

# FunTAL: Reasonably Mixing a Functional Language with Assembly

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Daniel Patterson,\* Jamie Perconti,\*  
Christos Dimoulas,<sup>†</sup> Amal Ahmed\*

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\* Northeastern University, <sup>†</sup> Harvard University

# Mixed language programs

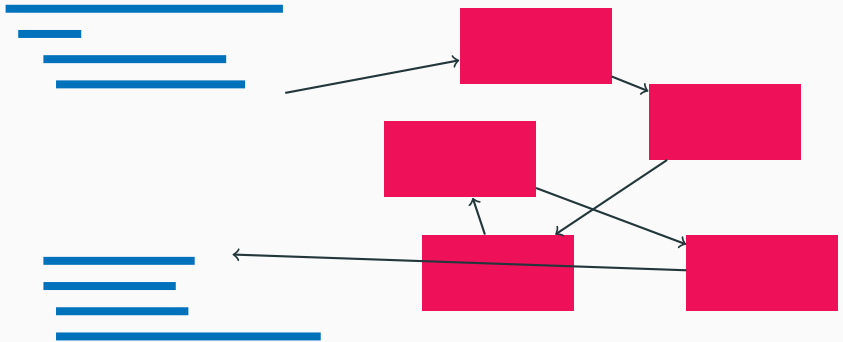
## Functional program



# Mixed language programs

Functional program

Inline assembly



# Questions we want to answer

How to safely mix assembly with high-level code?

How to reason about equivalence of mixed programs?

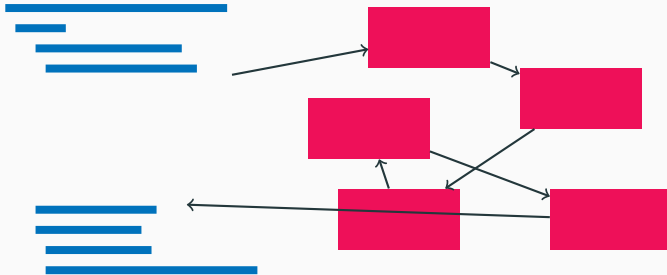
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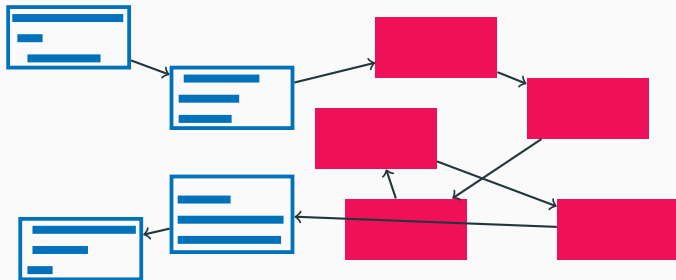
# Prior approaches to mixing

**Option 1:** Translate high-level code into continuation-passing style to match assembly control-flow.



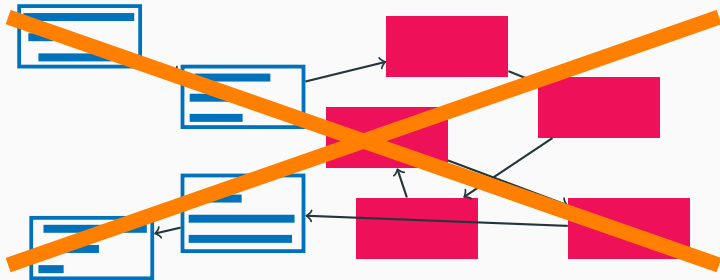
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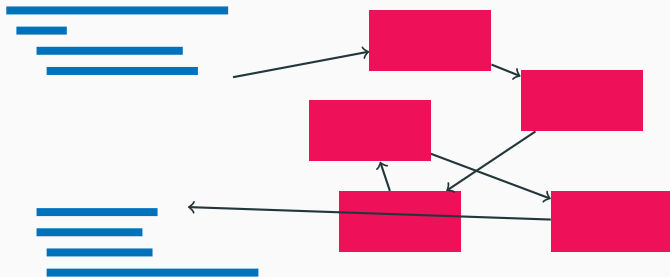
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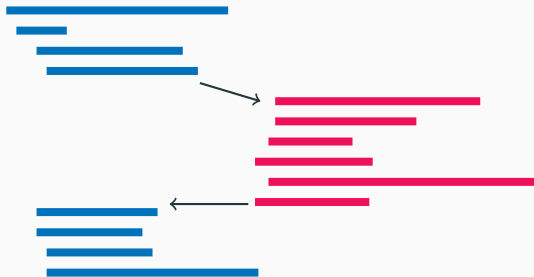
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**Option 2:** Impose high-level call-stack control-flow onto assembly.



