

Networked Life: Project

28/04/2023

Project Goal-

- Introduce new algorithms and techniques to provide custom recommendations to users based on what other users liked
- Learn some basic skills and gain practice experience in machine learning, and enrich your resume

Main Tasks

Part 1 Linear regression on Netflix dataset

Expand on the homework Q4 (i.e., linear regression) by reusing your written code previously, applying it to the Netflix training dataset

Part 2 Restricted Boltzmann Machines (RMB)

Develop a classic neural network model to predict a user's rating: restricted Boltzmann machines (RBM)

Part 3 Extensions to the RBM model

Build extensions to the RBM model using some hints we give you and any information you can find online

Part 1

Linear regression on Netflix dataset

Expand on the homework Q4 (i.e., linear regression) by reusing your written code previously, applying it to the Netflix training dataset

Dataset

- Two datasets in the folder (code):
 - training.csv: imported to a matrix by getTrainingData function in projectLib file.
 - validation.csv: imported to a matrix by getValidationData function in projectLib file.

	t	raining	set	validation set	test set
e.g.	movie ID	user ID	rating ID		hidden
	5	4	3		
·	:	:	:		

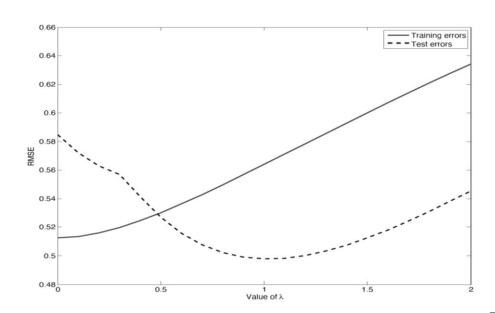
- Finish the parameter estimation param function to compute the baseline estimator for the training set, without regularization
- Finish the *predict* function to compute the predicted rating of every (movie, user) pair of the training set
- Then you can compute the RMSE to compare the two

$$\{r_{ui}\} \longrightarrow \text{Predictor } (b) \longrightarrow \hat{r}_{uj} \quad \forall u, j$$

* Regularize this model so that it does not overfit, by adding a penalty to your biases. You should now complete the *param_reg* function.

$$\min_{\{b_u,b_i\}} ||Ab - c||_2^2 + \lambda ||b||_2^2$$

Find the optimal λ



Review

Baseline Predictor

$$\hat{r}_{ui} = \bar{r} + b_u + b_i$$

$$b^* = (A^T A)^{-1} A^T c$$

$$b^* = (A^T A + \lambda I)^{-1} A^T c$$

Linear Regression

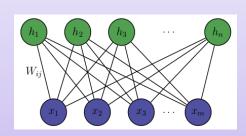
Neighborhood Predictor

$$d_{AB} = \frac{r_A^T r_B}{||r_A||_2 ||r_B||_2}$$

$$\hat{r}_{ui}^{N} = (\bar{r} + b_u + b_i) + \frac{\sum_{j \in \mathcal{L}_i} d_{ij} \tilde{r}_{uj}}{\sum_{j \in \mathcal{L}_i} |d_{ij}|}$$

Interactions among movies and users

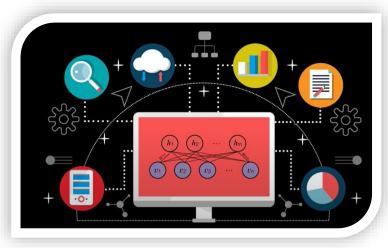
Restricted Boltzmann Machines (RBM)



undirected graphical model

Part 2

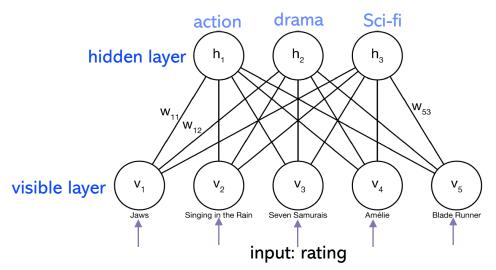
Restricted Boltzmann Machines (RBM)



rbm.py, mainRBM.py

RMB model

- Visible layer V
 - Each node is corresponding to a movie
 - Receives input (e.g., user's ratings)
- Hidden layer H
 - Each node represents a feature (e.g., whether user likes action movie or not)



 v_i, h_i are binary, i.e. $\{0,1\}$

✓ Find the best weights W

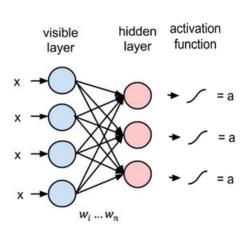
to represent our data

When visible layer receives input, the input is transformed to the hidden layer and passed through an activation function to produce the node's output:

