

# Lecture 1 Activity Results for Test Student

Score for this attempt: 1 out of 1

Submitted Jan 9 at 3:10pm

This attempt took 4 minutes.

## Question 1

1 / 1 pts

Find a general solution of  $u''(x) = 3u(x)$ .

- ☐  $u(x) = ce^{\sqrt{3}x}$
- ☐  $u(x) = ce^{-\sqrt{3}x}$
- ☒  $u(x) = c_1e^{\sqrt{3}x} + c_2e^{-\sqrt{3}x}$
- ☐  $u(x) = c_1e^{3x} + c_2e^{-3x}$
- ☐  $u(x) = c_1 \cos(\sqrt{3}x) + c_2 \sin(\sqrt{3}x)$

Correct!

Additional Comments:

## Question 2

0 / 0 pts

Find a general solution of  $u''(x) - 6u'(x) + 9u(x) = 0$ .

☐  $u(x) = ce^{3x}$

☐  $u(x) = c_1e^{3x} + c_2e^{-3x}$

☐  $u(x) = cxe^{3x}$

Correct!

☒  $u(x) = c_1e^{3x} + c_2xe^{3x}$

☐  $u(x) = c_1e^{-3x} + c_2xe^{-3x}$

Additional Comments:

### Question 3

0 / 0 pts

Let  $u_p(t)$  be a particular solution of  $u''(t) - 3u(t) = \cos(t^2)$ . Find a general solution of  $u''(t) - 3u(t) = \cos(t^2)$ .

☐  $u(t) = c_1u_p(t) + c_2e^{\sqrt{3}t}$

☐  $u(t) = c_1u_p(t) + c_2e^{-\sqrt{3}t}$

Correct!

☒  $u(t) = u_p(t) + c_1 e^{\sqrt{3}t} + c_2 e^{-\sqrt{3}t}$

☐  $u(t) = u_p(t) + c_1 e^{\sqrt{3}t} + c_2 t e^{\sqrt{3}t}$

☐  $u(t) = u_p(t) + c_1 \cos(\sqrt{3}t) + c_2 \sin(\sqrt{3}t)$

Additional Comments:

#### Question 4

0

/ 0 pts

Consider the PDE  $\cos(t)u_t + e^x u_x = x^2 \sin(t)$  for  $u(x, t)$ . We classify it as

☐ a first order, nonlinear, inhomogeneous PDE.

☐ a first order, linear, homogeneous PDE.

☒ a first order, linear, inhomogeneous PDE.

☐ a first order, nonlinear, homogeneous PDE.

☐ a second order, linear, inhomogeneous PDE.

Correct!

Additional Comments:

### Question 5

0 / 0 pts

Consider the eigenvalue problem  $\begin{cases} X''(x) = -\lambda X(x) \\ X(0) = 0, \quad X(L) = 0 \end{cases}$ .

The eigenvalues and eigenfunctions are

☐  $\lambda_n = (n\pi)^2, \quad X_n(x) = \sin(n\pi x), \quad n = 1, 2, \dots$

☒  $\lambda_n = \left(\frac{n\pi}{L}\right)^2, \quad X_n(x) = \sin\left(\frac{n\pi}{L}x\right), \quad n = 1, 2, \dots$

☐  $\lambda_n = \left(\frac{n\pi}{L}\right)^2, \quad X_n(x) = \sin\left(\frac{n\pi}{L}x\right), \quad n = 0, 1, 2, \dots$

☐  $\lambda_n = \left(\frac{2n\pi}{L}\right)^2, \quad X_n(x) = \sin\left(\frac{2n\pi}{L}x\right), \quad n = 1, 2, \dots$

☐  $\lambda_n = \left(\frac{n\pi}{L}\right)^2, \quad X_n(x) = \cos\left(\frac{n\pi}{L}x\right), \quad n = 0, 1, 2, \dots$

Correct!

Additional Comments:

## Question 6

0 / 0 pts

Which of the following is true? **Select all that apply.**

☐  $u_t = ku_{xx}$  is an inhomogeneous PDE.

☒  $u_t = ku_{xx}$  is a homogeneous PDE.

☐  $u(x, 0) = \sin(\frac{\pi}{L}x)$  is a homogeneous initial condition.

☒  $u(0, t) = \sin(t)$  is an inhomogeneous boundary condition.

☐  $u(0, t) = \sin(t)$  is a homogeneous boundary condition.

Additional Comments:

Correct!

Correct!

Unanswered

## Question 7

0 / 0 pts

Which statement below is true?

☐

$$\int_0^L \sin\left(\frac{\alpha\pi}{L}x\right) \sin\left(\frac{\beta\pi}{L}x\right) dx = \frac{1}{2} \left( \int_0^L \sin\left(\frac{(\alpha+\beta)\pi}{L}x\right) dx + \int_0^L \sin\left(\frac{(\alpha-\beta)\pi}{L}x\right) dx \right)$$



$$\int_0^L \sin\left(\frac{\alpha\pi}{L}x\right) \sin\left(\frac{\beta\pi}{L}x\right) dx = \frac{1}{2} \left( \int_0^L \cos\left(\frac{(\alpha + \beta)\pi}{L}x\right) dx + \int_0^L \cos\left(\frac{(\alpha - \beta)\pi}{L}x\right) dx \right)$$



$$\int_0^L \sin\left(\frac{\alpha\pi}{L}x\right) \sin\left(\frac{\beta\pi}{L}x\right) dx = \frac{1}{2} \left( \int_0^L \cos\left(\frac{(\alpha + \beta)\pi}{L}x\right) dx - \int_0^L \cos\left(\frac{(\alpha - \beta)\pi}{L}x\right) dx \right)$$



$$\int_0^L \sin\left(\frac{\alpha\pi}{L}x\right) \sin\left(\frac{\beta\pi}{L}x\right) dx = \frac{1}{2} \left( \int_0^L \sin\left(\frac{(\alpha + \beta)\pi}{L}x\right) dx - \int_0^L \sin\left(\frac{(\alpha - \beta)\pi}{L}x\right) dx \right)$$

Correct Answer



$$\int_0^L \sin\left(\frac{\alpha\pi}{L}x\right) \sin\left(\frac{\beta\pi}{L}x\right) dx = \frac{1}{2} \left( \int_0^L \cos\left(\frac{(\alpha - \beta)\pi}{L}x\right) dx - \int_0^L \cos\left(\frac{(\alpha + \beta)\pi}{L}x\right) dx \right)$$

Additional Comments:

Fudge Points:

You can manually adjust the score by adding positive or negative points to this box.

**Final Score:** 1 out of 1

Update Scores