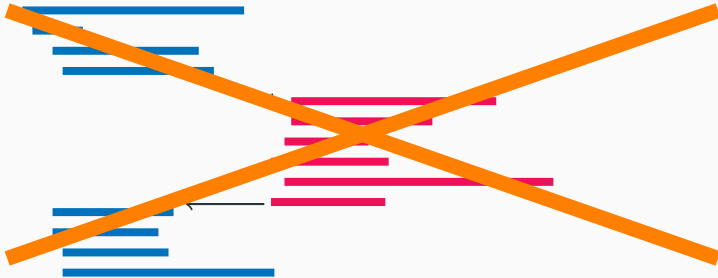
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We do this via a novel notion of a **return marker**, which allows us to define the notion of an assembly **component**.

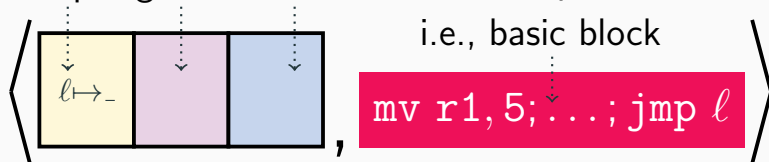
## Fun: Functional language

- Simply typed lambda calculus (STLC)
- with (iso-)recursive types

# TAL: Typed Assembly Language

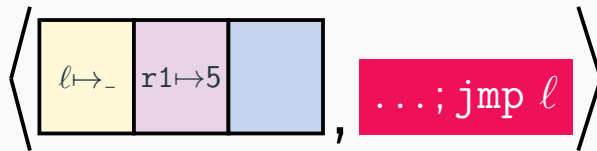
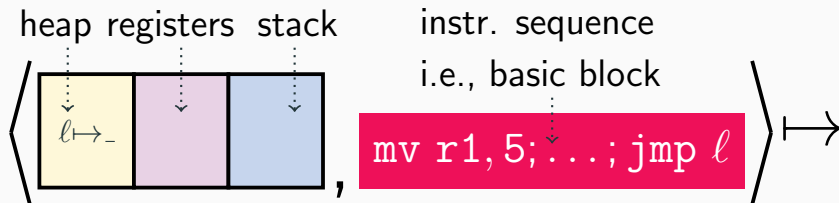
[Morrisett, Crary, Glew, Walker '98]

heap registers stack



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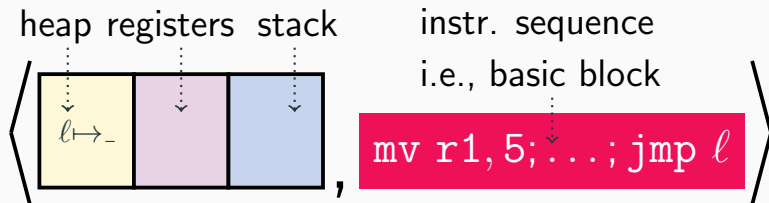
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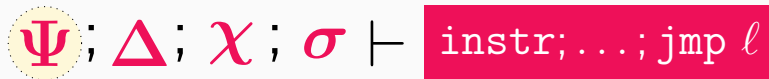
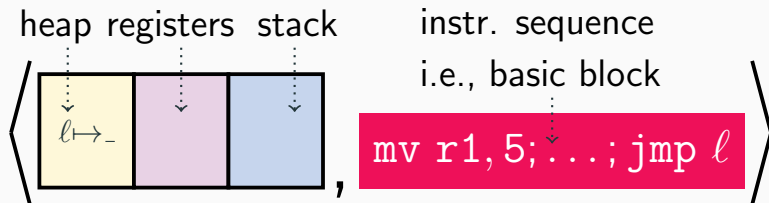
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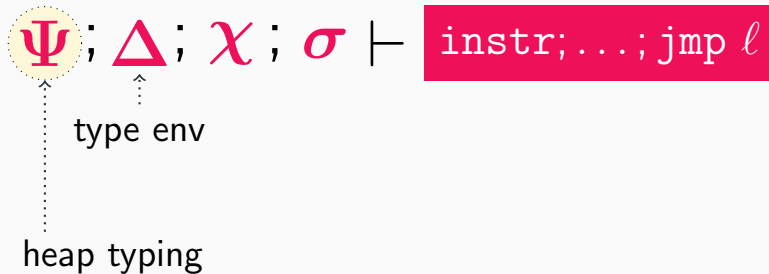
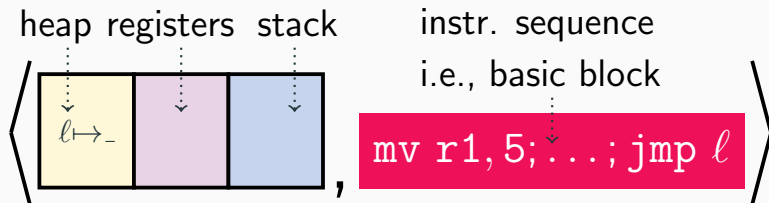
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heap typing