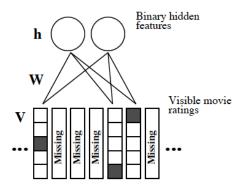
$$\mathbb{P}(h_j = 1 | \mathbf{v}) = \sigma \left(\sum_{i \in V} v_i W_{ij} \right), \text{ where } \sigma(x) = \frac{1}{1 + e^{-x}}.$$

the probability of feature j to be active.

In the *rbm.py* file, complete the function *sig*.



- RBM requires the input data to be binary form. To adapt to the requirement, we encode each rating as a binary vector
- The rating from a user can be one of the five options, $K = \{1, 2, 3, 4, 5\}$
- If a user gives a rating 3, that piece of data will be encoded by the vector (0, 0, 1, 0, 0)

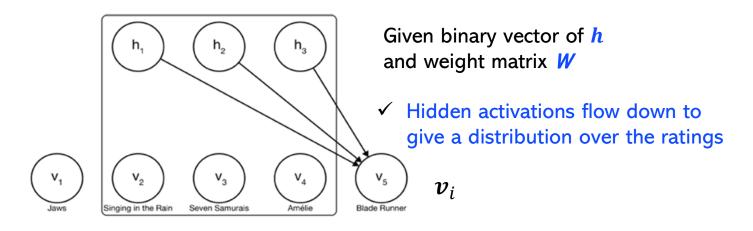


From visible states to the hidden ones:

$$\mathbb{P}(h_j = 1 | \mathbf{v}) = \sigma \left(\sum_{k \in K} \sum_{i \in V} v_i^k W_{ij}^k \right) .$$

Write a function to propagate the visible input (binary vectors of ratings) to the hidden layer, in visibleToHiddenVec

 After we compute the probability of features (hidden nodes), we then compute the predicted results of the user from hidden nodes to visible nodes



 Implement the hiddenToVisible function, taking as input a binary vector of hidden units and the edge weights.

Implement the function getPredictedDistribution to get the predicted distribution over the ratings for a movie

$$\mathbb{P}(v_i^k = 1 | \mathbf{h}) = softmax\Big(\sum_{j \in J} h_j W_{ij}^k\Big), \text{ where } softmax(x_k) = \frac{e^{x_k}}{\sum_{l \in K} e^{x_l}}$$

e.g.
$$P_i = (0.1, 0.2, 0.4, 0.3, 0)$$
, the probability that rating = 3 is 0.4 $K = \{1, 2, 3, 4, 5\}$

- ✓ Output is a distribution over all the possible K states, i.e., the probability that each of the K binary variables takes the value 1
- ✓ We need to transform the probability distribution of user's rating at different scores
 to a standard rating

- Implement the two functions predictRatingMax and predictRatingExp, which implement the two options below
 - e.g., A user's probabilities for a movie i at 5 different score options:

$$P_i = (0.1, 0.2, 0.4, 0.3, 0)$$
, the probability that rating = 3 is 0.4

- $K = \{1, 2, 3, 4, 5\}$
- \checkmark Predict the rating with the highest probability. In the above example, the prediction =3.
- ✓ Predict the rating as weighted average of probabilities

$$prediction = \sum_{k \in K} p_i^k k$$
.

