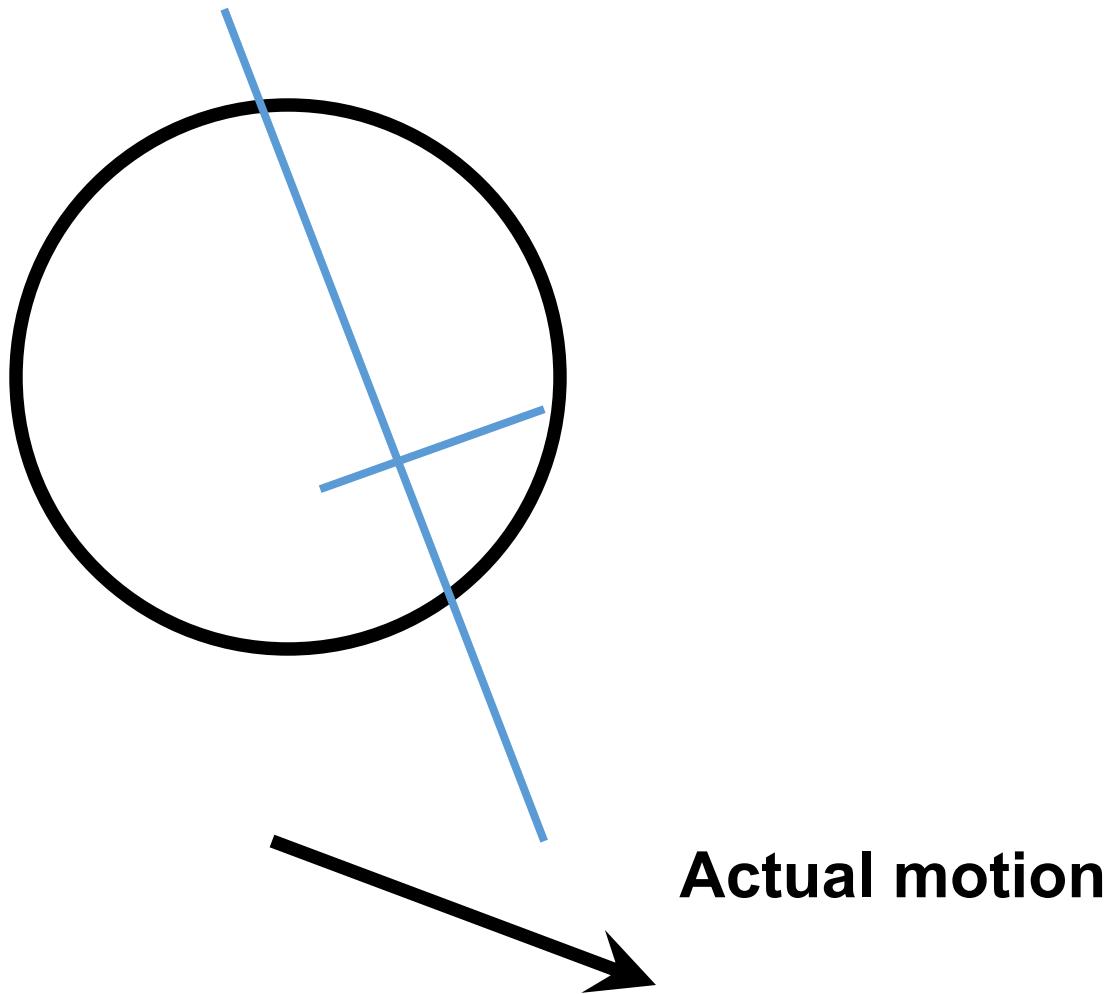
The aperture problem resolved



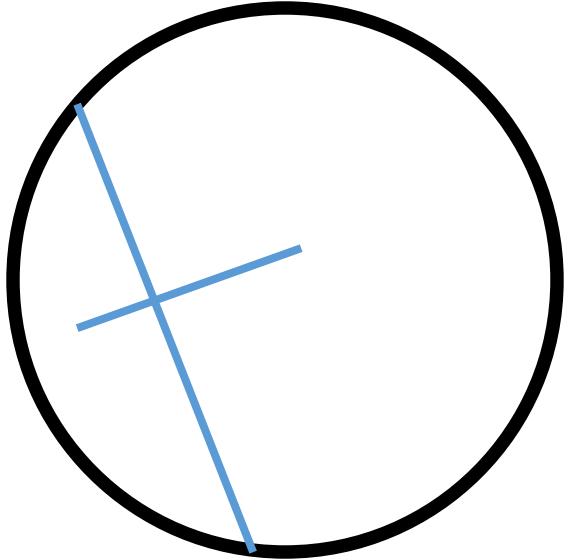
The aperture problem resolved



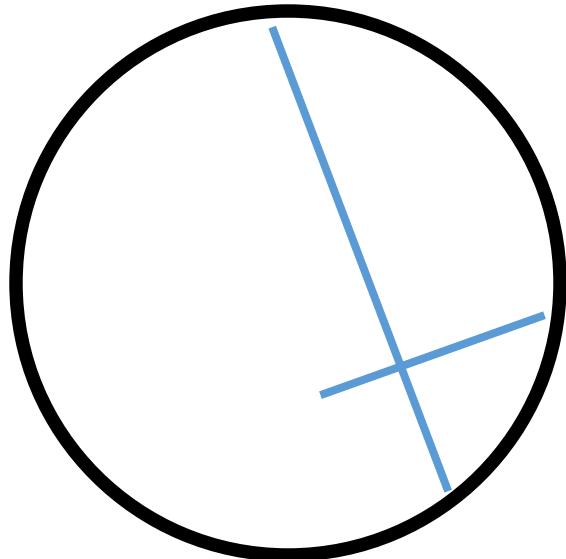
The aperture problem resolved



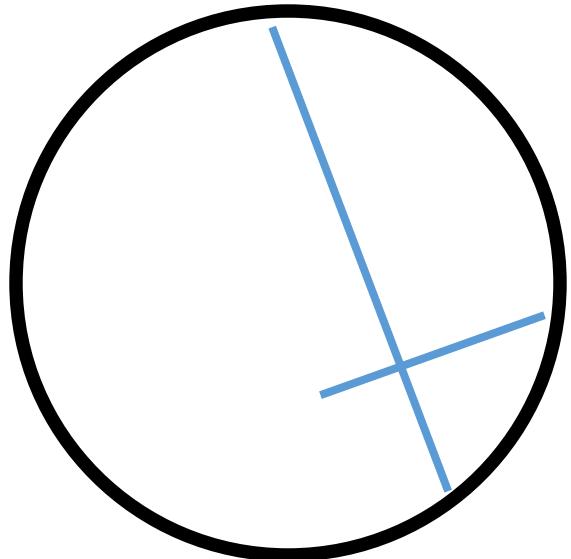
The aperture problem resolved



The aperture problem resolved



The aperture problem resolved

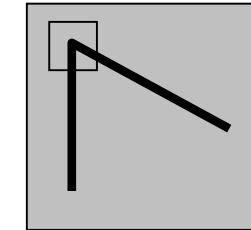
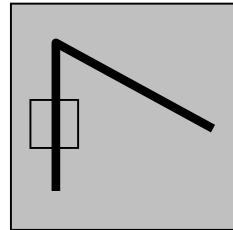
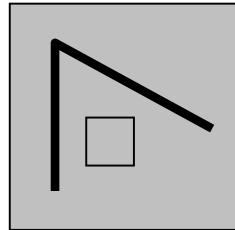


Perceived motion

Harris corner detection

1. Generate a **cornerness score** for each image

window



2. Find points whose surrounding window gave large corner response ($f > \text{threshold}$)
3. Take the points of local maxima, i.e., perform non-maximum suppression