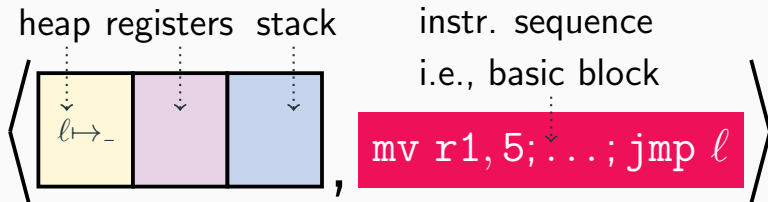
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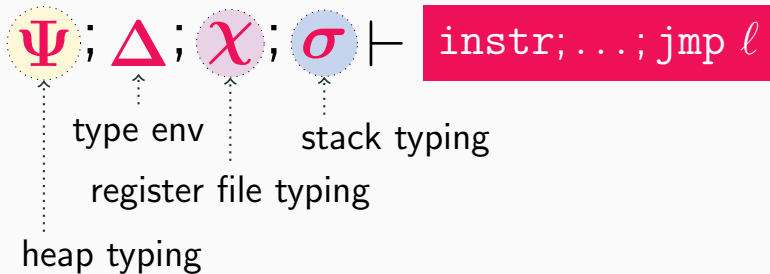
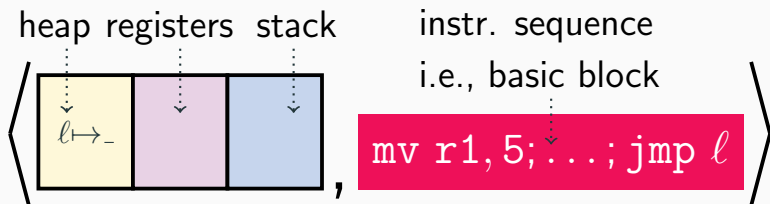
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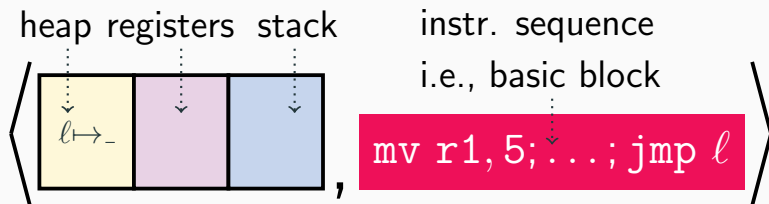
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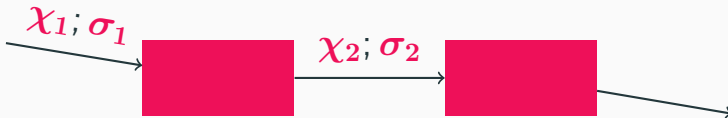
$\text{instr}; \dots; \text{jmp } \ell : \forall[\Delta].\{\chi; \sigma\}$

