Progress:

Preliminary Investigations of Home Equity Position Markets

E. Searle-White¹ D. Baron²

¹Mills College

²Western Washington University

November 7/ BSM Research Project Progress Talks



Outline

Outline

Introduction

A few weeks ago, we began our research into home equity position markets. To start, we reviewed some relevant topics in stochastic calculus, financial analysis, and economics.

Each week, we reviewed certain literature and also began to build very basic models that incorporated what we were learning, so each week, the models grew more complex.

Reviewed Topics:

- Stochastic Calculus
 - SDEs
 - Stochastic Processes and Option Pricing
- Modern Portfolio Theory
- Prospect Theory

Outline

Outline

Stochastic Calculus

Stochastic Calculus is frequently used to model movements in markets. It relies on the evaluation of *stochastic processes*, which are processes that involve random behavior.

A stochastic (or random) process models the evolution of a system over time. Unlike in deterministic situations, in a stochastic process even if the initial condition is known, there are several directions in which the process can evolve.

Stochastic Calculus

Stochastic Calculus is frequently used to model movements in markets. It relies on the evaluation of *stochastic processes*, which are processes that involve random behavior.

A stochastic (or random) process models the evolution of a system over time. Unlike in deterministic situations, in a stochastic process even if the initial condition is known, there are several directions in which the process can evolve.

Stochastic Process

Given a probability space (Ω, F, P) and a measurable space (S, Σ) , an S-valued stochastic process is a collection of S-valued random variables on Ω , indexed by T (time). So, a stochastic or random process X is a collection:

$${X_t: t \in T}$$

Note that there are both discrete and continuous stochastic processes.

Stochastic Process

Given a probability space (Ω, F, P) and a measurable space (S, Σ) , an S-valued stochastic process is a collection of S-valued random variables on Ω , indexed by T (time). So, a stochastic or random process X is a collection:

$$\{X_t:t\in T\}$$

Note that there are both discrete and continuous stochastic processes.

Brownian Motion

In particular, we studied a kind of process called a Brownian Motion or a Wiener Process, which is a very specific kind of random walk.

One key aspect of a Brownian Motion W_t (t representing time) is the following:

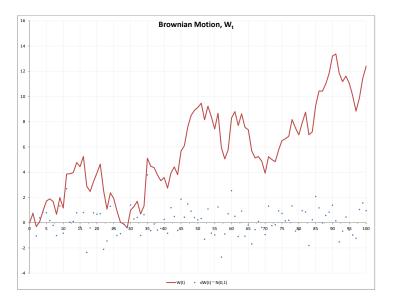
For
$$s \le t$$
, $(W_t - W_s) \sim N(0, t - s)$

Brownian Motion

In particular, we studied a kind of process called a Brownian Motion or a Wiener Process, which is a very specific kind of random walk.

One key aspect of a Brownian Motion W_t (t representing time) is the following:

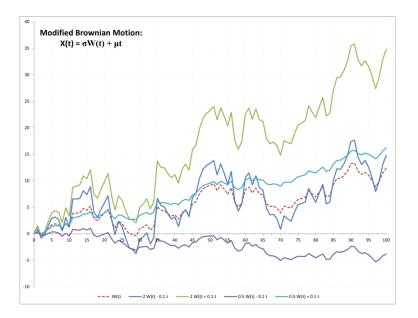
For
$$s \le t$$
, $(W_t - W_s) \sim N(0, t - s)$



Stochastic Equations

An example of a stochastic process X_t , with an underlying Brownian Motion W_t , volatility σ and drift μ is:

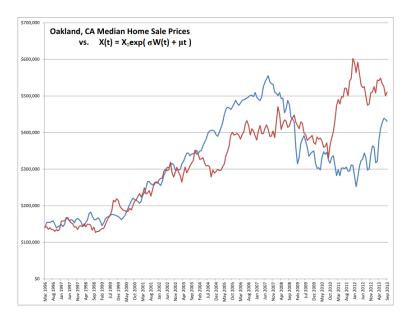
$$X_t = \int_0^t \sigma dW_s + \int_0^t \mu ds$$



Applications of Stochastic Processes

One application of such processes is to model home prices over a given time period.

It is known that the lognormal distribution is very accurate for modeling such prices.



Applications to the Model

These and other topics in stochastic calulus helped us to model home appreciation in certain neighborhoods, given that area's volitility, etc. We used this to track the growth of a home's value in relation to the growth of the neighborhoodappreciation in our first model.

Outline

Portfolio Theory Classic and Modern Approaches

Portfolio Theory attempts to organize and quantify exactly what the optimal 'portfolio' or bundle of assets for any given investor will be.

In Portfolio Theory, the goal is to correctly structure a group of investments to optimize gain while avoiding risk.

- Correlation
- Diversification

Portfolio Theory Classic and Modern Approaches

Portfolio Theory attempts to organize and quantify exactly what the optimal 'portfolio' or bundle of assets for any given investor will be.

In Portfolio Theory, the goal is to correctly structure a group of investments to optimize gain while avoiding risk.

- Correlation
- Diversification

Portfolio Theory Classic and Modern Approaches

Portfolio Theory attempts to organize and quantify exactly what the optimal 'portfolio' or bundle of assets for any given investor will be.

In Portfolio Theory, the goal is to correctly structure a group of investments to optimize gain while avoiding risk.

- Correlation
- Diversification

- Investors are rational and always risk-averse.
- Each investor will tolerate a certain amount of risk in exchange for a return above the *risk-free* return.
- Through these preferences, we can construct a function to determine the optimal portfolio of an investor in terms of risk and return.