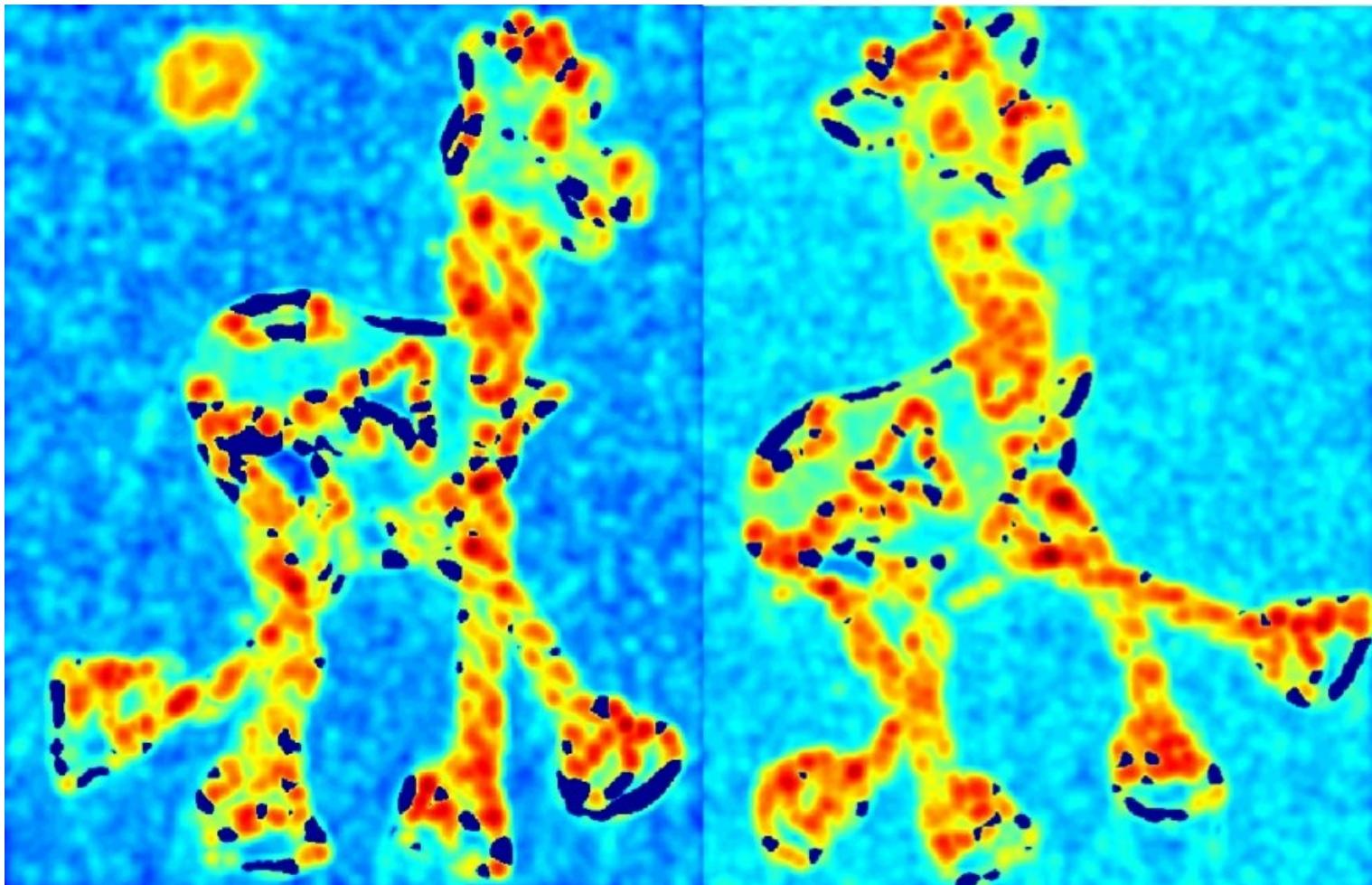
Harris detector steps



Source: James Hays

Harris detector steps

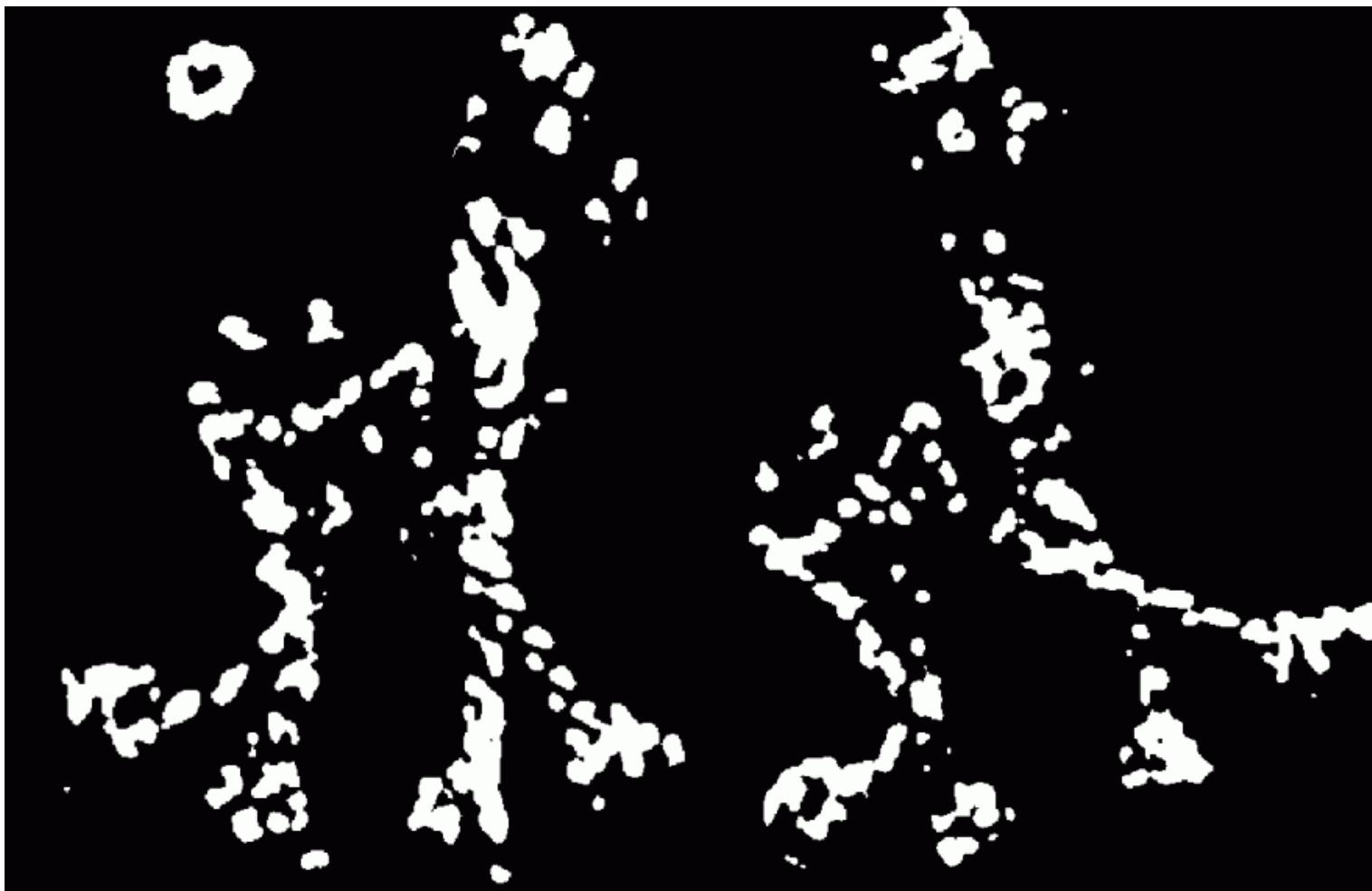
Compute corner response R



Source: James Hays

Harris detector steps

Find points with large corner response: $R > \text{threshold}$



Source: James Hays

Harris detector steps

Take only the points of local maxima of R



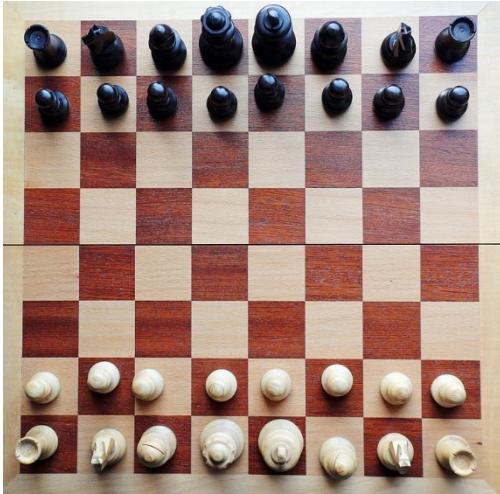
Source: James Hays

Harris detector steps



Source: James Hays

Harris corner detection: esempi



Harris corner detection: esempi

```
from matplotlib import pyplot as plt
import urllib.request

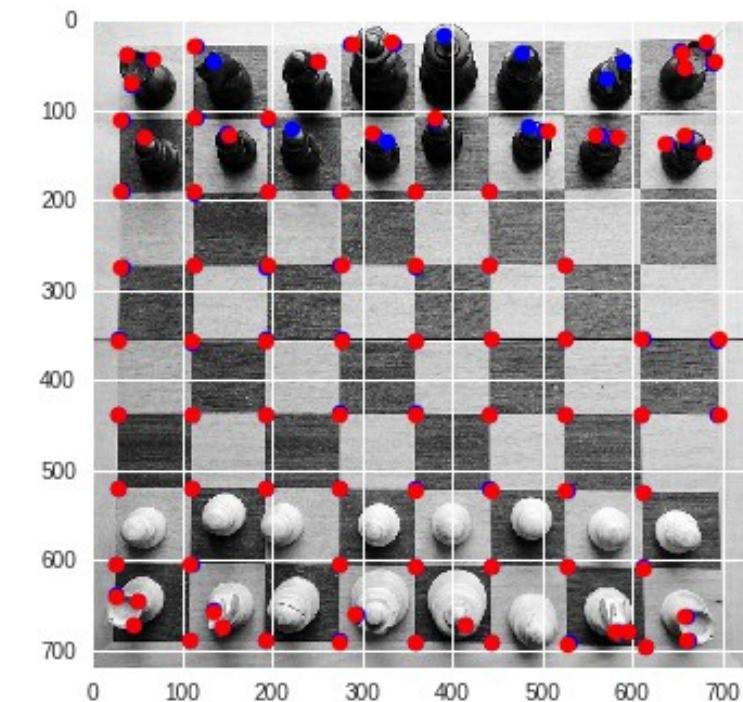
from skimage.io import imread
from skimage.color import rgb2gray