TAL types are preconditions

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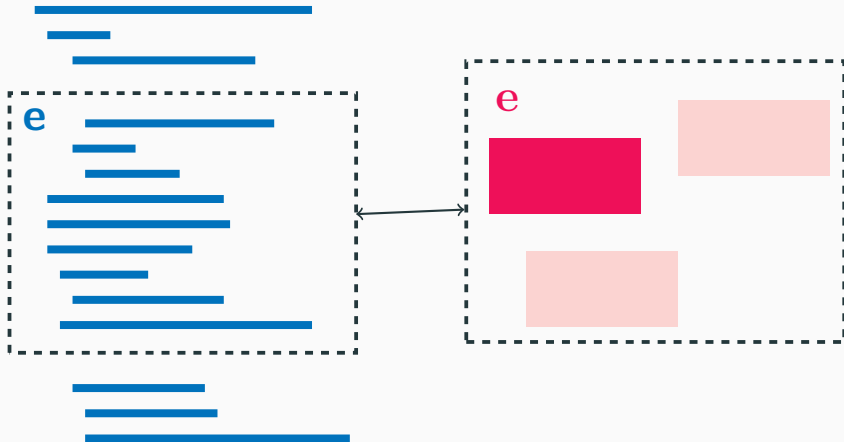
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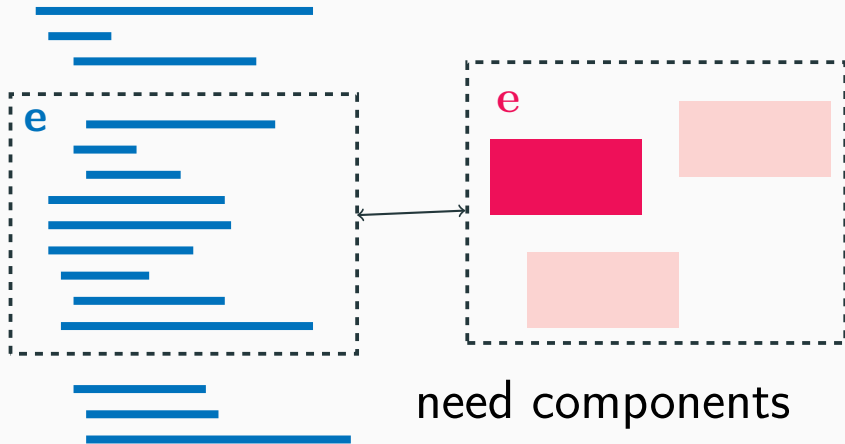




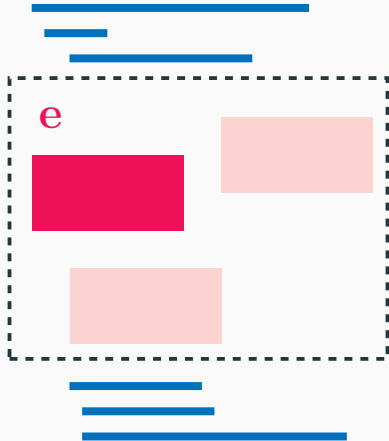
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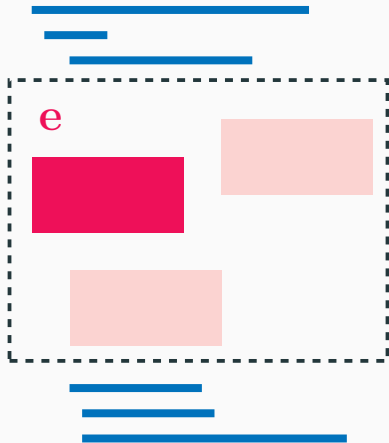
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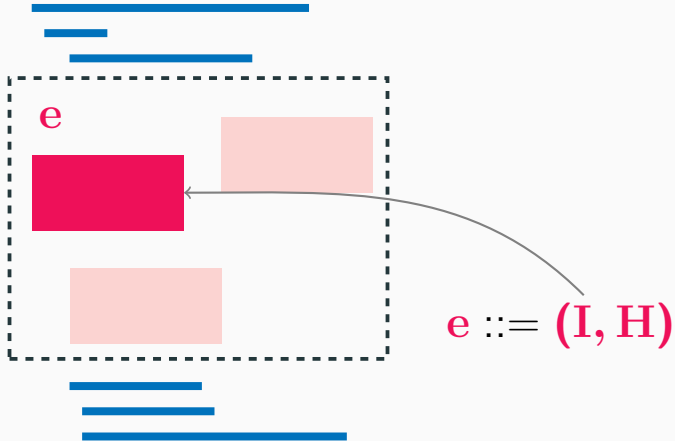


