

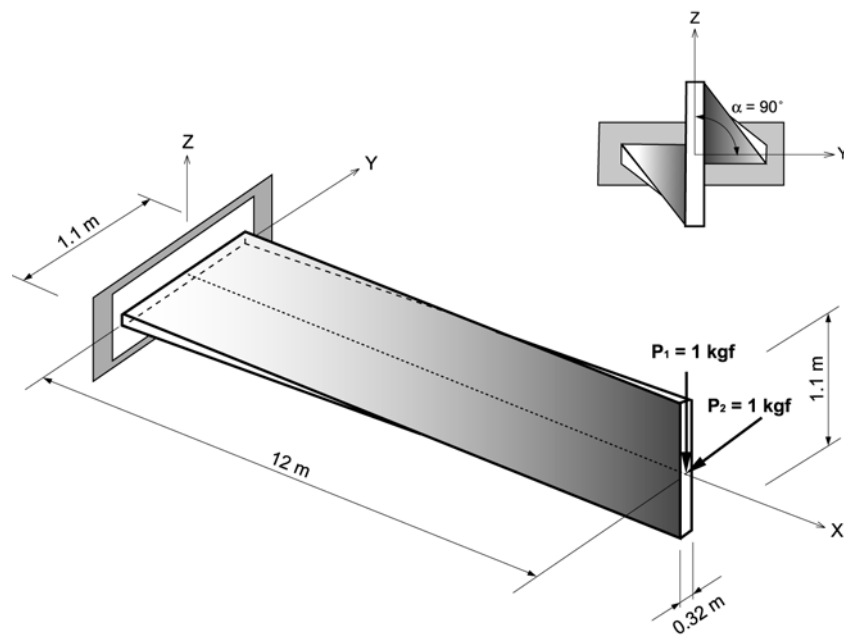
# Static-33

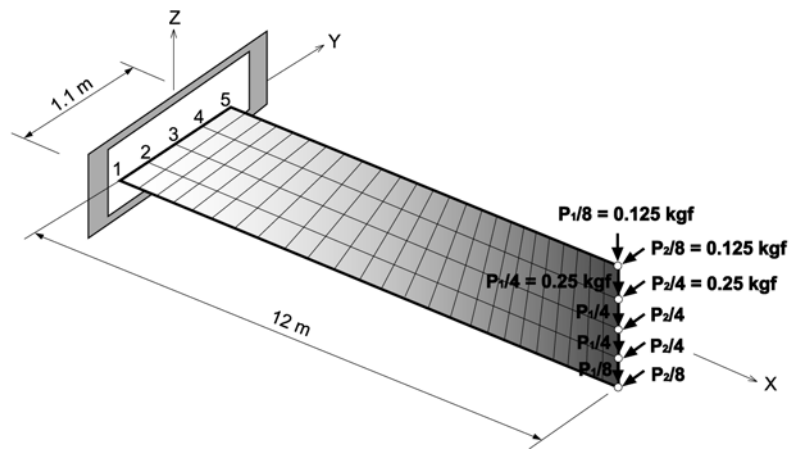
## Title

Twisted beam under tip shear loads

## Description

A twisted cantilever beam of rectangular cross-section is subjected to the action of unit static shear loads applied at the tip. Load  $P_1$  is applied in the in-plane and load  $P_2$  is applied in the out-of-plane directions. The undeformed cantilever configuration has a  $90^\circ$  twist. Determine the tip displacements in the load directions.