from skimage.feature import corner_harris, corner_subpix, corner_peaks

url = "https://dbloisi.github.io/corsi/images/chessboard-1.jpg"

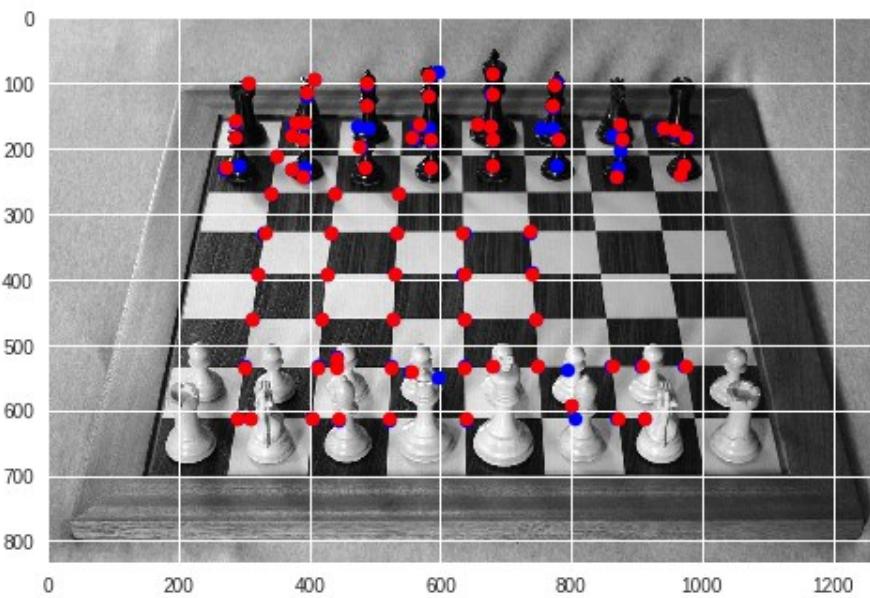
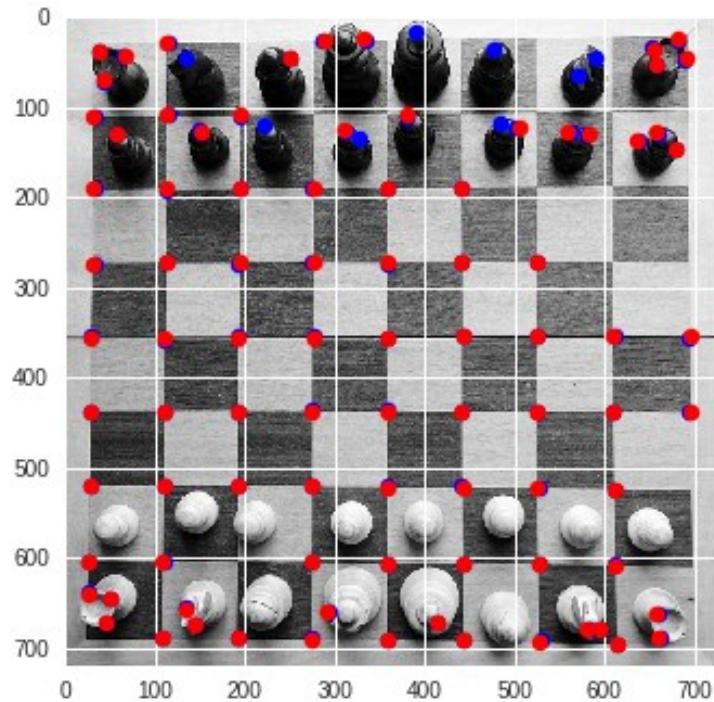
image = imread(urllib.request.urlopen(url))
image = rgb2gray(image)

coords = corner_peaks(corner_harris(image), min_distance=10)
coords_subpix = corner_subpix(image, coords, window_size=13)

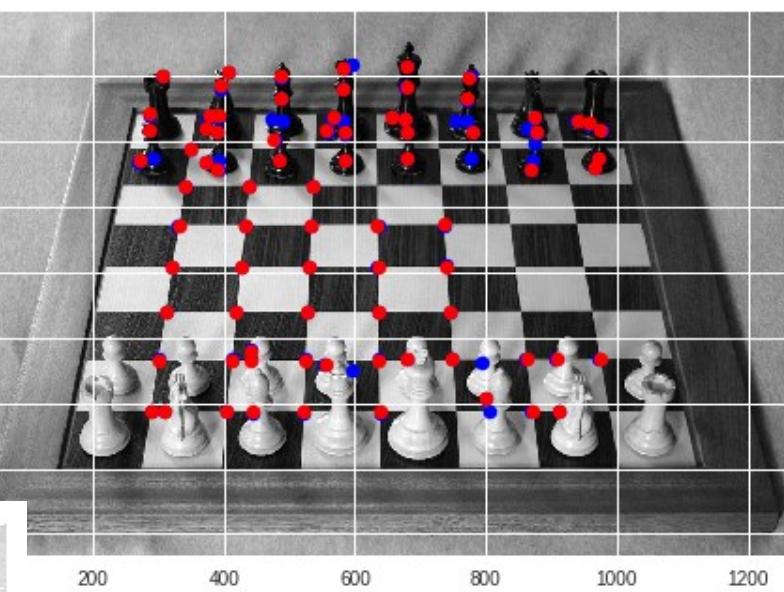
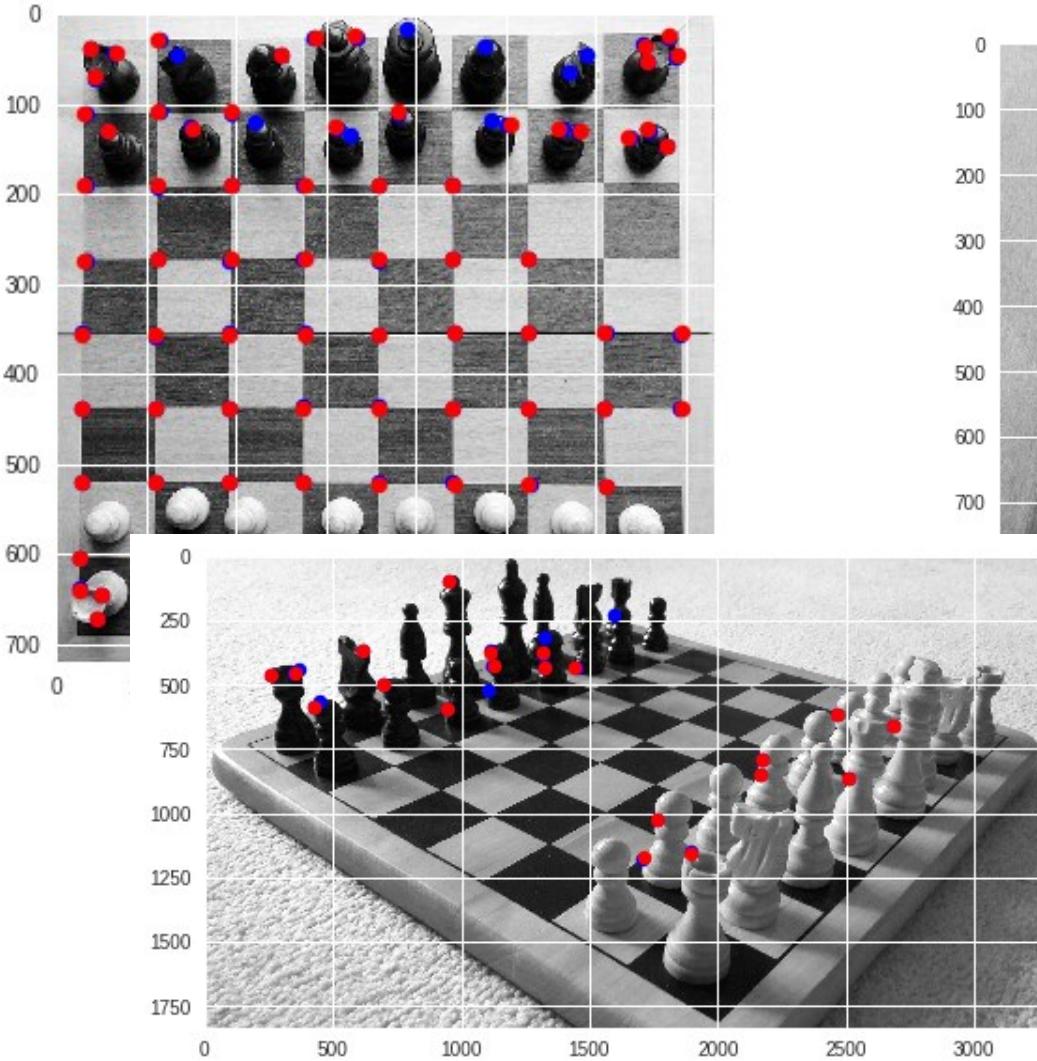
fig, ax = plt.subplots()
ax.imshow(image, interpolation='nearest', cmap=plt.cm.gray)
ax.plot(coords[:, 1], coords[:, 0], '.b', markersize=15)
ax.plot(coords_subpix[:, 1], coords_subpix[:, 0], '.r', markersize=15)
plt.show()
```