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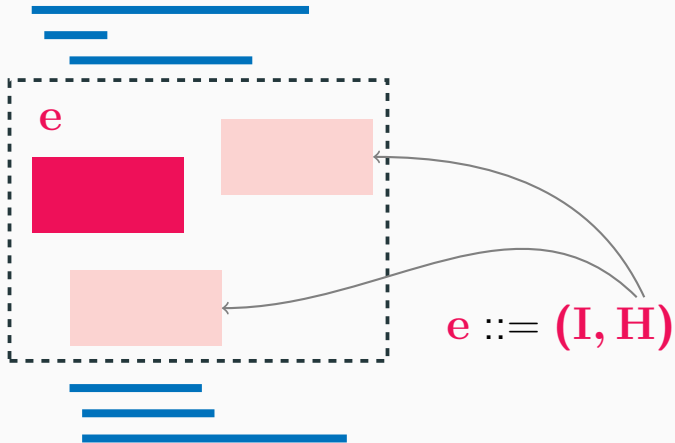


$$e ::= (I, H)$$

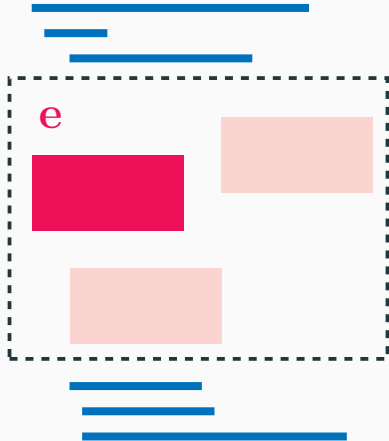
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writing this  
program requires  
multi-language

# Multi-languages in general

*[Matthews-Findler '07]*

Combine syntaxes from languages  $S$  and  $T$  and introduce boundary terms.

$${}^{\tau}ST(e_T) \mapsto^* {}^{\tau}ST(v_T) \mapsto v_S$$

$$TS^{\tau}(e_S) \mapsto^* TS^{\tau}(v_S) \mapsto v_T$$

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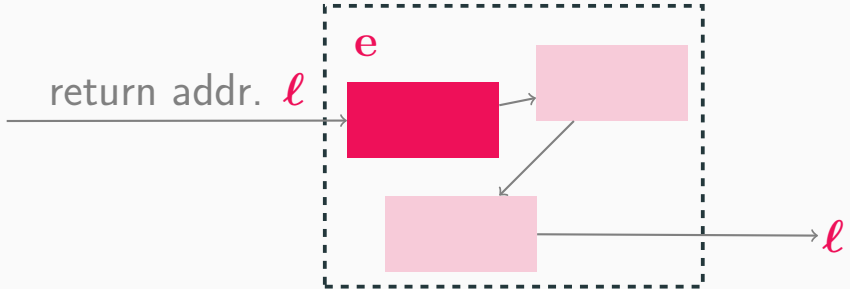
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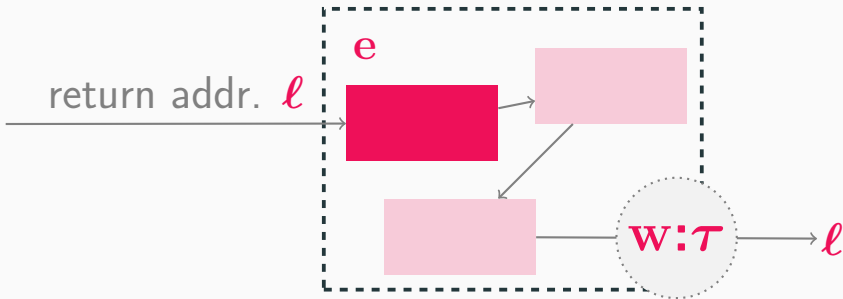
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# TAL components return to address