In the above example:

$$prediction = 0.1 \times 1 + 0.2 \times 2 + 0.4 \times 3 + 0.3 \times 4 + 0 \times 5 = 2.9$$

Find weights RBM $\{r_{ui}\}$ predictor ψ $\{\hat{r}_{ui}\}$

• Find the weights that maximize the probability that our model would generate the data it has been trained on, which is called log-likelihood $\max \log P(\mathbf{v})$

$$\frac{\partial \log p(\mathbf{v})}{\partial w_{ij}} = \langle v_i h_j \rangle_{data} - \langle v_i h_j \rangle_{model}$$

- Use a gradient ascent method.
 - Start from a random weight
 - ullet Update weights by adding the gradient $\,
 abla W^k_{i,j}$

$$W \leftarrow W + \epsilon \nabla W_{i,j}^k$$

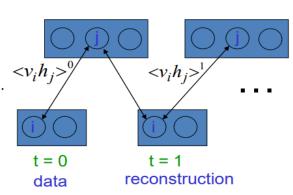
Gradient ascent method

Learning

- We start with the data \mathbf{v} , consisting by all the K-elements vectors v_i , $i \in M_u$, of all the movies M_u that a particular user u has rated. This part is implemented by the function getV in the rbm.py file.
- Compute $\mathbb{P}(h_i = 1|\mathbf{v})$ with visibleToHiddenVec.
- Call positive gradient $(PG)_{i,j,k} = \mathbb{P}(h_j = 1|\mathbf{v}) \cdot v_i^k$ (computed by probProduct).

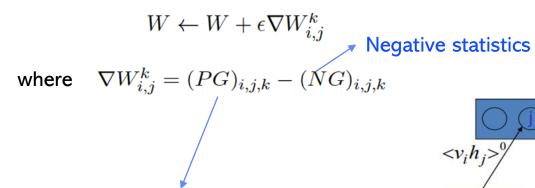
Unlearning:

- Sample the states of the hidden units according to $\mathbb{P}(h_j = 1 | \mathbf{v})$.
- Use hiddenToVisible to compute "negative" data $\overline{\mathbf{v}}$.
- Essentially repeat the steps of the Learning part, this time with "negative" data, i.e compute $\mathbb{P}(h_j = 1|\overline{\mathbf{v}})$ and call "negative" gradient $(NG)_{i,j,k} = \mathbb{P}(h_j = 1|\overline{\mathbf{v}}) \cdot \overline{v}_i^k$.

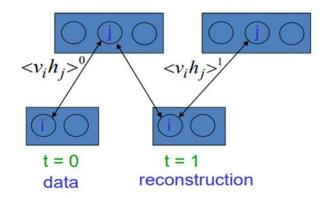


Gradient ascent method

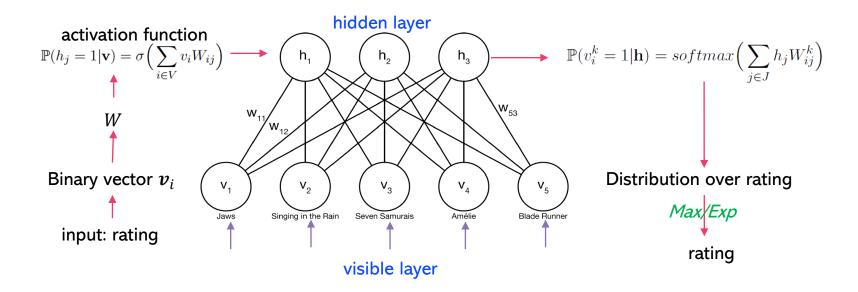
Synthesis: Update only the weights for the movies that the user has rated.



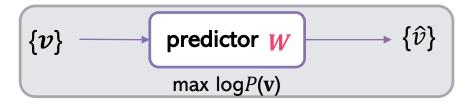
Positive statistics for the connection between visible node *i* and hidden node *j*



RMB model-



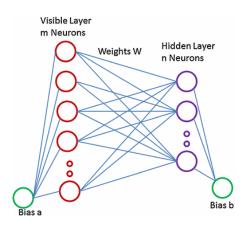
Gradient ascent method



Part 3

Some extensions by online references

- Momentum
- Adaptive learning rates
- Early stopping
- Regularization
- Mini Batch
- Biases
- Neighbourhood Method