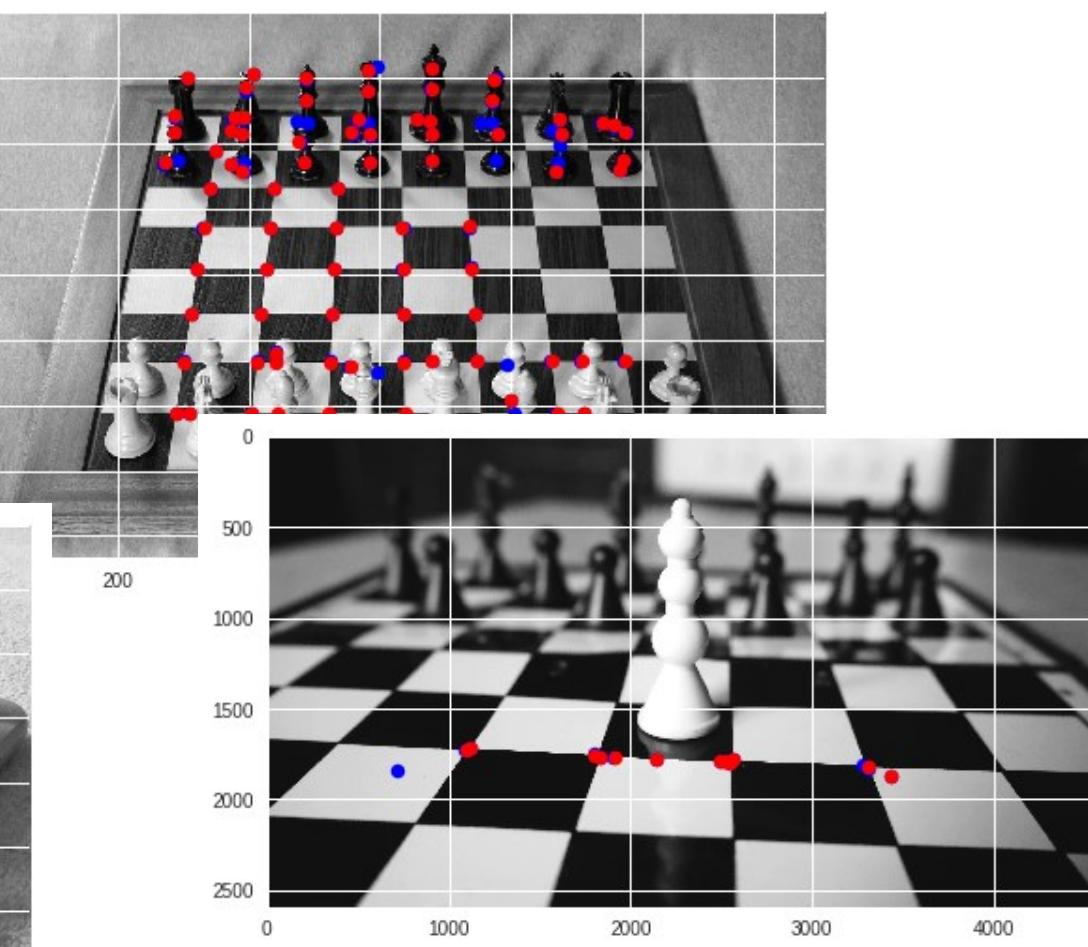
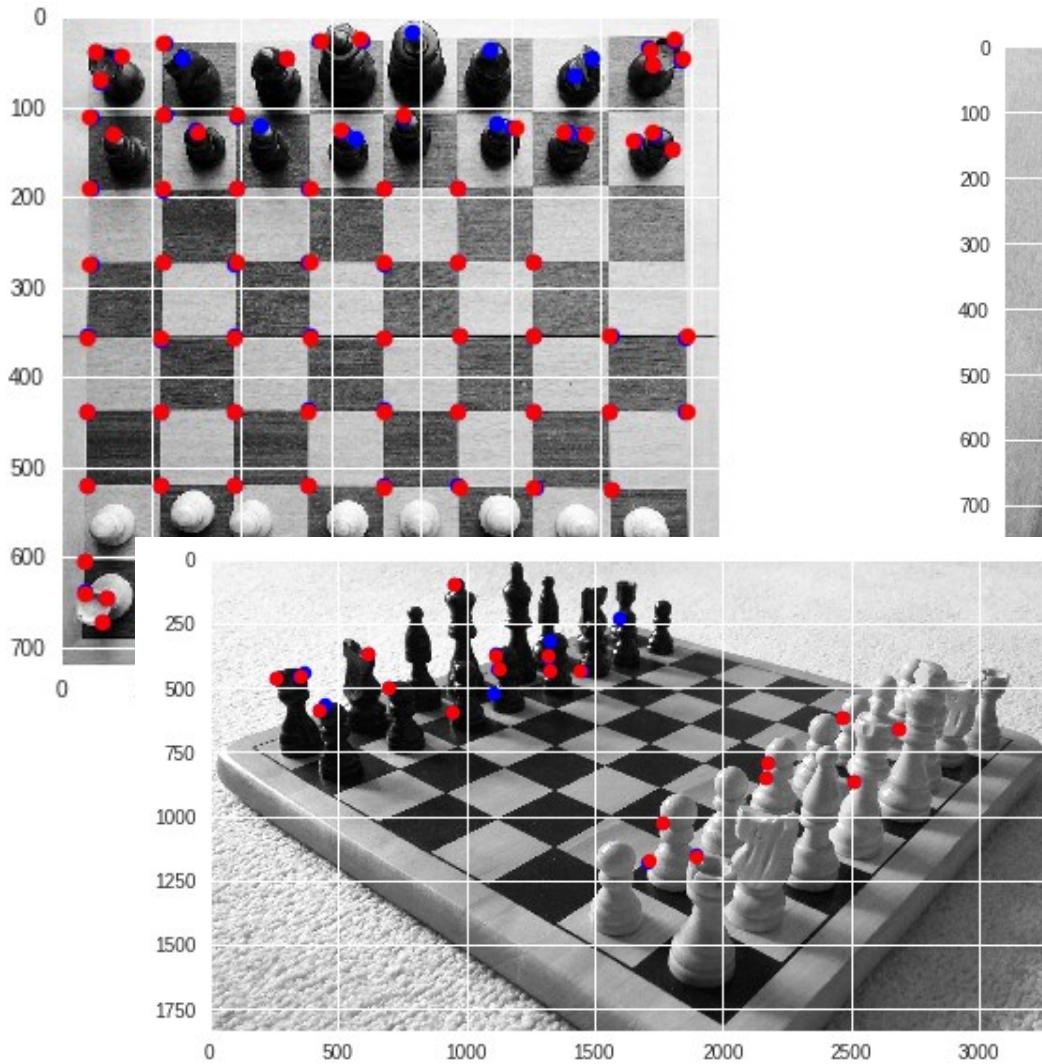
Harris corner detection: esempi