# Return value passed to address



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$$\Psi; \Delta; \chi; \sigma; \mathbf{q} \vdash (\mathbf{I}, \mathbf{H}) : \tau, \sigma'$$

return marker



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# Embedding Fun in TAL

$$\tau_{\mathcal{F}\mathcal{T}} \left( \begin{array}{c} \boxed{\tau_{\mathcal{F}\mathcal{T}} \left( \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right)} \\ \text{---} \\ \boxed{\phantom{\tau_{\mathcal{F}\mathcal{T}} \left( \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right)}} \end{array} \right)$$

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where  $\mathbf{v}:\tau \rightsquigarrow \mathbf{w}:\tau^+$

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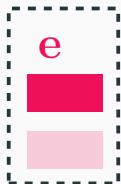
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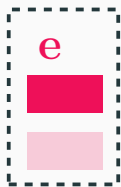
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So far, **q** can be **ra**, **n**, **end** $\{\tau; \sigma\}$



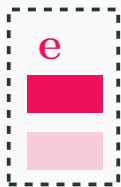
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$$\Psi; \Delta; \chi; \sigma; ra \vdash e : \tau, \sigma'$$

With these return markers, preconditions on  $e$  must specify all subsequent return markers.

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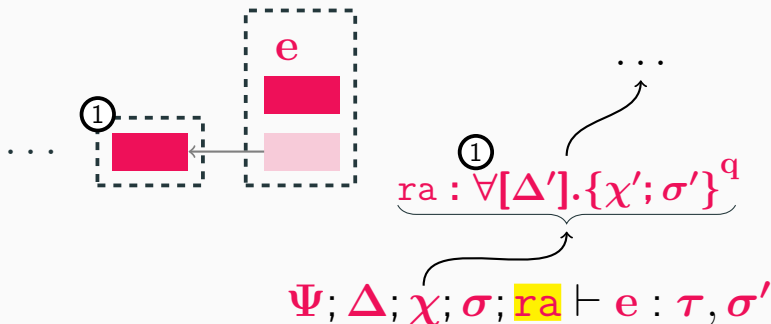


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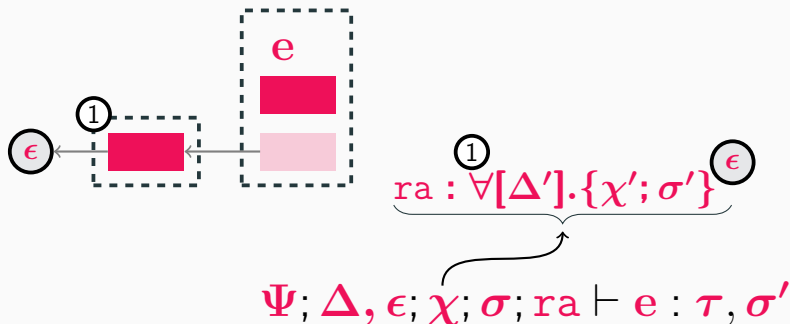