*Structural geometry and analysis model*

## MODEL

### *Analysis Type*

3-D static analysis

### *Unit System*

m, kgf

### *Dimension*

Length 12 m

### *Element*

Plate element

### *Material*

Modulus of elasticity  $E = 2.9 \times 10^7 \text{ kgf/m}^2$

Poisson's ratio  $\nu = 0.22$

**Sectional Property**

Rectangular cross-section:  $b = 1.1 \text{ m}$ ,  $t = 0.32 \text{ m}$

**Boundary Condition**

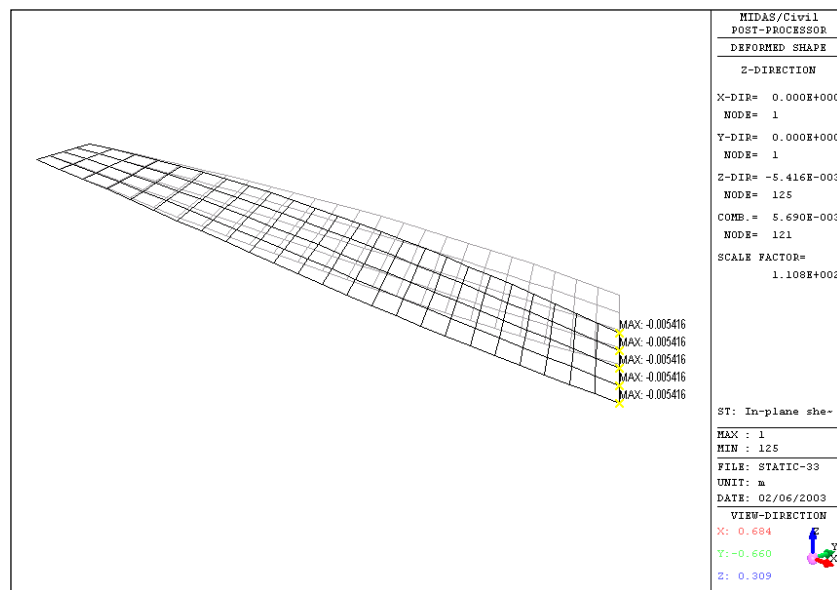
Node 1,2,4,5: Constrain  $D_X$ ,  $D_Z$  and  $R_Y$

Node 3: Constrain  $D_X$ ,  $D_Y$ ,  $D_Z$  and  $R_Y$

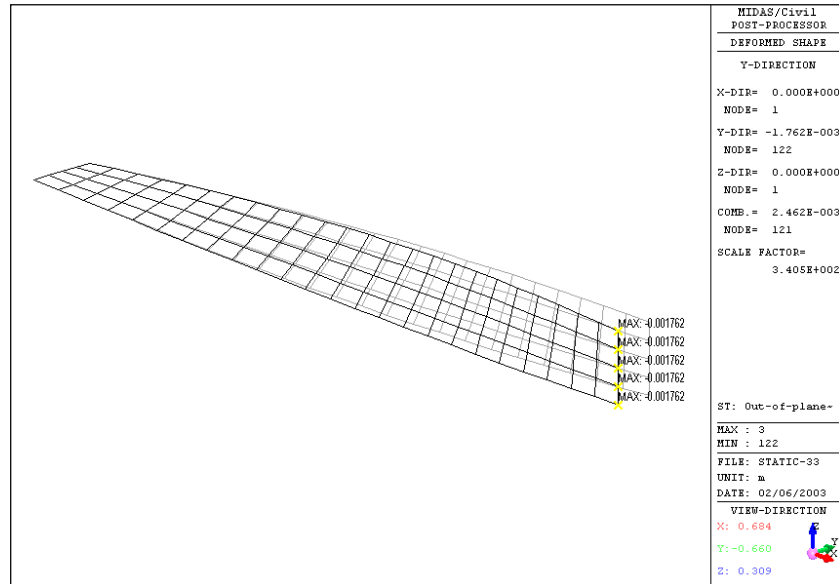
**Load Case**

Case 1: Unit static shear loads  $P_1 = 1.0 \text{ kgf}$  (Vertical)

Case 2: Unit static shear loads  $P_2 = 1.0 \text{ kgf}$  (Horizontal)

**Results**

*Tip displacements in the load directions (Case 1)*



Tip displacements in the load directions (Case 2)

## Comparison of Results

Unit: in		
Results	Theoretical	MIDAS/Civil
In-Plane ( $\delta_z$ )	-0.005424	-0.005416
Out-of-Plane ( $\delta_y$ )	-0.001754	-0.001780

## Reference

MacNeal, R. H., and Harder, R. L. (1985). "A Proposed Standard Set of Problems to Test Finite Element Accuracy", Finite Element in Analysis and Design, **1**, Elsevier Science Publishers, North-Holland, 3-20.