Harris corner detection: esempi



Harris corner detection: esempi

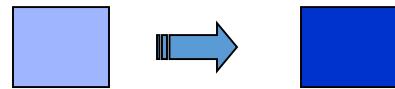


Invariance and covariance

We want corner locations to be *invariant* to photometric transformations and *covariant* to geometric transformations

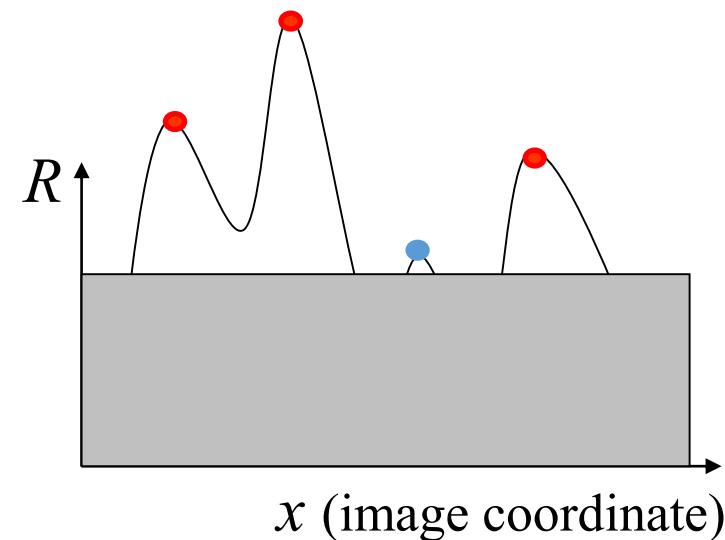
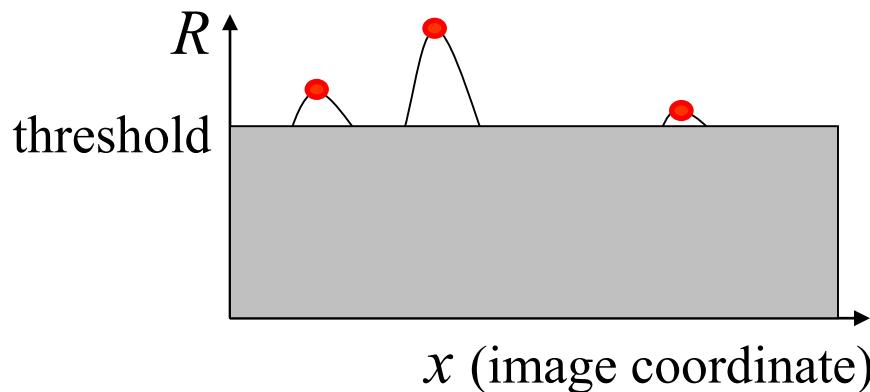
- **Invariance:** image is transformed and corner locations do not change
- **Covariance:** if we have two transformed versions of the same image, features should be detected in corresponding locations

Affine intensity change



$$I \rightarrow a I + b$$

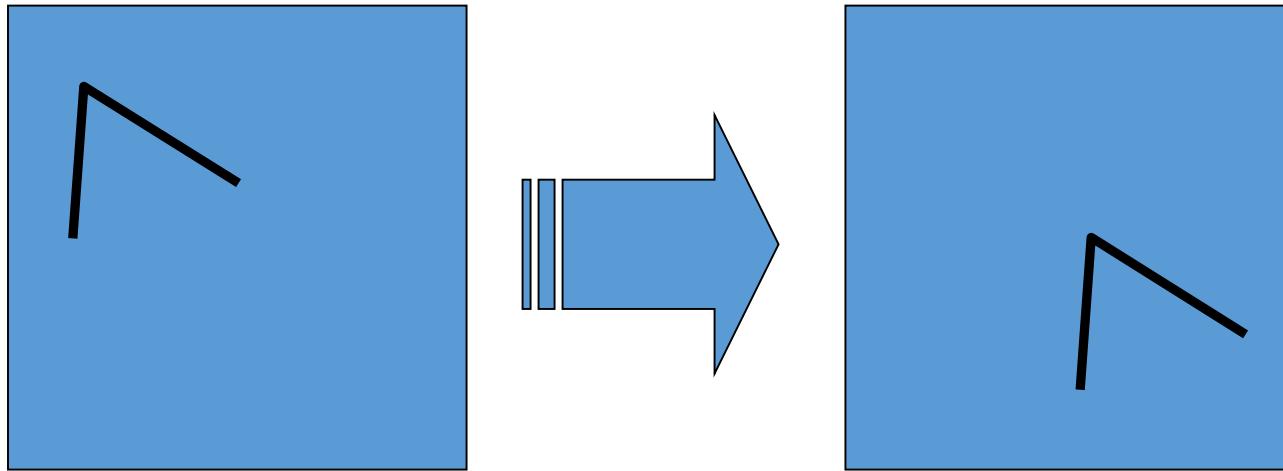
- Only derivatives are used \rightarrow invariance to intensity shift $I \rightarrow I + b$
- Intensity scaling: $I \rightarrow a I$



Partially invariant to affine intensity change

Source: James Hays

Translation

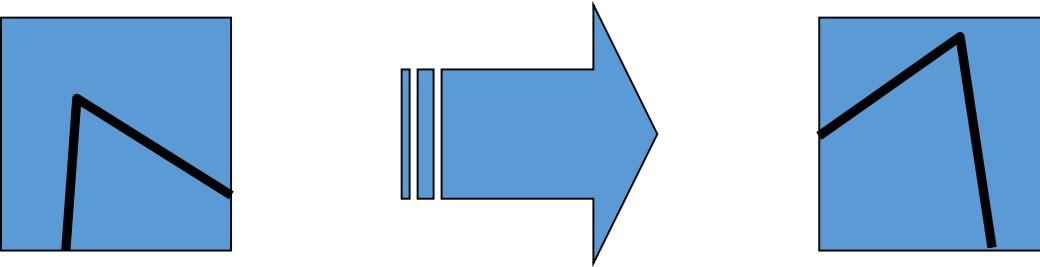


Derivatives and window function are shift-invariant

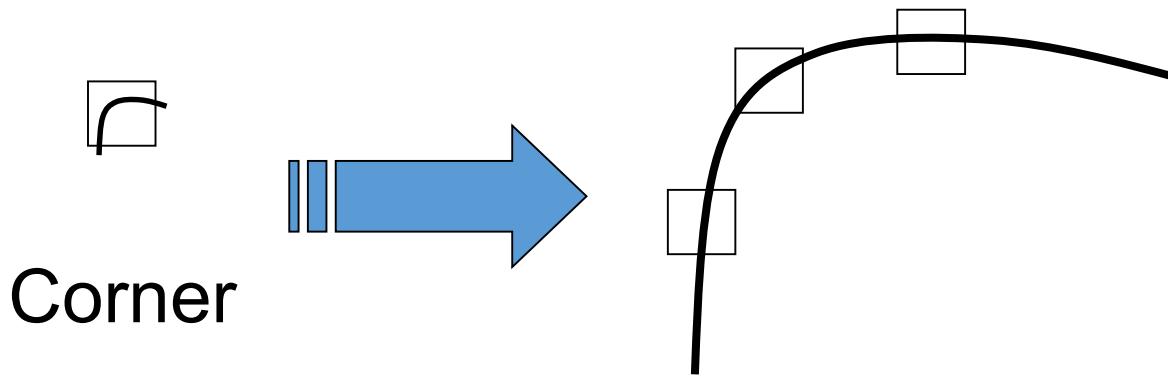
Corner location is covariant w.r.t. translation

