# Phantom Contracts for Better Linking

Or, why-oh-why can't we have cross-language type errors?

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# Summary

- Increasingly, languages provide programmers with rich types to enforce invariants.
- But linking components from different languages relies on unsafe FFIs with bad errors.
- Since linking happens after compilation, the key question is: how can we preserve source-level invariants through compilation?
- We propose enriching existing compiler target languages with phantom contracts, which are optional code that runs at type-checking time.
- Phantom contracts allow compiler writers to flexibly encode static invariants that cannot be expressed in the type system of the target.

## Sample Source Languages

```
Index<sup>±</sup> \tau ::= \eta \mid \forall \alpha. \tau \mid \tau \to \tau

\eta ::= \alpha \mid +0 \mid -\mid ?\mid \eta + \eta \mid \eta * \eta

e ::= n \mid x \mid e + e \mid e * e \mid \lambda x : \tau. e \mid e e

\lambda \alpha. e \mid e \mid \eta \mid

v ::= n \mid \lambda x : \tau. e \mid \Delta \alpha. e
```

Index<sup>±</sup> is a language with an indexed type system that allows index computations and abstraction over the sign of integers.

$$\frac{n \ge 0}{H; \Gamma \vdash n : +0} \qquad \frac{n < 0}{H; \Gamma \vdash n : -} \qquad \frac{x : \tau \in \Gamma}{H; \Gamma \vdash x : \tau}$$

$$\frac{H; \Gamma \vdash e_1 : \eta_1 \qquad H; \Gamma \vdash e_2 : \eta_2}{H; \Gamma \vdash e_1 + e_2 : \psi(\eta_1 + \eta_2)}$$

$$\frac{H; \Gamma \vdash e_1 : \eta_1 \qquad H; \Gamma \vdash e_2 : \eta_2}{H; \Gamma \vdash e_1 * e_2 : \Downarrow (\eta_1 * \eta_2)} \qquad \frac{H; \Gamma, x \tau_1 \vdash e : \tau_2}{H; \Gamma \vdash \lambda x.e : \tau_2 \rightarrow \tau_2}$$

$$\frac{H; \Gamma \vdash e : \tau_1 \to \tau_2 \qquad H; \Gamma \vdash e' : \tau_1}{H; \Gamma \vdash e e' : \tau_2} \qquad \frac{H, \alpha; \Gamma \vdash e : \tau}{H; \Gamma \vdash \Lambda \alpha. e : \forall \alpha. \tau}$$

```
\mathop{\Downarrow}(\eta_1*\eta_2) \quad = \quad *\mathop{\Downarrow}(\mathop{\Downarrow}(n_1),\mathop{\Downarrow}(n_2))
       H; \Gamma \vdash e : \forall \alpha.\tau
H; \Gamma \vdash e[\eta] : \psi(\tau[\eta/\alpha])
                                                                             * \downarrow (+0, +0) = +0
        + \downarrow (+0, +0) = +0
        + \Downarrow (-, +0)
                                                                              *↓(-,+0)
                                                                             * \Downarrow (+0, -)
        +↓(+0, -)
                                                                              * \downarrow (-,-)
        +↓(_, ?)
                                                                              *↓(_, ?)
                                = \eta_1 + \eta_2
                                                                                                     = \eta_1 * \eta_2
        + \downarrow (\eta_1, \eta_2)
                                                                              * \downarrow (\eta_1, \eta_2)
```

```
BabyDill \tau ::= int |\tau - \tau|!\tau |\tau \& \tau|\tau \otimes \tau

e ::= n |x|a| \lambda a : \tau . e | e e'|!e

let !x = e \text{ in } e' | \langle e, e' \rangle | e . 1 | e . 2

(e, e) |\text{let } (a, a') = e \text{ in } e'

v ::= () |\lambda a : \tau . e|!e| \langle e, e' \rangle | (v, v')
```

BabyDill is a language with linear and unrestricted variables.