- Investors are rational and always risk-averse.
- Each investor will tolerate a certain amount of risk in exchange for a return above the *risk-free* return.
- Through these preferences, we can construct a function to determine the optimal portfolio of an investor in terms of risk and return.

- Investors are rational and always risk-averse.
- Each investor will tolerate a certain amount of risk in exchange for a return above the *risk-free* return.
- Through these preferences, we can construct a function to determine the optimal portfolio of an investor in terms of risk and return.

- Investors are rational and always risk-averse.
- Each investor will tolerate a certain amount of risk in exchange for a return above the *risk-free* return.
- Through these preferences, we can construct a function to determine the optimal portfolio of an investor in terms of risk and return.

Indifference Curves

indifference curve picture

Correlation and Diversification

If R_p is the return of a given portfolio, R_i the return on a specific asset and w_i the weight of asset i (i.e. the proportion of asset i in the portfolio), we have

$$E(R_p) = \sum_i w_i E(R_i)$$

and the return variance of the portfolio σ_p^2 where

$$\sigma_p^2 = \sum_i w_i^2 \sigma_i^2 + \sum_i \sum_{i \neq j} w_i w_j \sigma_i \sigma_j \rho_{ij}$$

Where ρ_{ij} is the correlation coefficient between assets *i* and *j*.

Applications to the Model

Correlation and Diversification, cont'd

Though all home equity positionare part of the same market, each individual home equity position will have its own volatility and trends depending on where the underlying home is located.

How do local city economies affect other local economies?

Outline

Prospect Theory

The drawbacks of classic portfolio theory are obvious even to an outsider. Prospect theory attempts to uncover and mathematically describe some of the *irrational* behaviors exhibited by investors.

Prospect Theory suggests that when examining a risky prospect, there is an *editing process* investors go through to evaluate the decision at hand.

Prospect Theory

The drawbacks of classic portfolio theory are obvious even to an outsider. Prospect theory attempts to uncover and mathematically describe some of the *irrational* behaviors exhibited by investors.

Prospect Theory suggests that when examining a risky prospect, there is an *editing process* investors go through to evaluate the decision at hand.

Anomalies in Decision Making

- Certainty Effect
- Effect of Small Probabilities
- Framing Effect
- Isolation Effect

Anomalies in Decision Making

- Certainty Effect
- Effect of Small Probabilities
- Framing Effect
- Isolation Effect

Anomalies in Decision Making

- Certainty Effect
- Effect of Small Probabilities
- Framing Effect
- Isolation Effect

Anomalies in Decision Making

- Certainty Effect
- Effect of Small Probabilities
- Framing Effect
- Isolation Effect

Anomalies in Decision Making

- Certainty Effect
- Effect of Small Probabilities
- Framing Effect
- Isolation Effect

- How do investors evaluate a home before they purchase a home equity position?
- How do investors evaluate potential trades of home equity positions?
- How do homebuyers evaulate the outcomes related to selling an equity position in their home?

- How do investors evaluate a home before they purchase a home equity position?
- How do investors evaluate potential trades of home equity positions?
- How do homebuyers evaulate the outcomes related to selling an equity position in their home?

- How do investors evaluate a home before they purchase a home equity position?
- How do investors evaluate potential trades of home equity positions?
- How do homebuyers evaulate the outcomes related to selling an equity position in their home?

- How do investors evaluate a home before they purchase a home equity position?
- How do investors evaluate potential trades of home equity positions?
- How do homebuyers evaulate the outcomes related to selling an equity position in their home?

- How do investors evaluate a home before they purchase a home equity position?
- How do investors evaluate potential trades of home equity positions?
- How do homebuyers evaulate the outcomes related to selling an equity position in their home?

Outline

We have created three simple models thus far.

- First Model: One neighborhood, one home.
- Second Model: Three neighborhoods, three homes.
- Third Model: Three neighborhoods, three homes, one investor.

We have created three simple models thus far.

- First Model: One neighborhood, one home.
- Second Model: Three neighborhoods, three homes.
- Third Model: Three neighborhoods, three homes, one investor.

Outline

- When might homeowners sell homes?
- How can we model defaults by homeowners?
- Begin to model the secondary market.
 - Start with two investors (different preferences), one home in question.

- When might homeowners sell homes?
- How can we model defaults by homeowners?
- Begin to model the secondary market.
 - Start with two investors (different preferences), one home in question.

- When might homeowners sell homes?
- How can we model defaults by homeowners?
- Begin to model the secondary market.
 - Start with two investors (different preferences), one home in question.

- When might homeowners sell homes?
- How can we model defaults by homeowners?
- Begin to model the secondary market.
 - Start with two investors (different preferences), one home in question.

- How do we model the relationship between investor preferences and home prices?
- What kind of bubbles can we expect? How can we accurately model those?

Outline

Questions?

Thank you for your time and attention.

We appreciate the opportunity to pursue this research at BSM. We are grateful in particular to our project advisors Dezső and Rozi Miklos.

Reviewed Works

- Baxter M., Rennie A. Financial Calculus: An Introduction to Derivative Pricing. Cambridge, UK. Cambridge University Press. 1996.
- Hull, J. *Options, Futures, and Other Derivatives*. Upper Saddle River, NJ: Pearson Education, Inc; 2009.
- Miklos, R. "Prospect Theory and its Financial Applications". Universiteit van Amsterdam. 2011.
- Shreve, S. *Stochastic Calculus for Finance II :Continuous-Time Models*. Pittsburgh, PA. Springer. 2008.