Source: James Hays

Rotation and Scaling



Corner location is covariant w.r.t. rotation



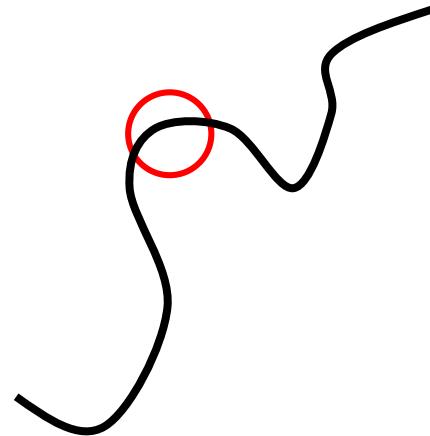
All points will be
classified as
edges

Corner location is not covariant to scaling!

Source: James Hays

Scale invariant detection

Suppose you're looking for corners

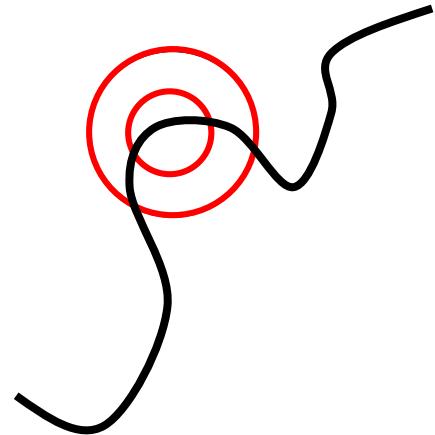


Key idea: find scale that gives local maximum of f

- in both position and scale
- One definition of f : the Harris operator

Scale invariant detection

Suppose you're looking for corners

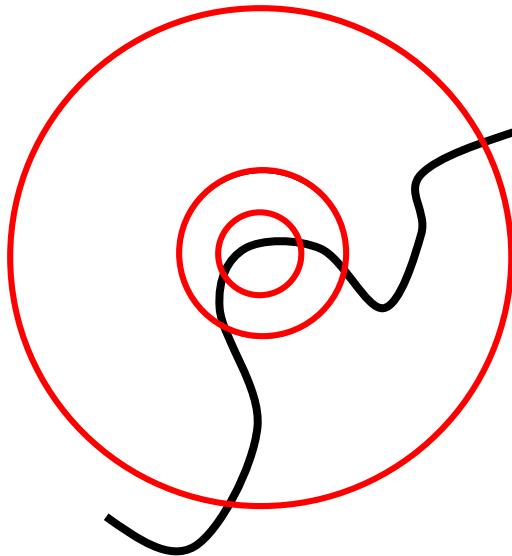


Key idea: find scale that gives local maximum of f

- in both position and scale
- One definition of f : the Harris operator

Scale invariant detection

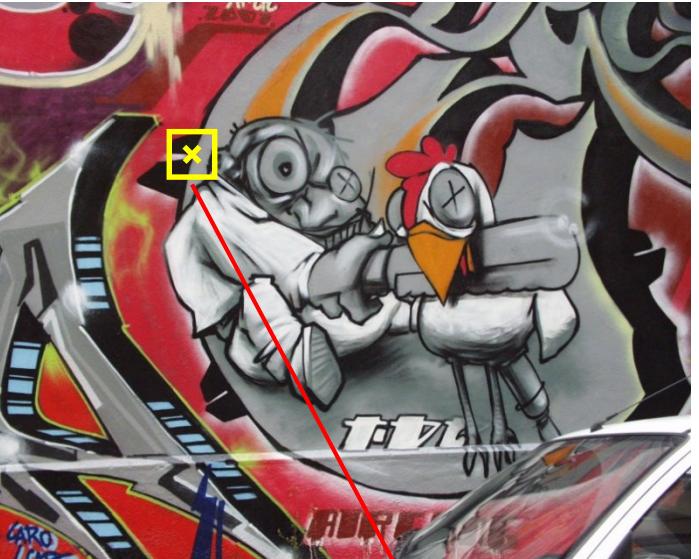
Suppose you're looking for corners



Key idea: find scale that gives local maximum of f

- in both position and scale
- One definition of f : the Harris operator

Scale invariance

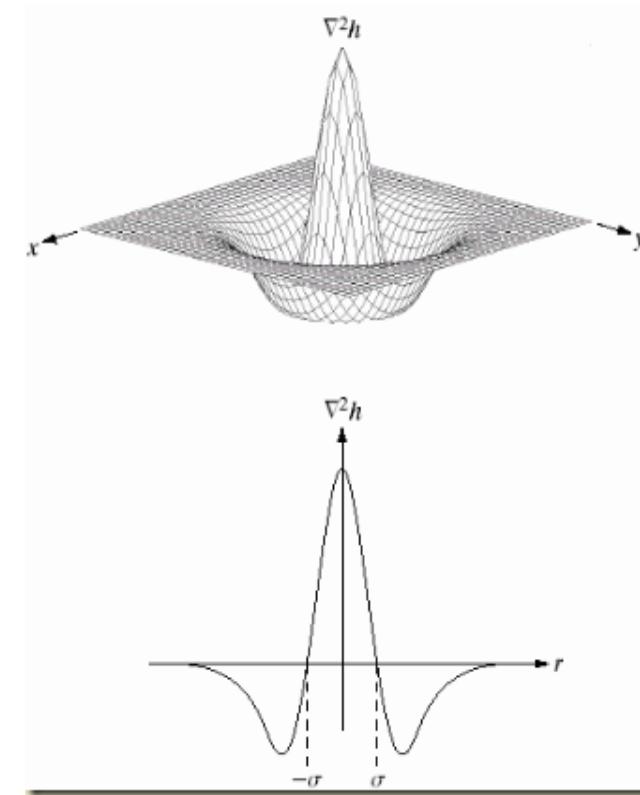
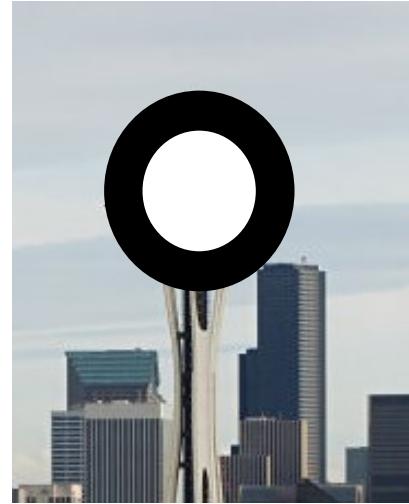
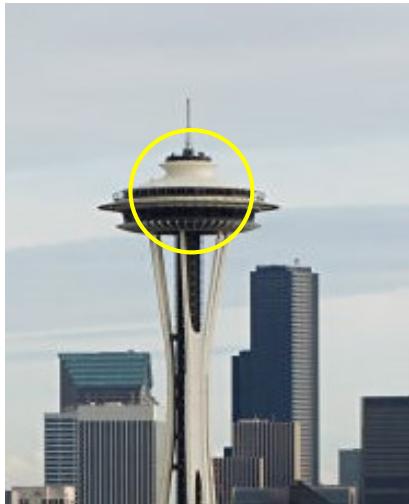


$$f(I_{i_1 \dots i_m}(x, \sigma)) = f(I_{i_1 \dots i_m}(x', \sigma'))$$

How can we independently select interest points in each image, such that the detections are repeatable across different scales?