$$\begin{array}{c} \mathbf{x}:\tau\in\Gamma\\ \hline \Gamma;\mathbf{a}:\tau\vdash\mathbf{a}:\tau & \hline \Gamma;\cdot\vdash\mathbf{x}:\tau & \hline \Gamma;\cdot\vdash\mathbf{n}:\mathbf{int}\\ \hline \\ \frac{\Gamma;\Delta,\mathbf{a}:\tau_1\vdash\mathbf{e}:\tau_2}{\Gamma;\Delta\vdash\lambda\mathbf{a}:\tau_1\cdot\mathbf{e}:\tau_1\multimap\tau_2}\\ \hline \\ \frac{\Gamma;\Delta_1\vdash\mathbf{e}:\tau_1\multimap\tau_2}{\Gamma;\Delta_3\vdash\mathbf{e}_2:\tau_1} & \Delta_3\cong\Delta_1,\Delta_2\\ \hline \\ \frac{\Gamma;\Delta_1\vdash\mathbf{e}:\tau}{\Gamma;\Delta_1\vdash\mathbf{e}:\tau_1} & \hline \\ \frac{\Gamma;\Delta\vdash\mathbf{e}:\tau}{\Gamma;\Delta\vdash\mathbf{e}:\tau_1} & \hline \\ \frac{\Gamma;\Delta\vdash\mathbf{e}:\tau}{\Gamma;\Delta\vdash\mathbf{e}:\tau_1} & \hline \\ \frac{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2}{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2}\\ \hline \\ \frac{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2}{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2} & \hline \\ \frac{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2}{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2}\\ \hline \\ \frac{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2}{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2} & \hline \\ \frac{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2}{\Gamma;\Delta\vdash\mathbf{e}:\tau_1\&\tau_2}\\ \hline \end{array}$$

$$\frac{\Gamma; \Delta_1 \vdash \mathbf{e} : !\tau \qquad \Gamma, \mathbf{x} : \tau; \Delta_2 \vdash \mathbf{e}' : \tau' \qquad \Delta_3 \cong \Delta_1, \Delta_2}{\Gamma; \Delta_3 \vdash \mathbf{let} ! \mathbf{x} = \mathbf{e} \text{ in } \mathbf{e}'}$$

$$\frac{\Gamma; \Delta_1 \vdash \mathbf{e}_1 : \tau_1 \qquad \Gamma; \Delta_1 \vdash \mathbf{e}_2 : \tau_2 \qquad \Delta_3 \cong \Delta_1, \Delta_2}{\Gamma; \Delta_3 \vdash (\mathbf{e}_1, \mathbf{e}_2) : \tau_1 \otimes \tau_2}$$

$$\begin{split} &\Gamma; \Delta_1 \vdash e : \tau_1 \otimes \tau_2 \\ &\Gamma; \Delta_2, a : \tau_1, a' : \tau_1 \vdash e' : \tau' \qquad \Delta_3 \cong \Delta_1, \Delta_2 \\ &\Gamma; \Delta_3 \vdash \mathsf{let}\; (a, a') = e \; \mathsf{in}\; e' : \tau' \end{split}$$

#### Core Idea

- Terms  $\hat{\mathbf{e}}$  are paired with phantom contracts  $\{\varphi\}$ : type-time operational code to encode static invariants.
- Our BabyDill compiler encodes the number of variable uses left (≤ 1).

```
\begin{array}{ll} ({\tt a}:{\tt \tau})^+ & \leftrightsquigarrow & {\tt a}\{{\tt a}:=\delta^2(-,!{\tt a},1)\} \\ (\lambda{\tt a}:{\tt \tau_1}.{\tt e})^+ & \leadsto & \lambda{\tt a}:{\tt \tau_1}^+.{\tt let}_\{{\tt a}\}=\emptyset\{{\tt ref}\,1\}\,{\tt in} \\ & {\tt let}_{\tt r}\{\}={\tt e}^+\,{\tt in} \\ & {\tt r}\}\{\delta^1({\tt assert},\delta^2({\tt sexp}=,!{\tt a},\emptyset));\} \end{array}
```

- Our Index<sup>±</sup> compiler encodes a representation of the source type.
- Safe interoperation of Index<sup>±</sup> & BabyDill means phantom contracts don't fail.

$$\lambda$$
 ( $\lambda$ a:int&int. a.1)<sup>+</sup>((2 \* 3)<sup>+</sup>, (4)<sup>+</sup>)  
 $\lambda$  ( $\lambda$ x:+0. x + 2)<sup>+</sup>(2)<sup>+</sup>

 Compiler writers can provide safe FFIs to help satisfy phantom contracts.

```
 \sqrt{(\lambda x:+0. x+2)^{+} not_neg(2)^{+}} 
 not_neg x = if(x < 0) fail else x{(\lambda+0)\lambda}
```