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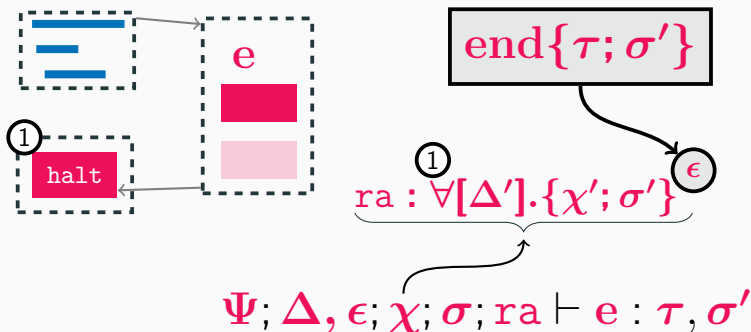
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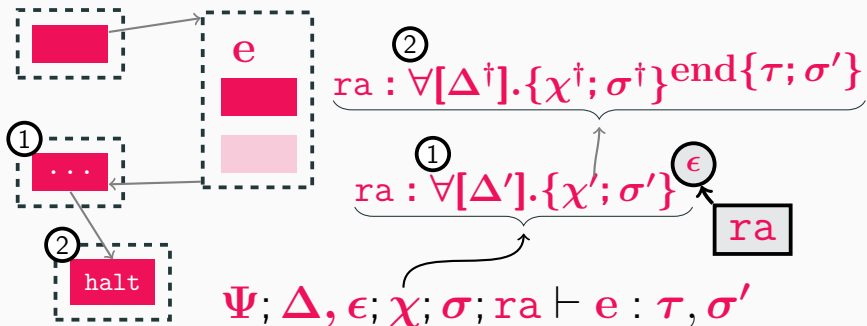
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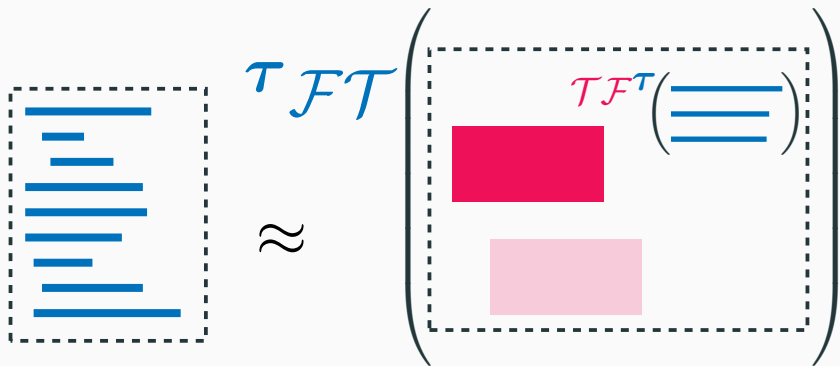
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# Proving program equivalence



Need logical relation for multi-language.



# How logical relations work

$\mathbf{e}:\tau \approx {}^\tau \mathcal{FT}(\mathbf{e}:\tau^+)$  means

$$\mathbf{e} \mapsto^* \mathbf{v}_1 \iff \mathcal{FT}(\mathbf{e}) \mapsto^* \mathbf{v}_2$$

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Write  $\mathbf{v}_1 \approx \mathbf{v}_2$  as  $(\mathbf{v}_1, \mathbf{v}_2) \in \mathcal{V}(\tau)$ .

## Equivalence of functions

$$(\lambda x. e_1, \lambda x. e_2) \in \mathcal{V}(\tau_1 \rightarrow \tau_2)$$

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$$\text{if } (v_1, v_2) \in \mathcal{V}(\tau_1) \implies$$

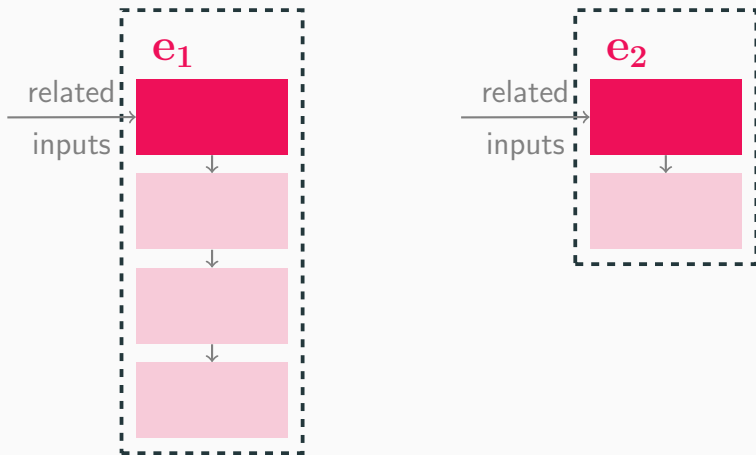
$$e_1[x \mapsto v_1] \approx e_2[x \mapsto v_2]$$

