## 1 System Model

Consider the geometric channel for the frequency selective massive multiple-input multiple-output (MIMO) composed by a set of L scattering clusters. The nth delay tap of the uth user equipment (UE) is expressed as

$$\mathbf{H}(f) = \sum_{l=1}^{L} \beta_l P(f) e^{-\jmath 2\pi f \tau_l} \mathbf{a}_{R,i}(\phi_{R,l}, \theta_{R,l}, f) \mathbf{a}_{T}^{H}(\phi_{T,l}, \theta_{T,l}, f), \tag{1}$$

Consider the transmitter and receiver beamforming filters  $\mathbf{w}_{R}$  and  $\mathbf{w}_{T}$ , respectively. The equivalent digital channel is represented as

$$G(f) = \sum_{l=1}^{L} \beta_l P(f) c_{R}(\phi_{R,l}, \theta_{R,l}, f) c_{T}(\phi_{T,l}, \theta_{T,l}, f) e^{-j2\pi f \tau_l},$$
(2)

where

$$\begin{aligned} c_{\mathrm{R}}(\phi_{\mathrm{R},l},\theta_{\mathrm{R},l},f) &= \mathbf{w}_{\mathrm{R}}^{H} \mathbf{a}_{\mathrm{R},i}(\phi_{\mathrm{R},l},\theta_{\mathrm{R},l},f) \\ &= \sum_{i=1}^{I_{R}} \mathbf{w}_{\mathrm{R}}^{*}[i] \mathrm{e}^{-\jmath \frac{2\pi}{c} \mathbf{u}^{T} \mathbf{d}_{i} f}. \end{aligned}$$