

Assignment_3

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R Markdown

This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see <http://rmarkdown.rstudio.com>.

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
library(caret)

## 载入需要的程辑包: ggplot2

## 载入需要的程辑包: lattice

library(class)
library(ISLR)
library(readr)
library(reshape)

##
## 载入程辑包: 'reshape'

## The following object is masked from 'package:class':
##
##      condense

DF <- read_delim(file = 'UniversalBank.csv', delim=',')

## Rows: 5000 Columns: 14

## -- Column specification -----
##
## Delimiter: ","
## dbl (14): ID, Age, Experience, Income, ZIP Code, Family, CCAvg, Education,
##           M...
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

```

DF <- rename(DF, c('CreditCard'='CC', `Personal Loan` = 'PL', 'Securities Account'='SA', 'CD Account'='CDA'))
names(DF)

## [1] "ID"          "Age"          "Experience"   "Income"       "ZIP Code"
## [6] "Family"      "CCAvg"        "Education"    "Mortgage"     "PL"
## [11] "SA"          "CDA"          "Online"       "CC"

DF$PL=as.factor(DF$PL)
summary(DF)

##           ID           Age           Experience           Income           ZIP Code
## Min.      :  1   Min.      :23.00   Min.      : -3.0   Min.      :  8.00   Min.      : 9307
## 1st Qu.:1251   1st Qu.:35.00   1st Qu.:10.0   1st Qu.: 39.00   1st Qu.:91911
## Median :2500   Median :45.00   Median :20.0   Median : 64.00   Median :93437
## Mean    :2500   Mean    :45.34   Mean    :20.1   Mean    : 73.77   Mean    :93153
## 3rd Qu.:3750   3rd Qu.:55.00   3rd Qu.:30.0   3rd Qu.: 98.00   3rd Qu.:94608
## Max.    :5000   Max.    :67.00   Max.    :43.0   Max.    :224.00   Max.    :96651
##           Family           CCAvg           Education           Mortgage           PL
## Min.      :1.000   Min.      : 0.000   Min.      :1.000   Min.      :  0.0   0:4520
## 1st Qu.:1.000   1st Qu.: 0.700   1st Qu.:1.000   1st Qu.:  0.0   1: 480
## Median :2.000   Median : 1.500   Median :2.000   Median :  0.0
## Mean    :2.396   Mean    : 1.938   Mean    :1.881   Mean    : 56.5
## 3rd Qu.:3.000   3rd Qu.: 2.500   3rd Qu.:3.000   3rd Qu.:101.0
## Max.    :4.000   Max.    :10.000   Max.    :3.000   Max.    :635.0
##           SA           CDA           Online           CC
## Min.      :0.0000   Min.      :0.0000   Min.      :0.0000   Min.      :0.000
## 1st Qu.:0.0000   1st Qu.:0.0000   1st Qu.:0.0000   1st Qu.:0.000
## Median :0.0000   Median :0.0000   Median :1.0000   Median :0.000
## Mean    :0.1044   Mean    :0.0604   Mean    :0.5968   Mean    :0.294
## 3rd Qu.:0.0000   3rd Qu.:0.0000   3rd Qu.:1.0000   3rd Qu.:1.000
## Max.    :1.0000   Max.    :1.0000   Max.    :1.0000   Max.    :1.000

```

Task A Create a pivot table for the training data with Online as a column variable, CC as a row variable, and Loan as a secondary row variable. The values inside the table should convey the count. In R use functions `melt()` and `cast()`, or function `table()`. In Python, use pandas dataframe methods `melt()` and `pivot()`.

```

Train_Index = createDataPartition(DF$PL, p=0.6, list=FALSE) # 60% reserved for Train
Train.df=DF[Train_Index,]
Validation.df=DF[-Train_Index,]

```

```
mytable <- xtabs(~ CC+PL+Online, data=Train.df)
ftable(mytable)

##      Online      0      1
## CC PL
## 0  0      778 1125
##    1      81  122
## 1  0      330  479
##    1      35   50
```

Task B Consider the task of classifying a customer who owns a bank credit card and is actively using online banking services. Looking at the pivot table, what is the probability that this customer will accept the loan offer? [This is the probability of loan acceptance (Loan = 1) conditional on having a bank credit card (CC = 1) and being an active user of online banking services (Online = 1)].

$$p(\text{PL}=1 \& \text{CC}=1 \& \text{Online}=1 \mid \text{CC}=1 \& \text{Online}=1) = 50 / (479 + 50) = 0.095$$

Task C Create two separate pivot tables for the training data. One will have Loan (rows) as a function of Online (columns) and the other will have Loan (rows) as a function of CC.

```
table(PL=Train.df$PL, Online=Train.df$Online)

##      Online
## PL      0      1
## 0 1108 1604
## 1  116  172

table(PL=Train.df$PL, CC=Train.df$CC)

##      CC
## PL      0      1
## 0 1903  809
## 1  203   85
```

Task D Compute the following quantities [$P(A \mid B)$ means “the probability of A given B”]: i. $P(\text{CC} = 1 \mid \text{Loan} = 1)$ (the proportion of credit card holders among the loan acceptors) ii. $P(\text{Online} = 1 \mid \text{Loan} = 1)$ iii. $P(\text{Loan} = 1)$ (the proportion of loan acceptors) iv. $P(\text{CC} = 1 \mid \text{Loan} = 0)$ v. $P(\text{Online} = 1 \mid \text{Loan} = 0)$ vi. $P(\text{Loan} = 0)$

- i. $P(\text{CC} = 1 \mid \text{Loan} = 1) = 83 / (205 + 83) = 0.29$
- ii. $P(\text{Online} = 1 \mid \text{Loan} = 1) = 180 / (108 + 180) = 0.625$
- iii. $P(\text{Loan} = 1) = (108 + 180 + 205 + 83) / (1117 + 1595 + 108 + 180 + 1914 + 798 + 205 + 83) = 0.096$
- iv. $P(\text{CC} = 1 \mid \text{Loan} = 0) = 798 / (1914 + 798) = 0.29$
- v. $P(\text{Online} = 1 \mid \text{Loan} = 0) = 1595 / (1117 + 1595) = 0.59$
- vi. $P(\text{Loan} = 0) = 1 - P(\text{Loan} = 1) = 0.904$

Task E Use the quantities computed above to compute the naive Bayes probability $P(\text{Loan} = 1 \mid \text{CC} = 1, \text{Online} = 1)$.

$P(CC = 1) = (798+83)/(1914+205+798+83) = 0.29$
 $P(Online = 1) = (1595+180)/(1117+108+1595+180) = 0.59$
 $P(Loan = 1 | CC = 1, Online = 1) = [P(CC = 1 | Loan = 1)P(Online = 1 | Loan = 1)P(Loan = 1)] / [P(CC = 1)P(Online = 1)]$
 $= 0.29 \cdot 0.625 \cdot 0.096 / (0.29 \cdot 0.59) = 0.10$

Task F Compare this value with the one obtained from the pivot table in (B). Which is a more accurate estimate?

Task E is more accurate.

Task G Which of the entries in this table are needed for computing $P(Loan = 1 | CC = 1, Online = 1)$? Run naive Bayes on the data. Examine the model output on training data, and find the entry that corresponds to $P(Loan = 1 | CC = 1, Online = 1)$. Compare this to the number you obtained in (E).

```

library(e1071)
nb.model<-naiveBayes (PL~CC+Online, data=Train.df)
To_Predict=data.frame(CC=1, Online = 1)
predict(nb.model,To_Predict,type='raw')

##           0           1
## [1,] 0.9042433 0.09575667

```

The result is very close to (E).

.