• Or extend their compilers once common encodings become established.

```
(n:int)^+ \rightsquigarrow n\{\langle\langle +0\rangle\rangle\} \text{ if } n >= 0
(\lambda x:+0. x + 2)^+(2)^+
```

### Sample Target Language

```
Phantom  \tau \  \, ::= \  \, \inf \mid \tau \to \tau' \mid \tau \times \tau' \mid \mu \alpha.\tau \mid \alpha \\ e \  \, ::= \  \, \hat{e}\{\varphi\} \\ \hat{e} \  \, ::= \  \, x \mid n \mid e + e \mid e * e \mid \lambda x : \tau.e \mid e \; e' \\ \qquad \qquad \qquad (e,e) \mid fst \; e \mid snd \; e \mid fold \; e \\ \qquad \qquad \qquad unfold \; e \mid let \; x\{\nu\} : \tau = e \; in \; e' \\ v \  \, ::= \  \, n \mid fold \; v \mid \lambda x : \tau.e \mid (v,v) \\ \varphi \  \, ::= \  \, \ell \mid sexp \mid ref \; sexp \mid \varphi := \varphi \mid !\varphi \mid \nu \\ \qquad \qquad \qquad match \; \varphi \mid n\nu_1.\varphi_1 \mid s\nu_2.\varphi_2 \mid b\nu_3.\varphi_3 \mid (\nu_4,\nu_5).\varphi_4 \\ \qquad \qquad \lambda \nu : \varphi \tau.\varphi \mid \varphi \; \varphi' \mid \varphi; \varphi' \mid \delta^n(op^n,\varphi_1,\ldots\varphi_n) \\ sexp \  \, ::= \  \, n \mid s \mid true \mid false \mid (sexp, sexp') \\ op^1 \  \, ::= \  \, assert \mid not \mid length \mid \ldots \\ op^2 \  \, ::= \  \, sexp \mid ref \; sexp \mid \varphi \tau \to \varphi \tau \\ \\ \Gamma; \; S \vdash \hat{e} : \; \tau; \; S' \qquad \; \Gamma \vdash (S',\varphi) \Downarrow (S'',\varphi') \qquad \; x : \; \tau \in \Gamma
```

$$\frac{\Gamma; S \vdash e_1 : \text{int}; S' \qquad \Gamma; S' \vdash e_2; S'' : \text{int}}{\Gamma; S \vdash e_1 * e_2 : \text{int}; S''}$$

$$\frac{\Gamma, \mathbb{X} : \tau; \mathbb{S} \vdash \mathbb{e} : \tau'; \mathbb{S}'}{\Gamma; \mathbb{S} \vdash \lambda \mathbb{X} : \tau. \mathbb{e} : \tau \to \tau'; \mathbb{S}'} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau \to \tau'; \mathbb{S}'}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau \to \tau'; \mathbb{S}'} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau \to \tau'; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1; \mathbb{S}'} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_1 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2 \times \tau_2; \mathbb{S}''}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2; \mathbb{S}''} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2 \times \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e} : \tau_2} \qquad \frac{\tau_2}{\Gamma; \mathbb{S} \vdash \mathbb{e}$$

$$\frac{\Gamma; S \vdash e : \tau_1 \times \tau_2; S'}{\Gamma; S \vdash \text{snd } e : \tau_2; S'} \qquad \frac{\Gamma; S \vdash e : \tau[\mu\alpha.\tau/\alpha]; S'}{\Gamma; S \vdash \text{fold } e : \mu\alpha.\tau; S'}$$

$$\frac{\Gamma; S \vdash e : \mu \alpha.\tau; S'}{\Gamma; S \vdash \text{unfold } e : \tau[\mu \alpha.\tau/\alpha]; S'}$$

$$\frac{\Gamma; S_1 \vdash \hat{\textbf{e}}_1 : \tau; S_2}{\Gamma \vdash (S_2, \varphi) \Downarrow (S_3, \varphi') \qquad \Gamma, \textbf{x} : \tau, \nu : \varphi'; S_3 \vdash \textbf{e}_2 : \tau_2; S_4}{\Gamma; S_1 \vdash \text{let } \textbf{x} \{ \nu \} : \tau = \hat{\textbf{e}}_1 \{ \varphi \} \text{ in } \textbf{e}_2 : \tau_2; S_4}$$

$$\frac{\Gamma \vdash (S_1, \varphi_1) \Downarrow (S_2, n_1) \qquad \Gamma \vdash (S_2, \varphi_2) \Downarrow (S_3, n_2) \qquad n_3 = n_1 - n_2}{\Gamma \vdash (S_1, \delta^2(-, \varphi_1, \varphi_2)) \Downarrow (S_3, n_3)}$$