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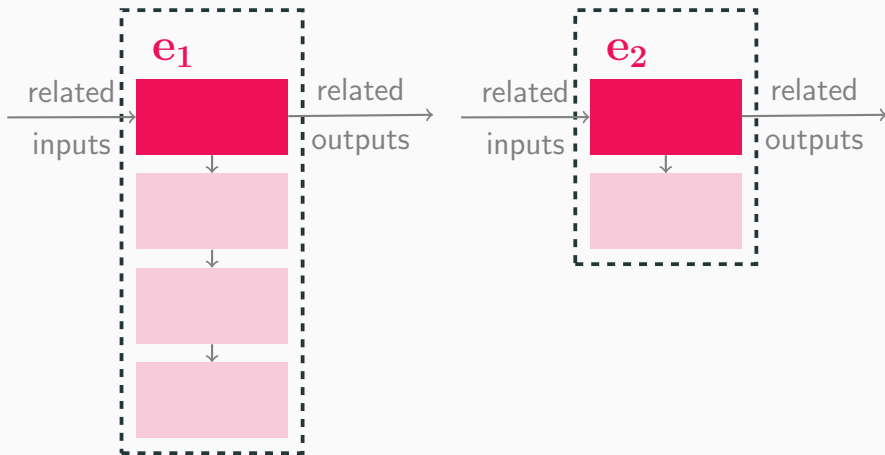
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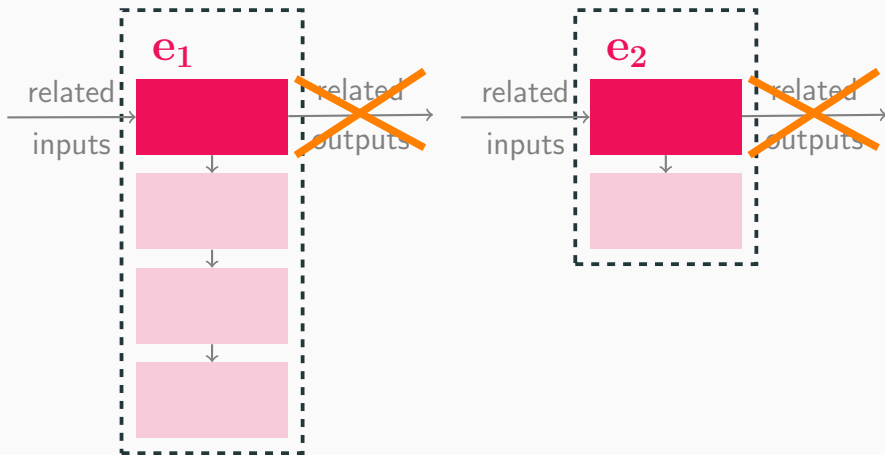
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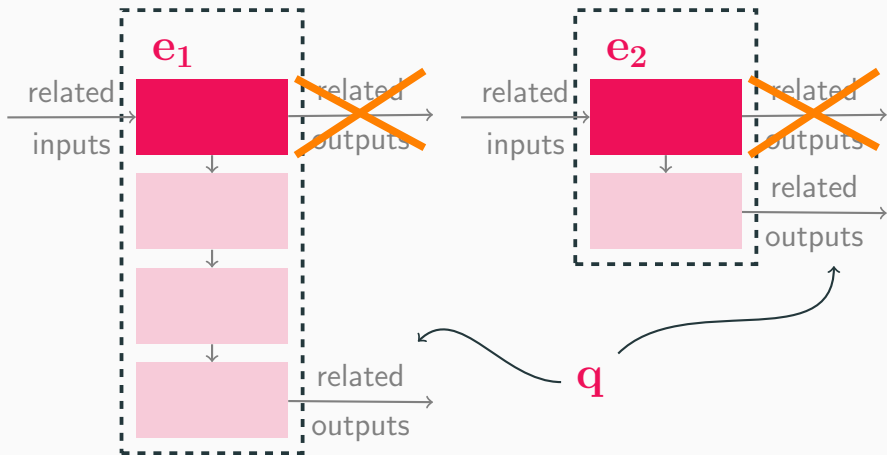
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How to safely mix assembly with high-level code? ✓

How to reason about equivalence of mixed programs? ✓

# Future work

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- Verification of some types of JIT transformations.



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- Correctness for compilers targeting TAL (as suggested by [*Perconti-Ahmed '14*]).
- Using return markers for slightly higher level (i.e., SSA-like) languages.

# Conclusion

**Return markers** allow **safe mixing of components** where high-level code remains high-level and low-level remains low-level.

See paper for (much) more detail and a web-based interpreter for **FunTAL**.