Section (

TA: Dante Buhl

Agenda

### Section 6

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UCSC Math-19B

February 20, 2024

# Plan for Today

Section 6

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Agenda

#### Topics to Cover

- Trig Substitution
- Partial Fraction Decomposition

### Section Activity 6

■ 1 question

#### Upcoming Assignments

- Homework 6 (Due Fri, Feb. 16<sup>th</sup>)
- Midterm (On Mon, Feb  $26^{th}$ )

### Learning Outcomes

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Agenda Review

- Revisiting the notion of substitution and trigonometric substitution.
- Applying the methods of Partial Fraction Decomposition.

# Trig Substitution

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Agenda Review This substitution method is used when a trigonometric identity can reduce the complexity of an integral. Lets look at an example.

$$\int \sqrt{1 - x^2} dx$$
The Usual Suspects:
$$x = \sin(\theta), \quad dx = \cos(\theta) d\theta$$

$$\int \sqrt{\cos^2(\theta)} \cos(\theta) d\theta$$

$$\cos^2(x) + \sin^2(x) = 1$$

$$1 + \tan^2(x) = \sec^2(x)$$

$$= \int \cos^2(\theta) d\theta$$

$$\cot^2(x) + 1 = \csc^2(x)$$

# Partial Fraction Decomposition

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Agenda Review Partial Fraction Decomposition expands rational function into a sum/difference of smaller rational functions. i.e.

$$\frac{1}{x^2 - 5x + 6} = \frac{1}{(x - 2)(x - 3)} = \frac{A}{x - 2} + \frac{B}{x - 3}$$

Notice that the two terms on the right are easier to integrate than the one on the left. They integrate into natural logarithms.

# Partial Fraction Decomposition (Continued)

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Agenda Review Partial Fraction Decomposition coefficients are found using a series of equations.

$$1 = A(x-3) + B(x-2)$$

Note: it helps to isolate the equations by orders of x. One equation for  $x^0$ , one for  $x^1$ , one for  $x^2$ , and so on as needed.

$$A + B = 0,$$
  $-3A - 2B = 1$   
 $A = -B,$   $-3A + 2A = 1$   
 $A = -1,$   $B = 1$ 

# Warm Up - Partial Fraction Decomposition

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Agenda Review

$$\int \frac{1}{x^2 - 2x} dx$$

When your group is done working on this problem, review polyonomial long division and then let me know (I'll come give you the section activity code).