# Sample Compilers

```
Index<sup>±</sup> → Phantom
                            (n:+0)^+ \longrightarrow n\{\langle (+0)\rangle\}
                              (\mathbf{n}:-)^+ \iff \mathbf{n}\{\langle\!\langle -\rangle\!\rangle\}
               (e_1 + e_2 : \eta)^+ \rightsquigarrow (e_1^+ + e_2^+) \{\langle \langle \eta \rangle \rangle \}
                (e_1 * e_2 : \eta)^+ \iff (e_1^+ * e_2^+) \{ \langle \langle \eta \rangle \rangle \}
                              (\mathbf{x}:\tau)^+ = \mathbf{x}\{\delta^1(\text{assert}, \delta^2(\text{sexp}=, \langle \langle \tau \rangle \rangle, \nu_{\mathbf{x}})); \langle \langle \tau \rangle \rangle\}
    (\lambda x:\tau.e:\tau\to\tau')^+=(\lambda x:\tau^+.let_{v_x}:int=0\{\langle\langle\tau\rangle\rangle\}ine^+)
                                                                        \{\langle\!\langle \tau \to \tau' \rangle\!\rangle\}
                      (e \ e' : \tau))^+ \quad \rightsquigarrow \quad let \ f\{\nu_f\} : (\tau' \to \tau)^+ = e^+ \ in
                                                                        let a\{v_a\} : \tau'^+ = e'^+ in
                                                                        (f a){match v_f}
                                                                        |('\mapsto',(\nu_{\tau'},\nu_{\tau})).
                                                                        \delta^1(\text{assert}, \delta^2(\text{sexp}=, \nu_{\tau'}, \nu_a)); \langle \langle \tau \rangle \rangle \}
             (\Lambda \alpha.e : \forall \alpha.\tau)^+ \quad \leadsto \quad e^+ \{\langle\!\langle \forall \alpha.\tau \rangle\!\rangle\}
          (e[\eta] : \tau[\eta/\alpha])^+ \quad \Leftrightarrow \quad e^+\{\langle\!\langle \tau[\eta/\alpha] \rangle\!\rangle\}
             \langle\!\langle \forall \alpha. \tau \rangle\!\rangle = (\forall \forall ', (\alpha, \langle\!\langle \tau \rangle\!\rangle))
                                                                                                        (\forall \alpha. tau)^+ = \tau^+
        \langle\!\langle \tau \to \tau' \rangle\!\rangle \quad = \quad (' \mapsto ', (\langle\!\langle \tau \rangle\!\rangle, \langle\!\langle \tau' \rangle\!\rangle)) \qquad (\tau \to \tau')^+ \quad = \quad \tau^+ \to \tau'^+
                     \langle\!\langle \alpha \rangle\!\rangle = '\alpha'
                                                                                                                              \eta^+ = int
                  \langle \langle +0 \rangle \rangle = ' + 0'
      \langle\langle \eta_1 + \eta_2 \rangle\rangle = ('+', (\langle\langle \eta_1 \rangle\rangle, \langle\langle \eta_2 \rangle\rangle))
        \langle \langle \eta_1 * \eta_2 \rangle \rangle = ('*', (\langle \langle \eta_1 \rangle \rangle, \langle \langle \eta_2 \rangle \rangle))
BabyDill 	→ Phantom
                                        (\mathbf{x}:\boldsymbol{\tau})^+ \quad \boldsymbol{\rightsquigarrow} \quad \mathbf{x}\{\}
```