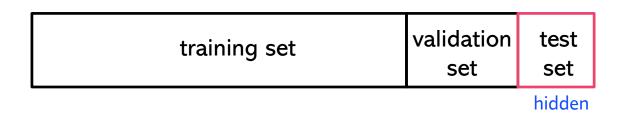


-Your algorithms

- Two algorithms
 - ✓ Linear regression (λ)
 - \checkmark RBM (F, ϵ)
- It is important to train your model on the training set, and then see how well it performs on previously unseen data contained in the validation set
- You can change the hyperparameters to make the algorithms more performant

Test data

- Test your program on test data (*test.csv*)
- When you produce the rating file (for all movies and for all users),
 name it in the following format: <Group ID>_v<version number>.txt
- After receiving your file, we will compute the RMSE obtained on the test set and give you its value



Bonus

- Submit result once every week from week 10 to week 13 (Based on RBM, not Regression)
- At the end of each week, the current best RMSE (over all previous weeks) will be broadcasted to the class, for you to know which is the current goal to beat. Also, each week, the team with the best outstanding RMSE over the test set will get a bonus of 5 points
- At most 10-bonus score for each group

Round	Dates		
1	Monday, April 10 - Sunday, April 16 (11:59 PM)		
2	Monday, April 17 - Sunday, April 23 (11:59 PM)		
3	Monday, April 24 - Sunday, April 30 (11:59 PM)		
4	Monday, May 1 - Sunday, May 7 (11:59 PM)		

Submission and Grading

- Project Group: Same with homework group.
- Submission: Source code (best RMSE) + Report (Deadline: May 10)
- Grading:
 - (25%) Part 1: Linear regression (linearRegression.py, projectLib.py)
 - (25%) Part 2: Basic RBM (rbm.py, mainRBM.py)
 - (25%) Part 3: Extensions of the RBM
 - (25%) Part 4: Report
 - 5 bonus points for the group submitting the best results each week
 - Up to 10 bonus points for each group

cProfile

- Provide deterministic profiling of Python programs. A profile is a set of statistics that describes how often and for how long various parts of the program executed. These statistics can be formatted into reports via the pstats module.
- cProfile.run("mainRBM()", "profilingStats")

```
import pstats
from pstats import SortKey
p_0412 = pstats.Stats("profilingStats_0412_getallusersratings")
p_0412.strip_dirs().sort_stats(SortKey.CUMULATIVE).print_stats(50)
```

```
42263453 function calls (42263447 primitive calls) in 68.967 seconds
Ordered by: cumulative time
List reduced from 164 to 50 due to restriction <50>
ncalls tottime percall cumtime percall filename:lineno(function)
                                    69.057 {built-in method builtins.exec}
          0.000
                   0.000
                           69.057
                                    69.057 <string>:1(<module>)
                           69.057
          0.008
                   0.008
                                    69.049 mainRBM.py:10(mainRBM)
          0.373
                   0.373
                           69.049
                   0.000
                          49.353
                                    8.226 rbm.py:196(predict)
     6
          0.000
                                    8.226 rbm.py:199(<listcomp>)
          0.168
                   0.028
                          49.353
                                     0.000 rbm.py:184(predictMovieForUser)
                   0.000
                          49.185
218130
          2.799
                                     0.000 rbm.py:143(getPredictedDistribution)
                           44.412
218130
          0.203
                   0.000
                                     0.000 rbm.py:59(visibleToHiddenVecWithBias)
                           40.482
222130
         15.309
                   0.000
```

- ncalls: number of calls
- tottime: total time spent in given function (excluding time made in calls to sub-functions)
- cumtime: cumulative time spent in this and all subfunctions

Numba

- Accelerate Python functions by translating them to optimized machine code.
- Especially good for loops and Numpy calculations.
- Easy to use. Just apply one of the Numba decorators to your Python function, and Numba does the rest.

 You can apply it to all functions in the project. But you may need to handle a few bugs and exceptions (datatypes...)

```
from numba import jit

@jit(nopython=True)
def softmax(x):
    # Numerically stable softmax function
    e_x = np.exp(x - np.max(x))
    return e_x / e_x.sum()
```

Thanks!

Do you have any questions?