Differences between inside and outside

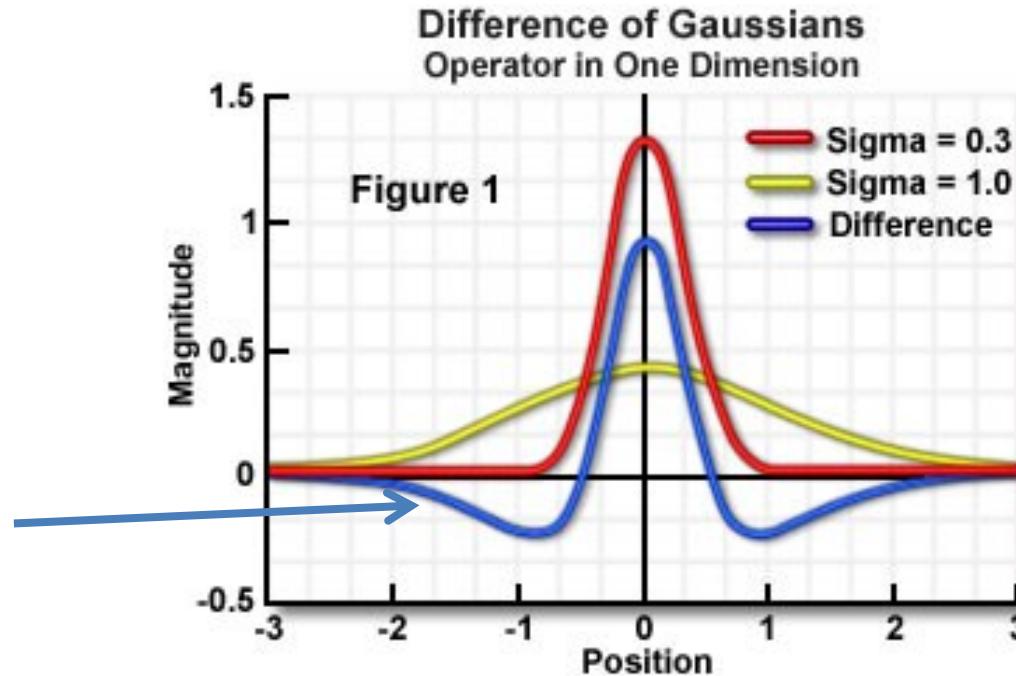
We can use a Laplacian function



Source: Linda Shapiro

Difference-of-Gaussian (DoG)

In practice, the Laplacian is approximated using a Difference of Gaussian (DoG)



Gaussian is invariant to scale change, i.e., $f * \mathcal{G}_\sigma * \mathcal{G}_{\sigma'} = f * \mathcal{G}_{\sigma''}$ and has several other nice properties [Lindeberg, 1994]

Difference-of-Gaussian (DoG)

G1



-

G2



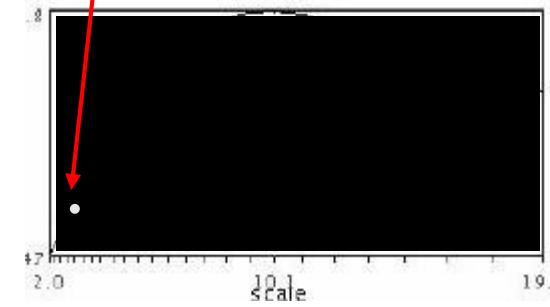
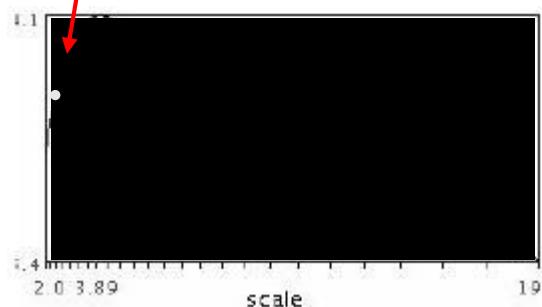
=

DoG



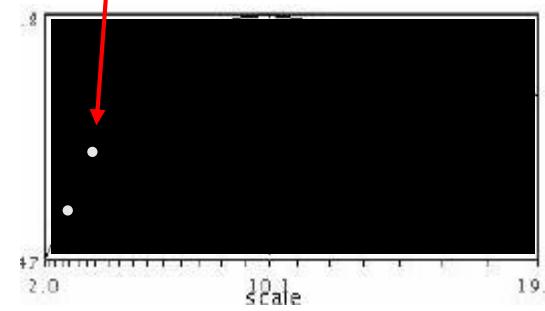
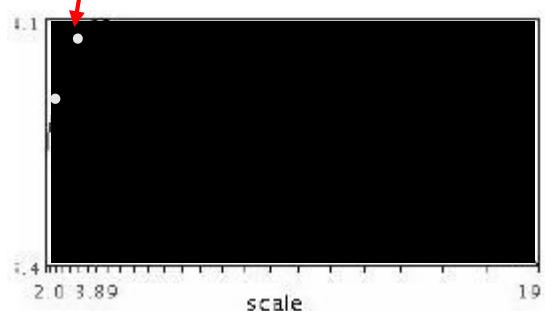
Automatic scale selection

- Function responses for increasing scale (scale signature)



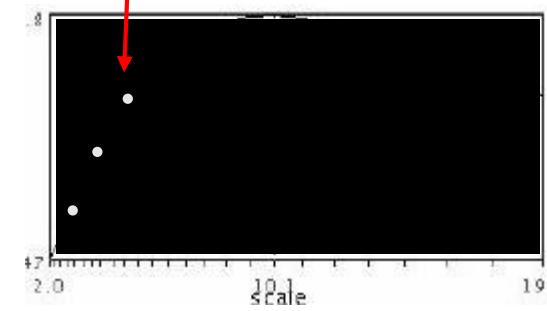
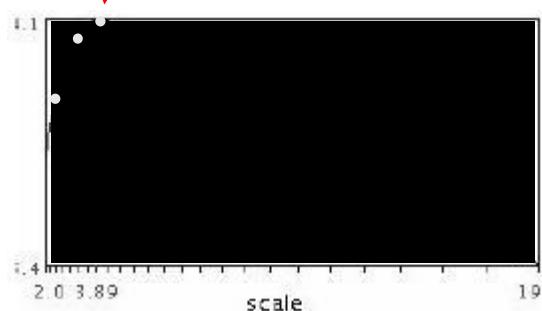
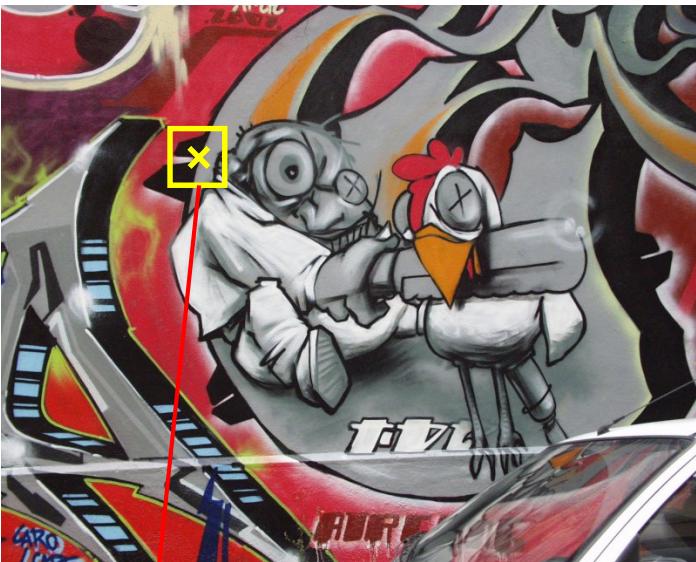
Automatic scale selection

- Function responses for increasing scale (scale signature)