#### $(a : \tau)^+ \iff a\{a := \delta^2(-, !a, 1)\}$ $(n:int)^+ \rightsquigarrow n{}$ $(\lambda a : \tau_1.e)^+ \longrightarrow \lambda a : \tau_1^+.let_{a} = 0 \{ref 1\} in$ $let_r{} = e^+ in$ $r\{\delta^1(assert, \delta^2(sexp=, !a, 0));\}$ $(e e')^+ \rightsquigarrow e^+ e'^+ \{\}$ $(!e)^+ \rightsquigarrow e^+{}$ $(\texttt{let !x} = \texttt{e} : \tau \texttt{ in } \texttt{e'})^+ \quad \rightsquigarrow \quad \texttt{let } \texttt{x}\{\} : \tau^+ = \texttt{e}^+ \texttt{ in } \texttt{e'}^+ \{\}$ $(\Gamma; \mathbf{a}_1 : \tau_1 \dots \vdash \mathsf{w} \mathsf{let} \mathsf{v}_1 \{\} = \mathbf{e}_1^+ \mathsf{in}$ $\langle e_1, e_2 \rangle : \tau_1 \& \tau_2)^+$ $let_{\{\}} = \emptyset\{\delta^1(assert, \delta^2(sexp=, !a_1, \emptyset))\}$ ...; $a_1 := 1...$ in $(v_1, e_2^+)$ {} $(e.2)^+ \rightsquigarrow \text{snd } e^+ \{\}$ $((e_1, e_2))^+ \rightsquigarrow (e_1^+, e_2^+)\{\}$ $(\operatorname{let}(a, a') = e \iff \operatorname{let} t\{\}: (\tau_1 \otimes \tau_2)^+ = e^+ \text{ in }$ let $a{a}:\tau_1^+ = fst t{ref 1} in$ in e')+

```
\begin{array}{rcl} & & \text{in } \mathbf{e'}^{+}\{\delta^{1}(\mathsf{assert}, \delta^{2}(\mathsf{sexp=}, !a, \mathbf{0})); \\ & & \delta^{1}(\mathsf{assert}, \delta^{2}(\mathsf{sexp=}, !a', \mathbf{0}))\} \\ & & \text{int}^{+} & = & \text{int} & (\tau \multimap \tau')^{+} & = & \tau^{+} \to \tau'^{+} \\ & & (!\tau)^{+} & = & \tau^{+} & (\tau_{1}\&\tau_{2})^{+} & = & \tau_{2}^{+} \times \tau_{2}^{+} \\ & & (\tau_{1} \otimes \tau_{2})^{+} & = & \tau_{2}^{+} \times \tau_{2}^{+} \end{array}
```

let  $a'\{a'\}: \tau_2^+ = \text{snd t}\{\text{ref 1}\}$ 

# Discussion

- Particular phantom contract encodings are *only* given meaning by compilers, since  $\{\varphi\}$  can be attached to *any* term  $\hat{e}$ .
- But given a source language A, we can define:

ullet Then two languages  ${\it A}$  and  ${\it B}$  are safe-to-link if:

$$\forall e_A, e_B. \ e_A^+ \bowtie e_B^+ \ \text{links w/o error} \implies e_B^+ \in \bigcup_{\tau} \mathcal{E}_A[\![\tau]\!]$$

 $\mathcal{E}_A[\![\tau]\!] = \{\hat{e}\{\varphi\} \mid \text{acts as } \tau, \text{ with } A\text{-compiler encoding}\}$ 

i.e., linkable  $\emph{B}$  output is expressible as  $\emph{A}$  behavior.

- But could also design a specialized T and  $\mathcal{E}_T[[\tau]]$  as a rich low-level interface.
- Phantom contracts enable this design process without needing to change the target language.

$\nu:\varphi\in\Gamma$	$\Gamma \vdash (S, \varphi) \Downarrow (S', true)$
$\Gamma \vdash (S, \nu) \Downarrow (S, \varphi)$	$\overline{\Gamma \vdash (S, \delta^1(assert, \varphi)) \Downarrow (S', true)}$
$\mathtt{fresh}\: \ell$	$\ell \in S$
$\Gamma \vdash (S, \operatorname{ref} \varphi) \Downarrow (S[\ell \mapsto \varphi],$	$ \overline{\ell}) \qquad \overline{\Gamma \vdash (S, \ell := \varphi) \Downarrow (S[\ell \mapsto \varphi], \emptyset)} $
$\Gamma \vdash (S, \varphi_1) \Downarrow (S', s)$	
$\Gamma$ , $\nu$ :s $\vdash$ (S', $\varphi_2$ ) $\downarrow$ (S", $\varphi_3$ )	$\varphi_2'$ ) $S[\ell] = \varphi$

 $\Gamma \vdash (S, !\ell) \downarrow (S, \varphi)$ 

 $\Gamma \vdash (S, \mathsf{match} \ \varphi_1 | \ \mathsf{sv}.\varphi_2) \ \Downarrow (S'', \varphi_2)$