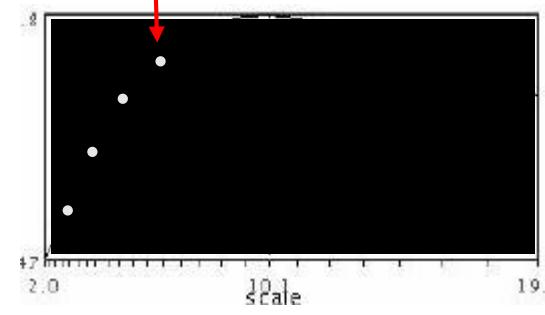
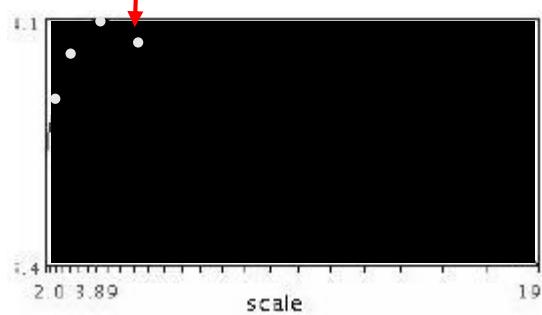
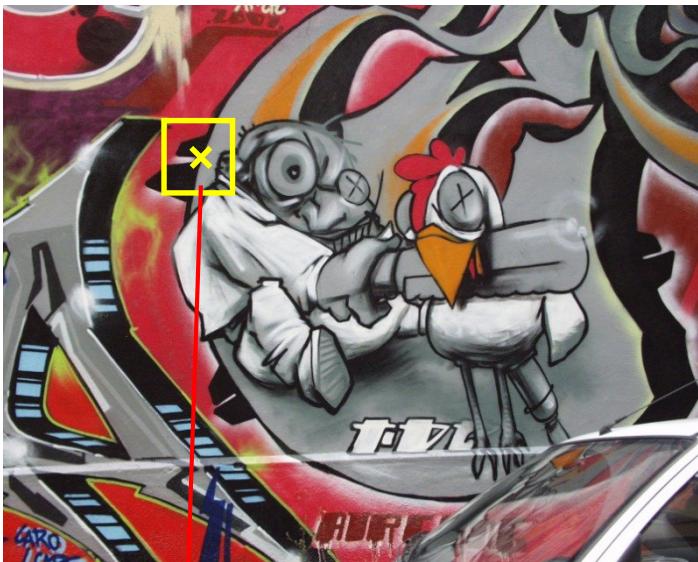
Automatic scale selection

- Function responses for increasing scale (scale signature)



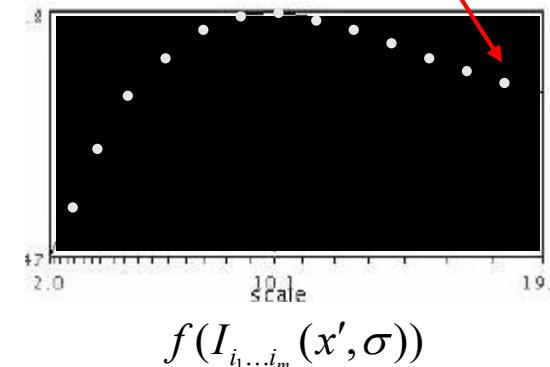
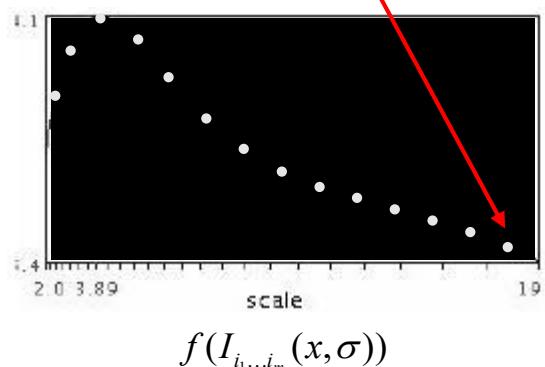
Automatic scale selection

- Function responses for increasing scale (scale signature)



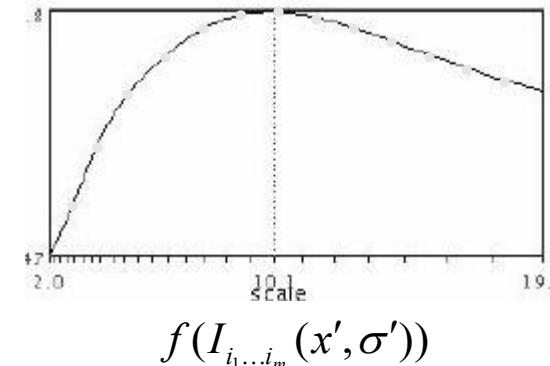
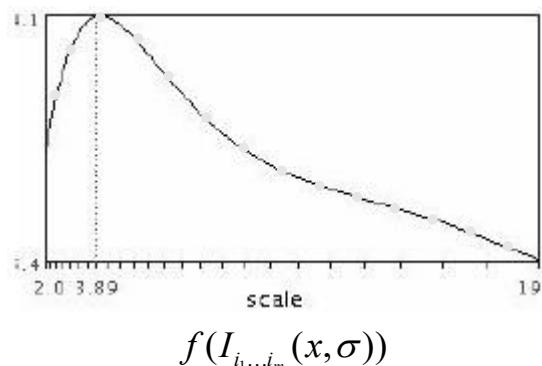
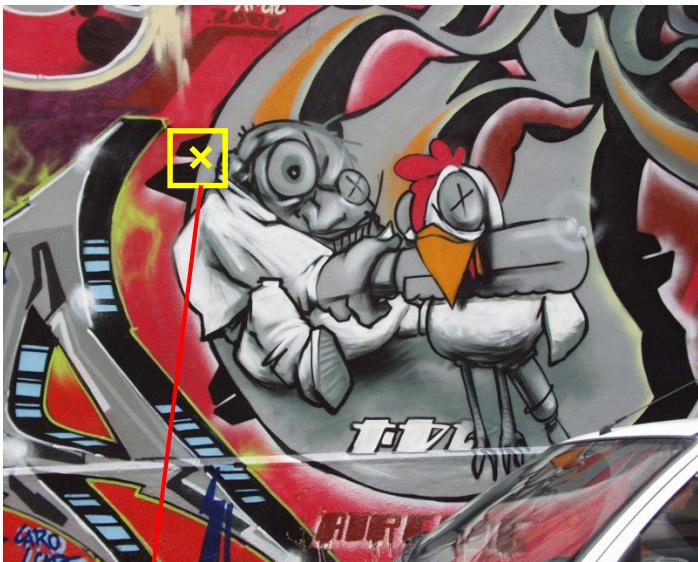
Automatic scale selection

- Function responses for increasing scale (scale signature)



Automatic scale selection

- Function responses for increasing scale (scale signature)



Implementation

- Instead of computing f for larger and larger windows, we can implement using a fixed window size with a Gaussian pyramid



(sometimes need to create in-between
levels, e.g. a $\frac{3}{4}$ -size image)

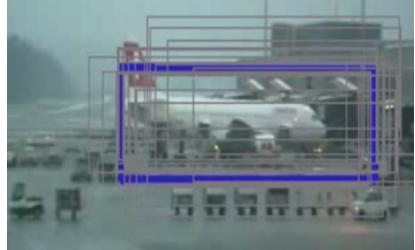
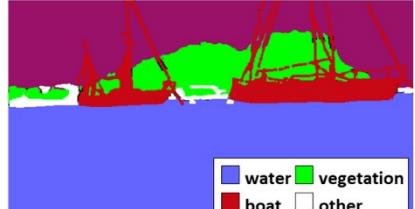
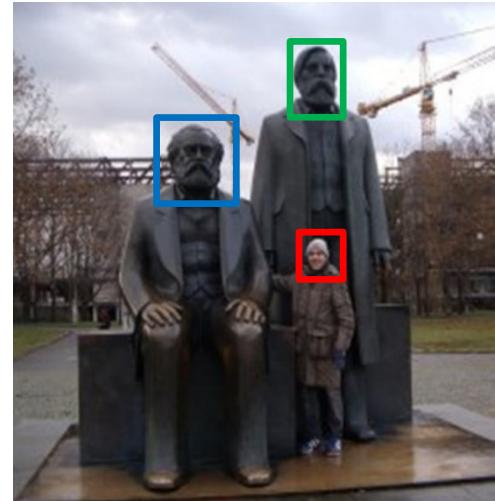
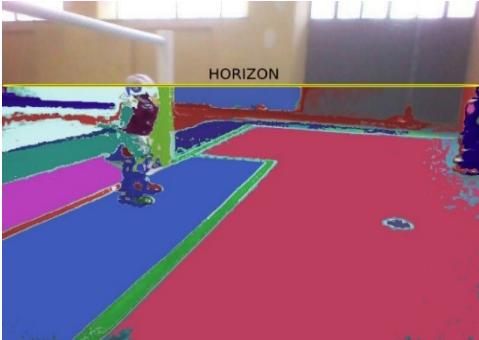
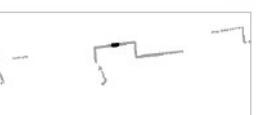


UNIVERSITÀ DEGLI STUDI DELLA BASILICATA

Corso di Sistemi Informativi
A.A. 2019/2020

Features

Aprile 2020



Docente
Domenico Daniele Bloisi